

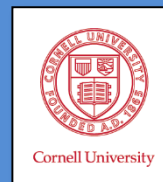
# The Fermi Surface of High- $T_c$ Superconductors

Sudipfest 2019

Brad Ramshaw

Laboratory for Atomic and Solid State Physics

Cornell University



# Collaborators

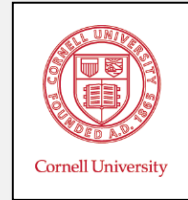
Ross McDonald  
Neil Harrison  
Mun Chan  
Jon Betts  
Zengwei Zhu  
Arkady Shekhter



Kimberly Modic



Yawen Fang



James Day  
Doug Bonn  
Walter Hardy  
Ruixing Liang



Paul Goddard  
Saman  
Ghannadzadeh



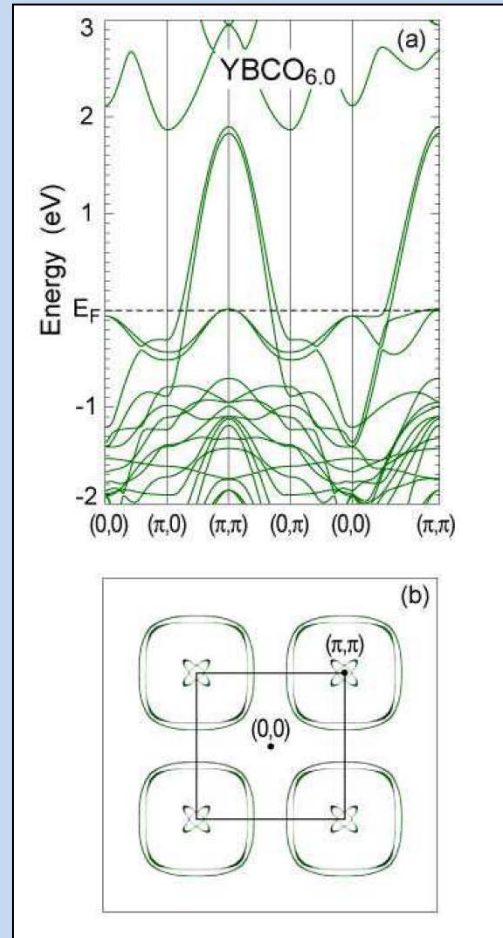
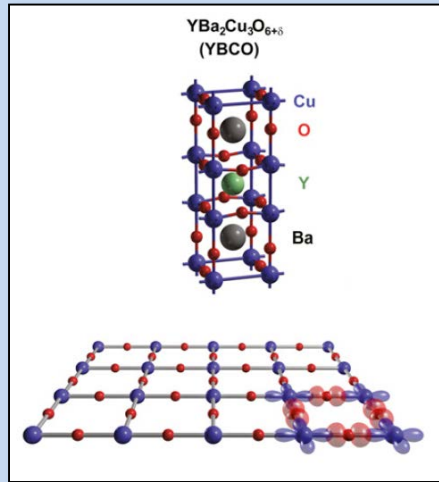
Suchitra  
Sebastian  
Beng Tam



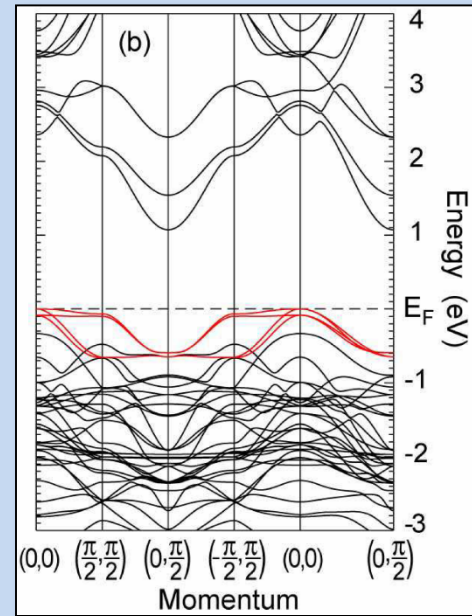
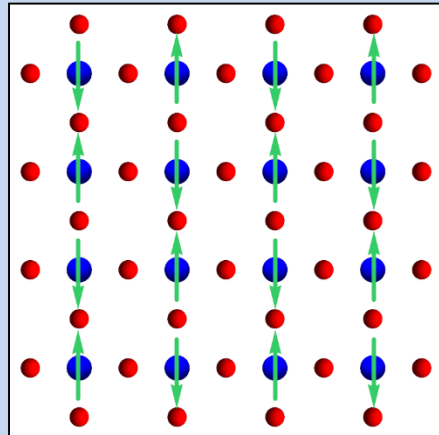
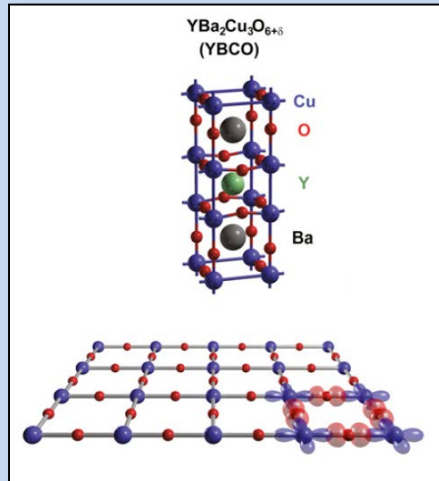
Louis Taillefer  
Gael  
Grisonnanche  
Anaëlle Legros  
Francis Laliberte



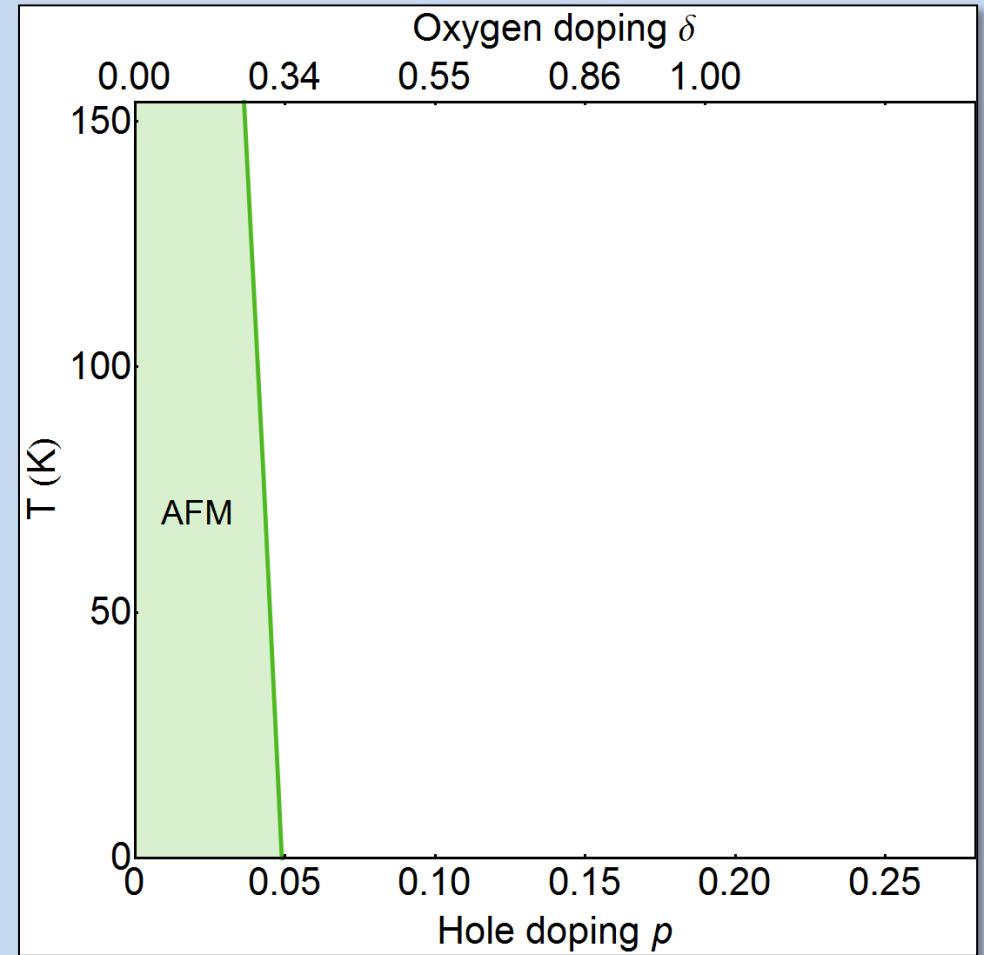
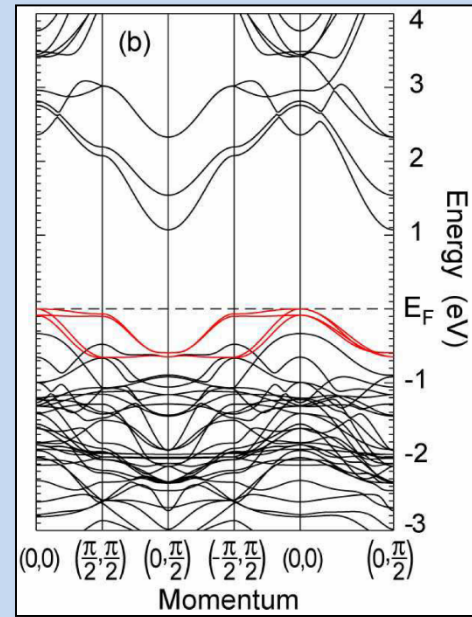
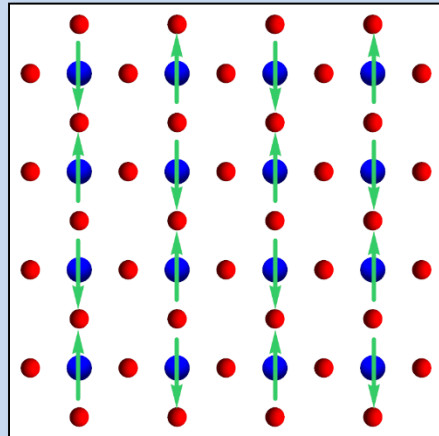
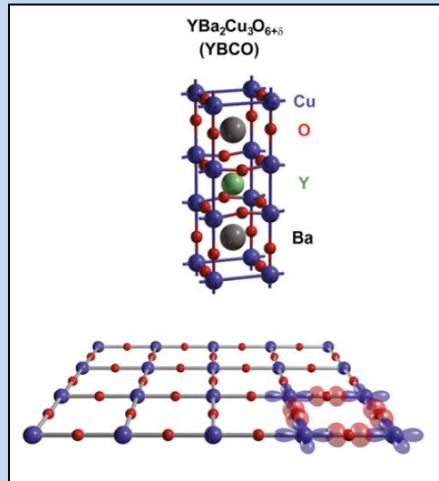
# From Insulator to Superconductor



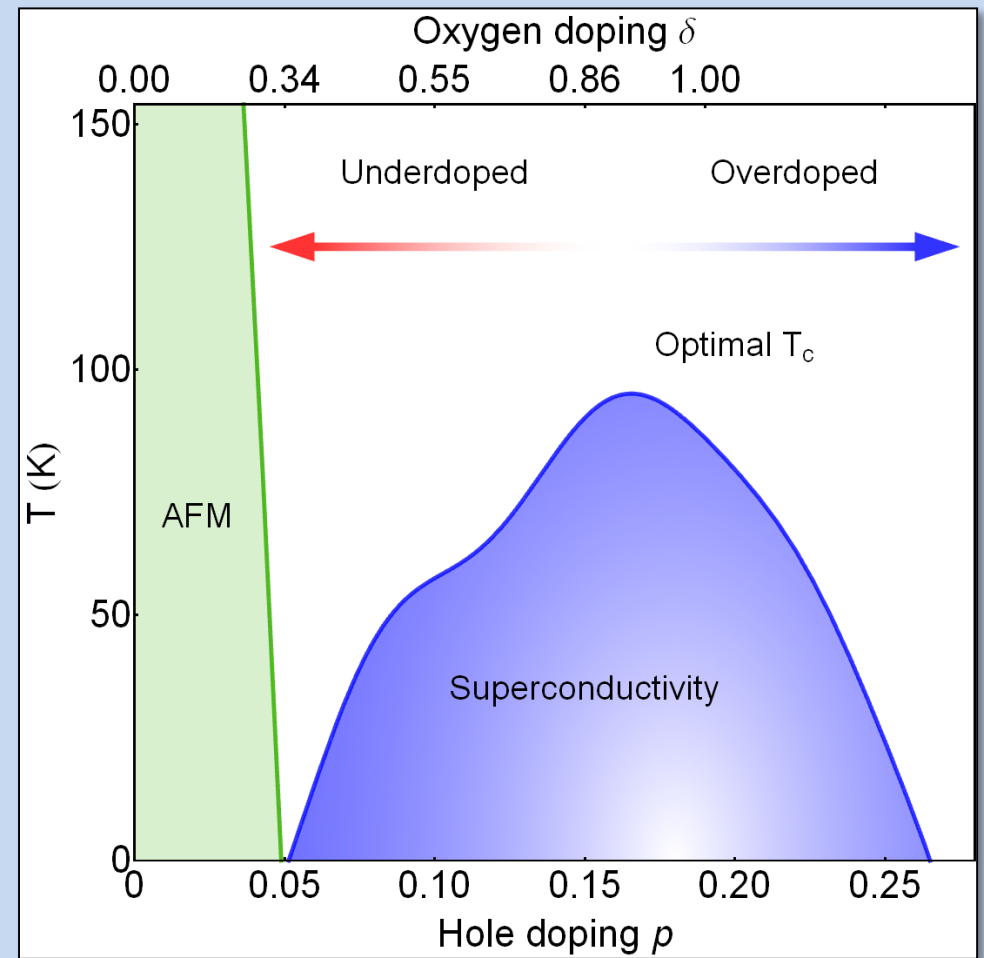
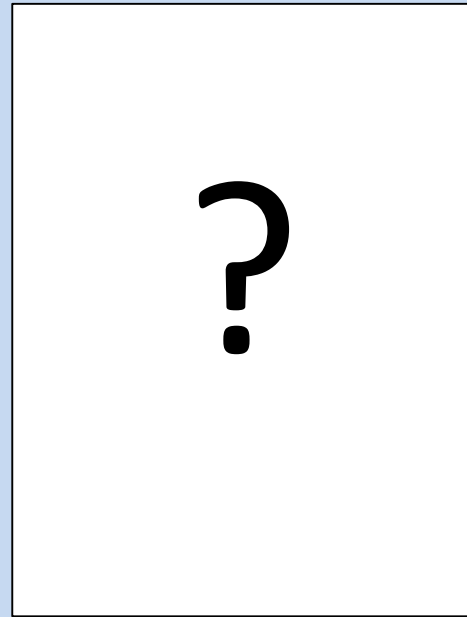
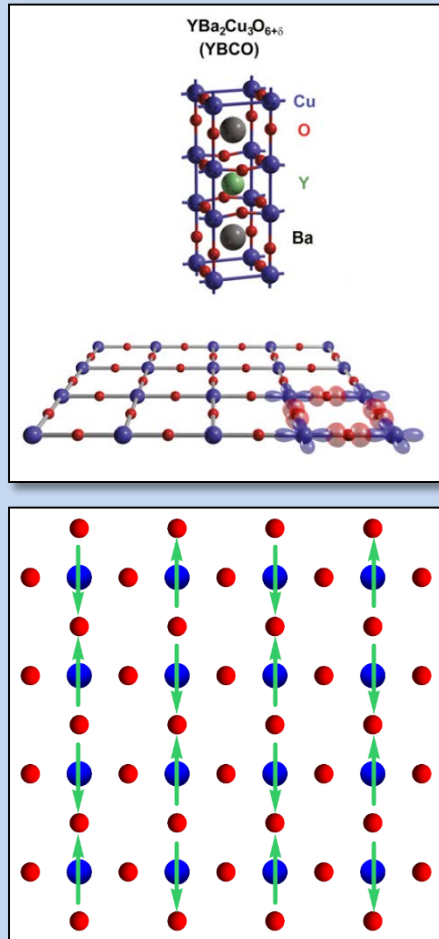
# From Insulator to Superconductor



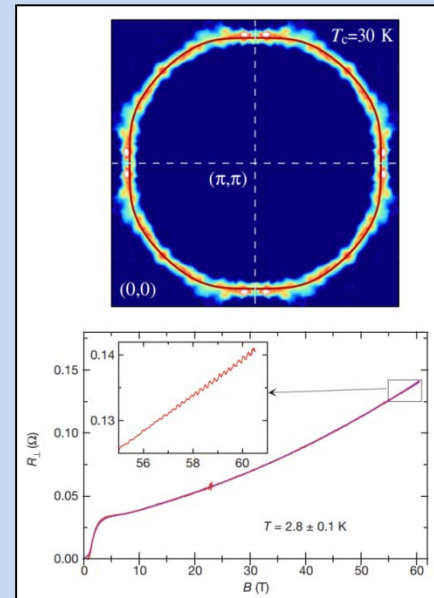
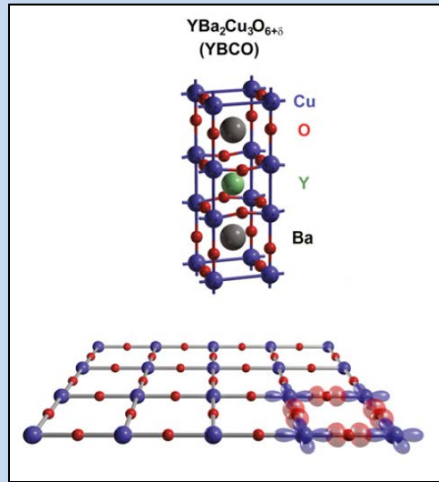
# From Insulator to Superconductor



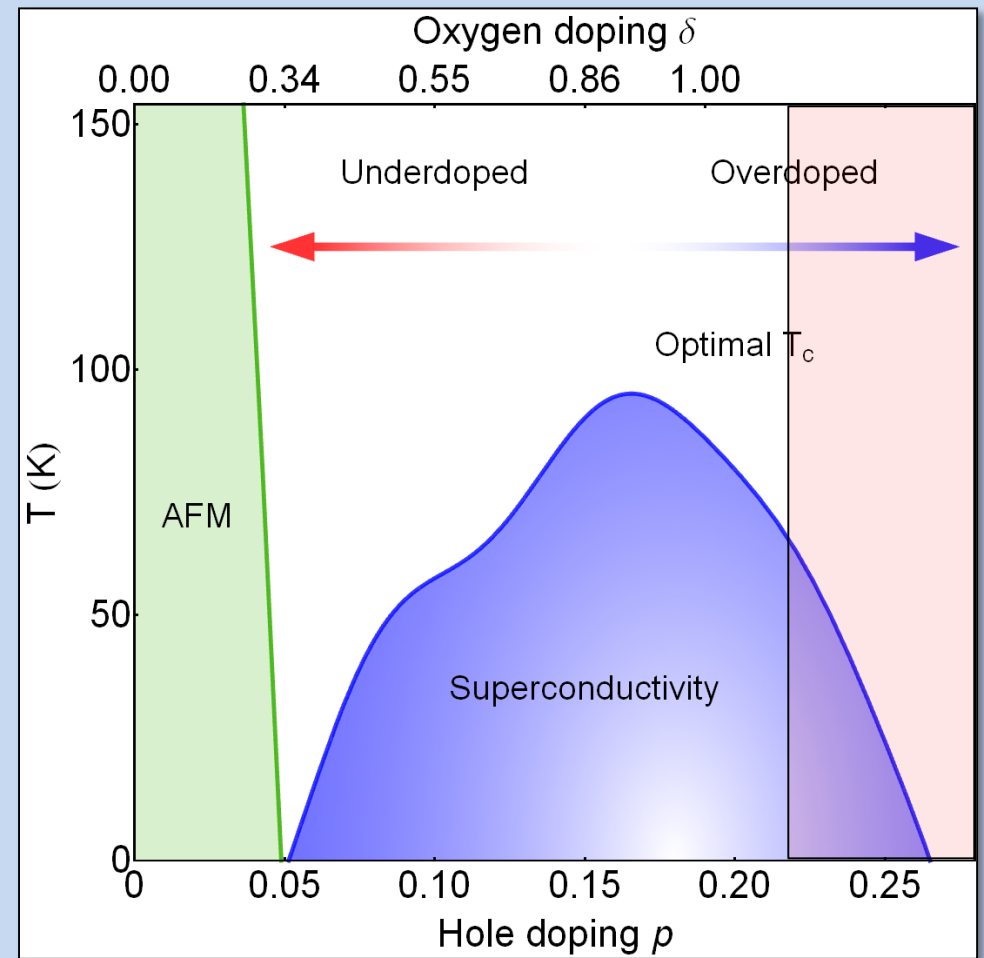
# From Insulator to Superconductor



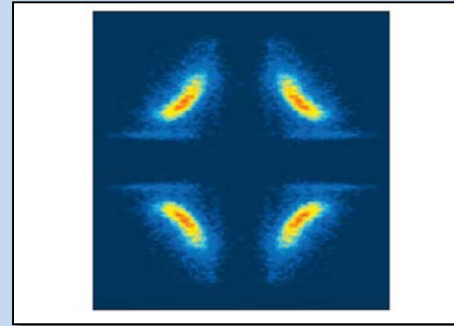
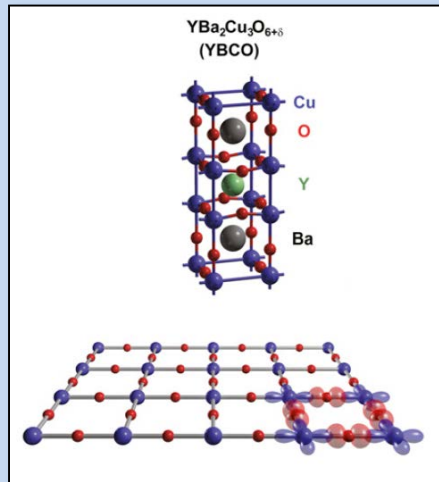
# From Insulator to Superconductor



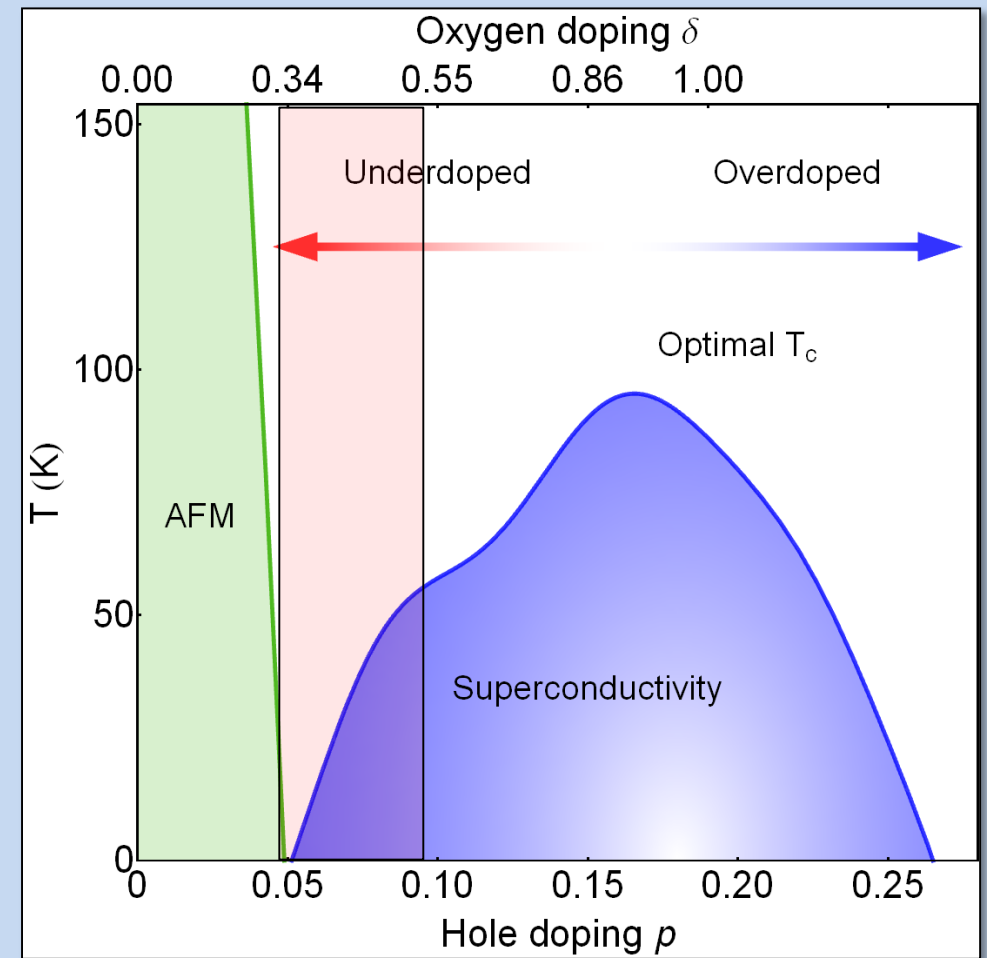
Fermi surface  
volume is  $1+p$



# From Insulator to Superconductor

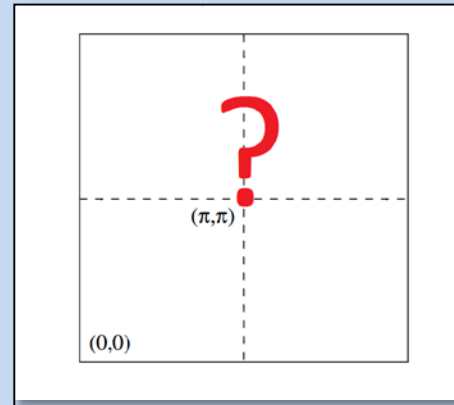
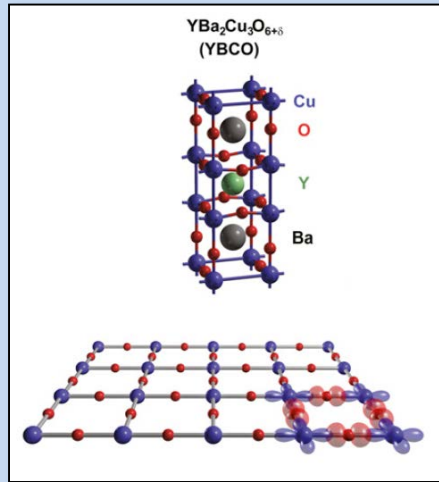


Hall effect indicates  $p$  holes at low doping

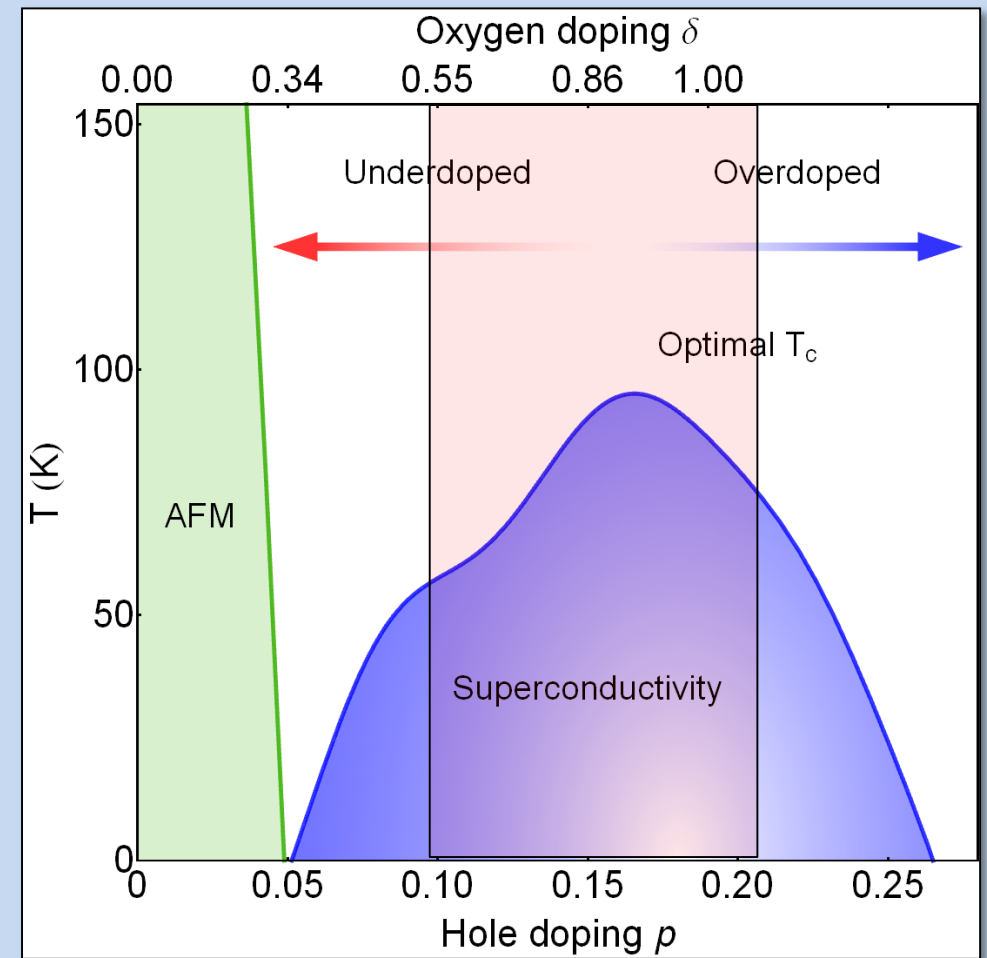




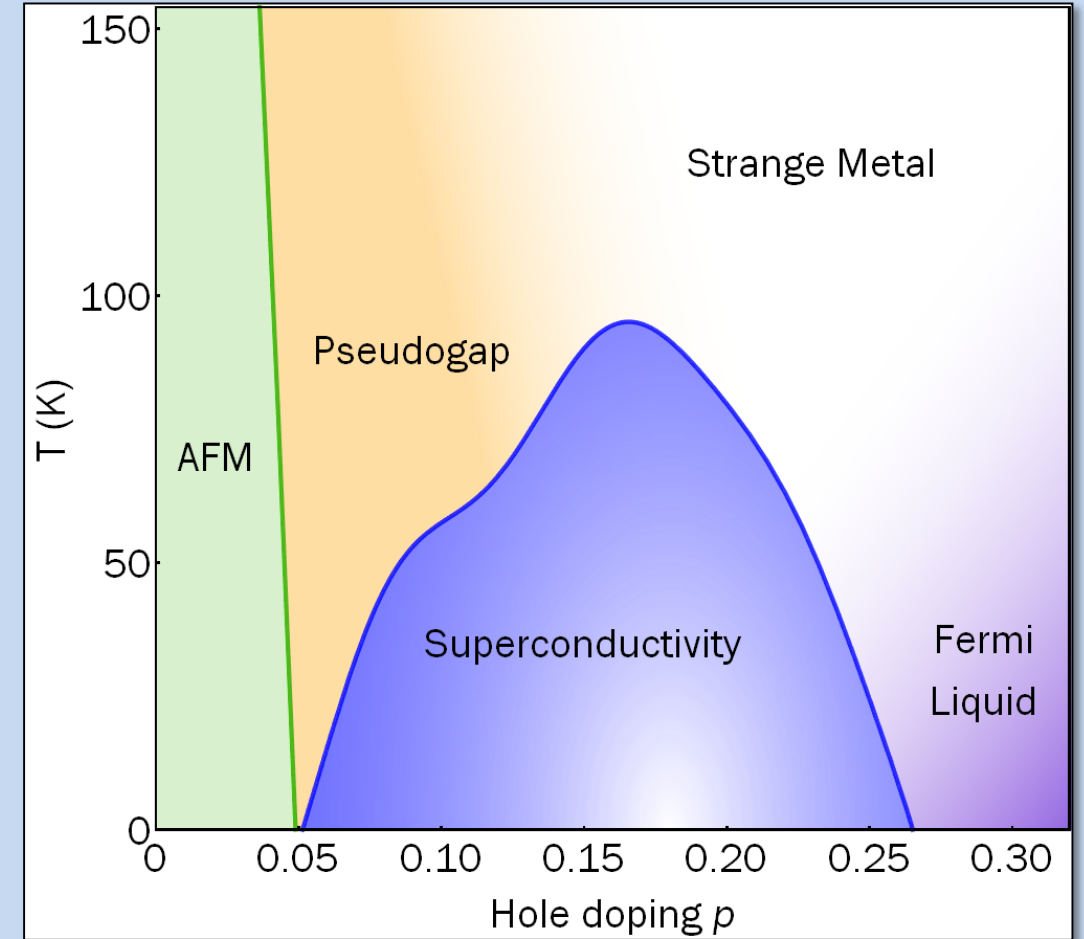
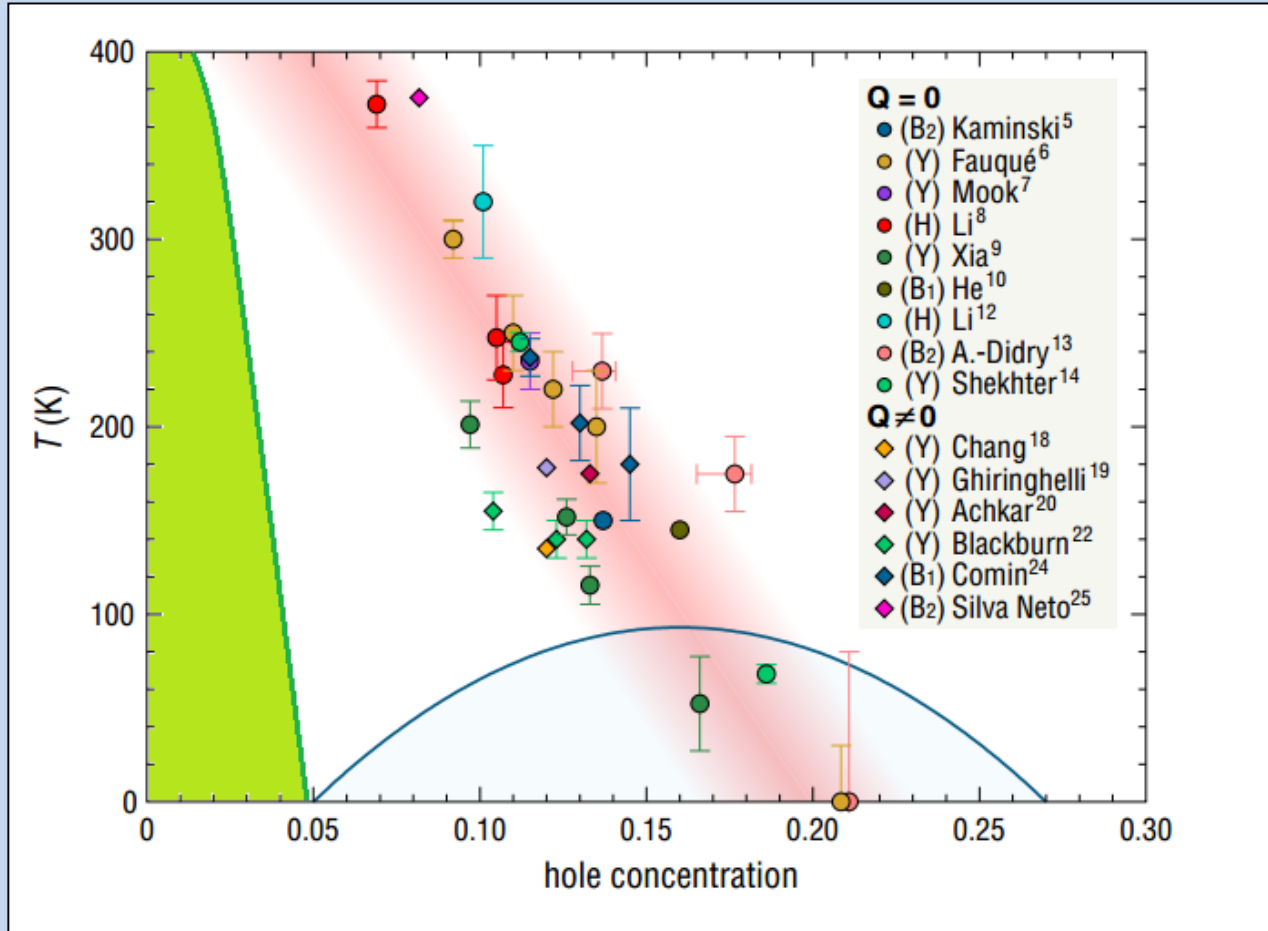
# From Insulator to Superconductor



How to get from  $p$  to  $1+p$  ?

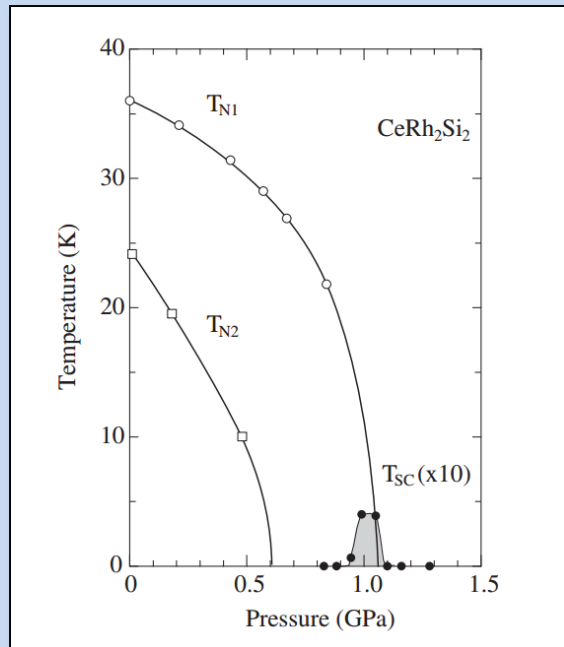


# Broken Symmetry in the Phase Diagram

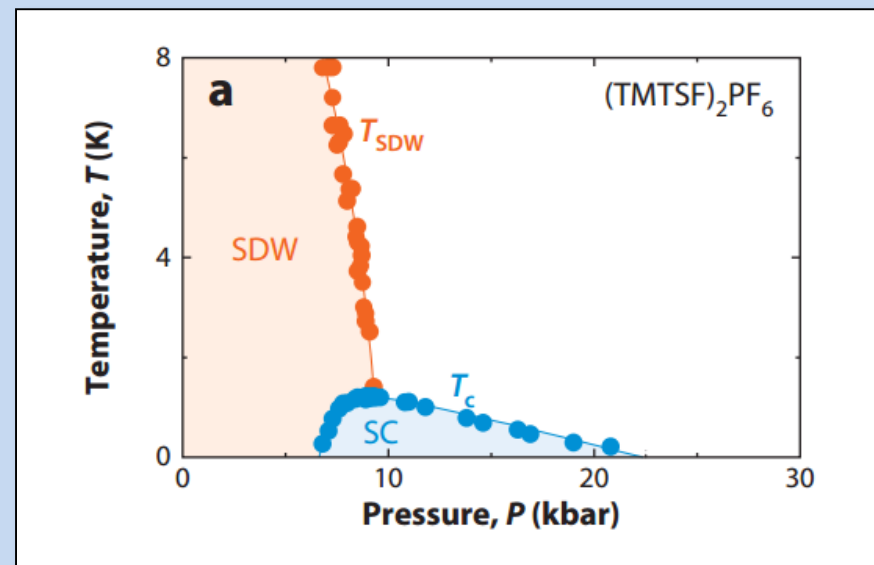


# Broken Symmetry and Unconventional Superconductivity

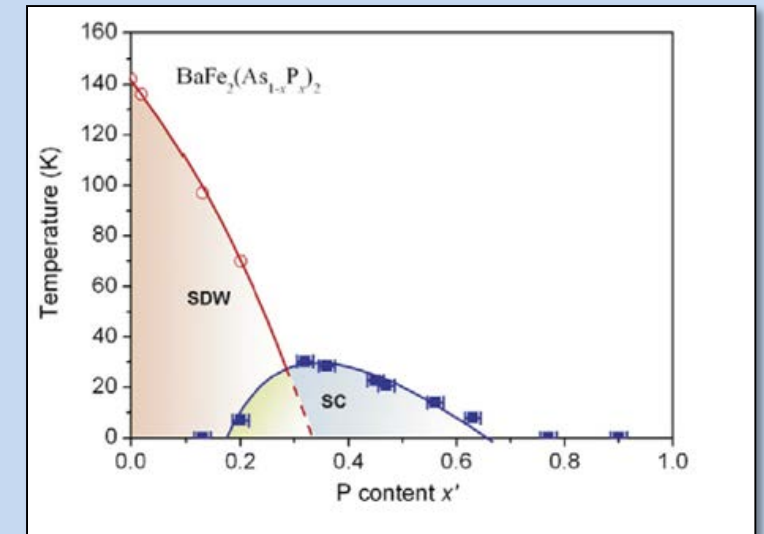
## Heavy Fermions



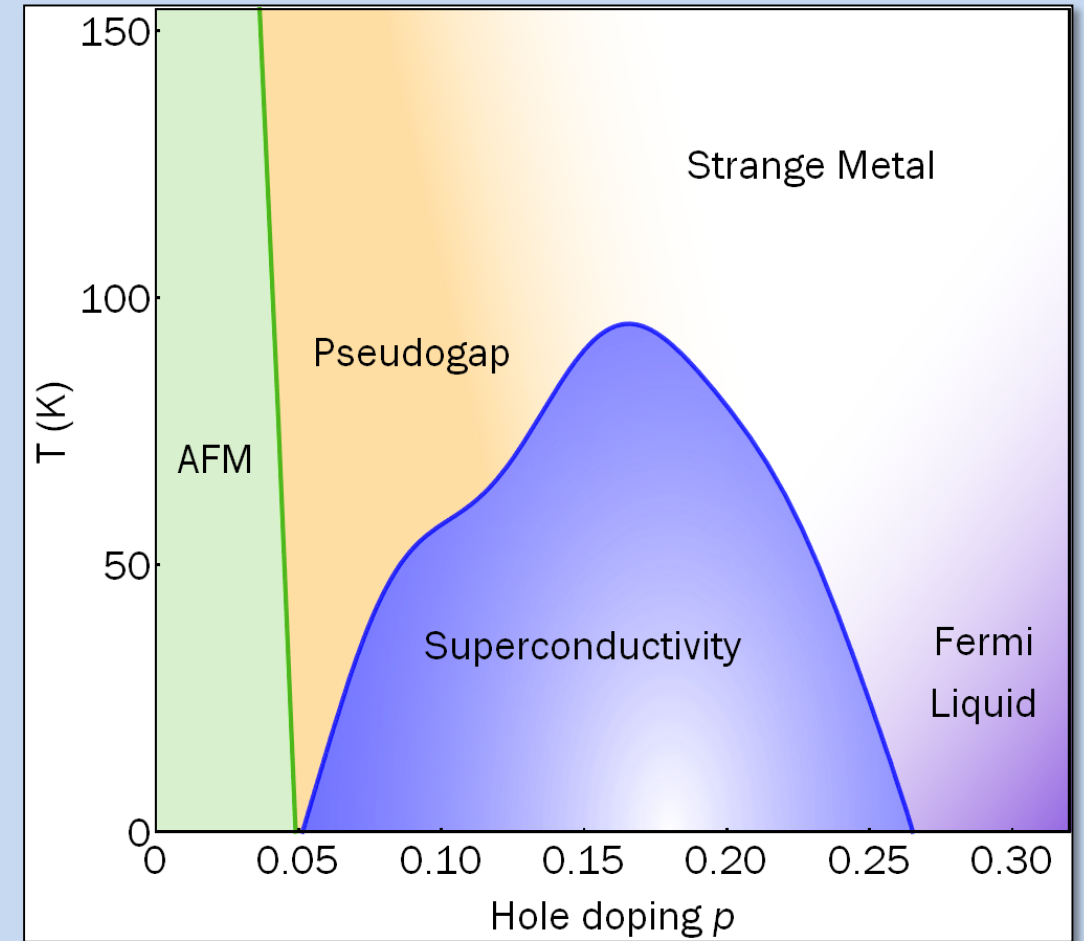
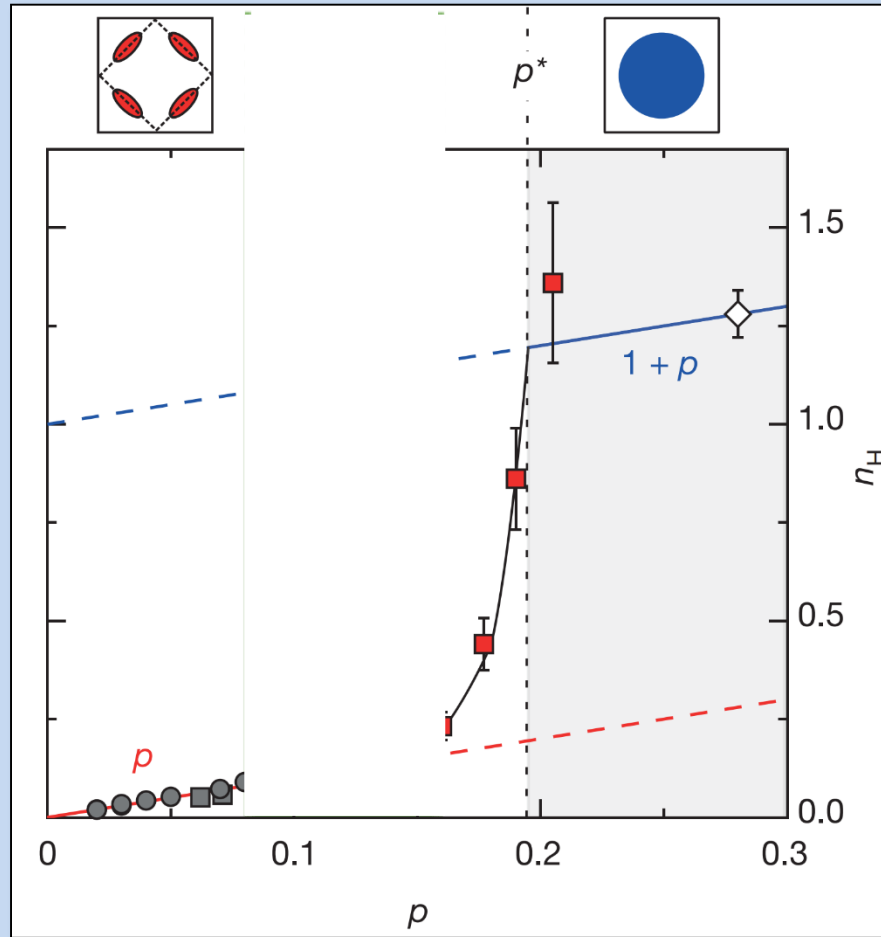
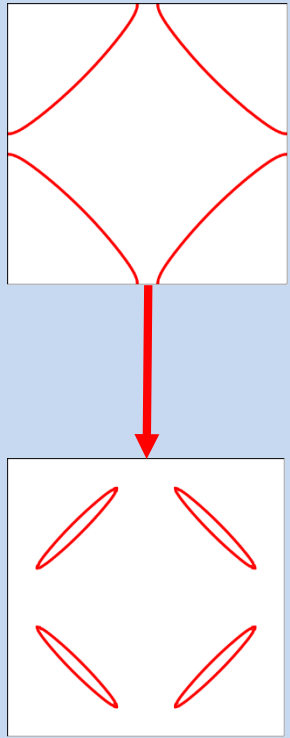
## Organics



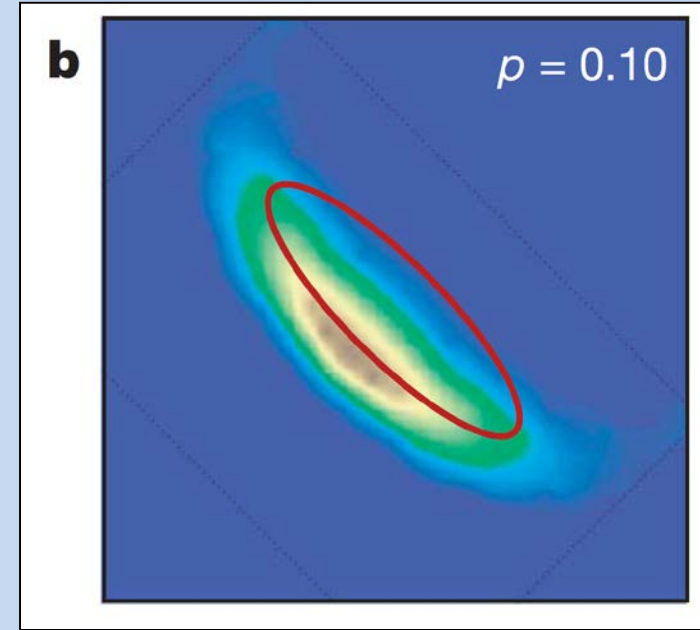
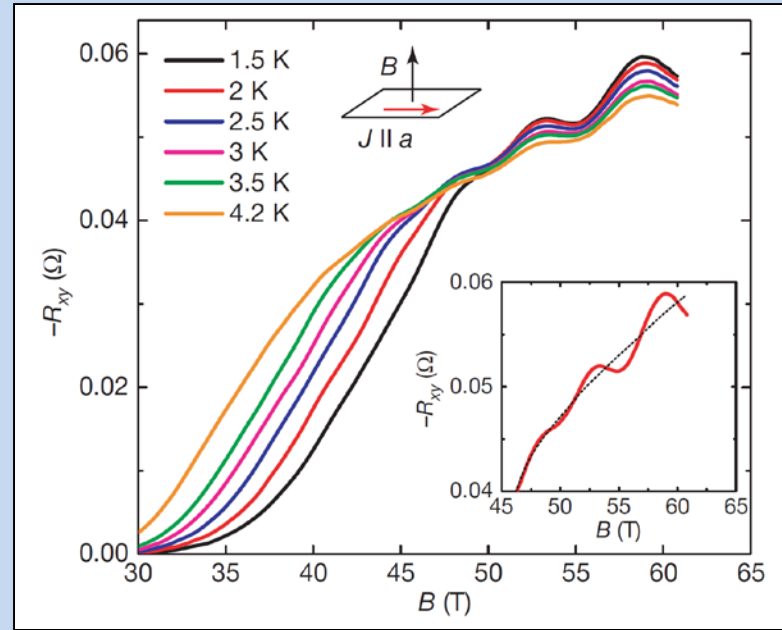
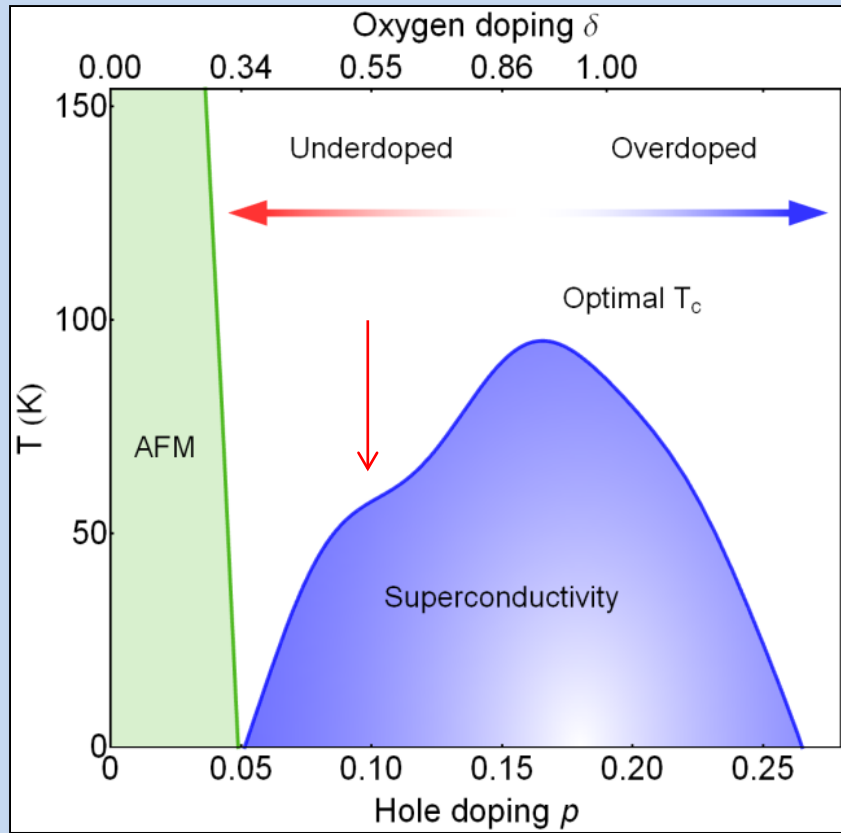
## Iron Arsenides



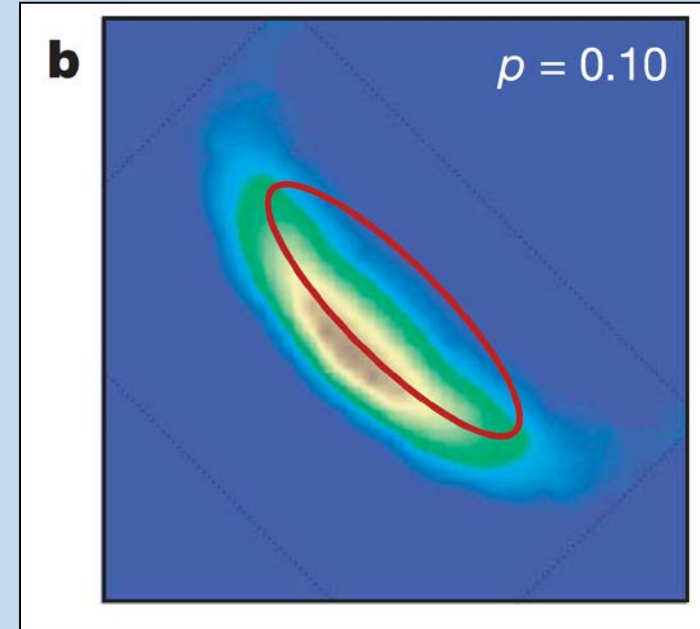
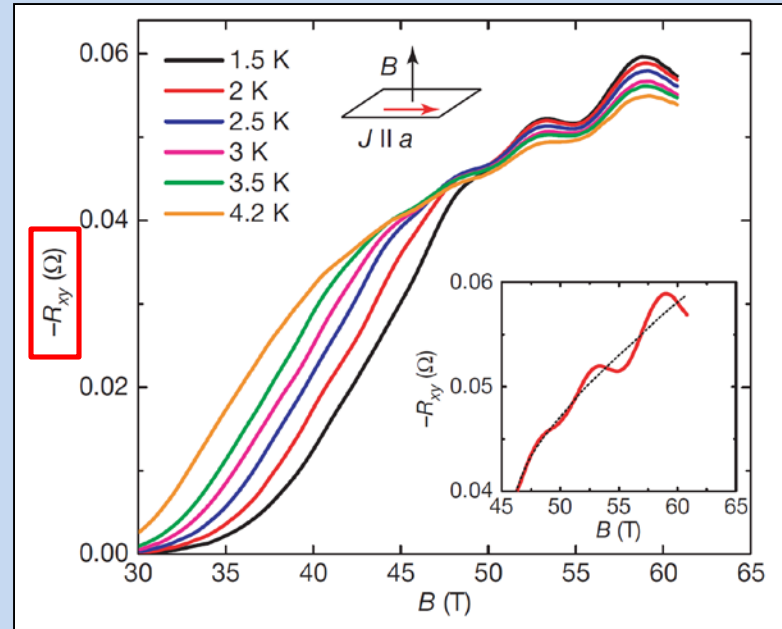
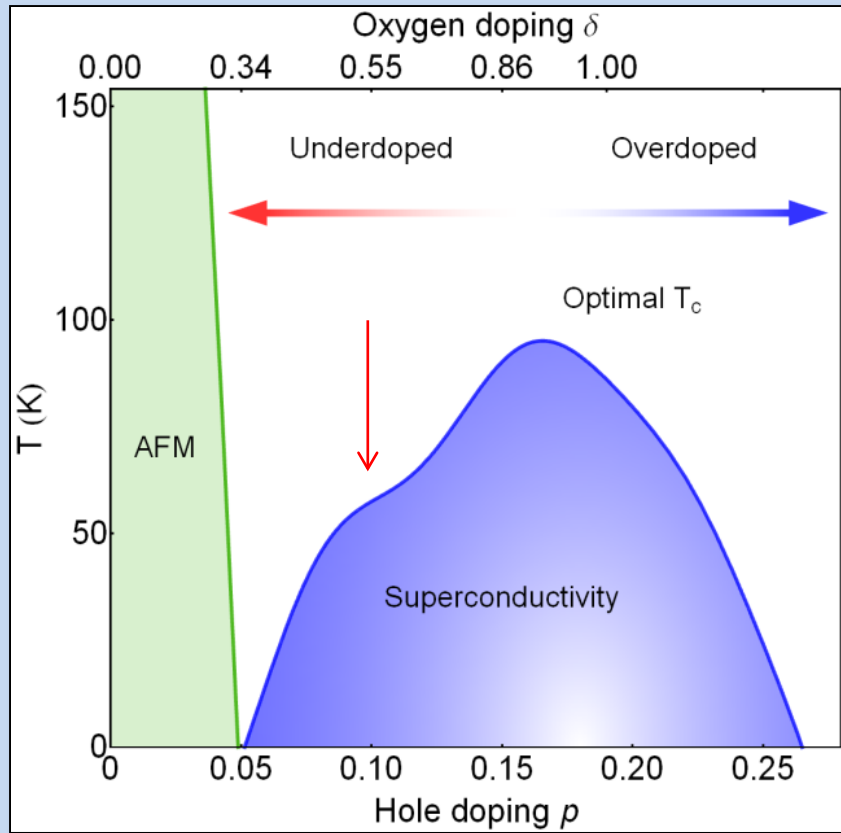
# From Insulator to Superconductor



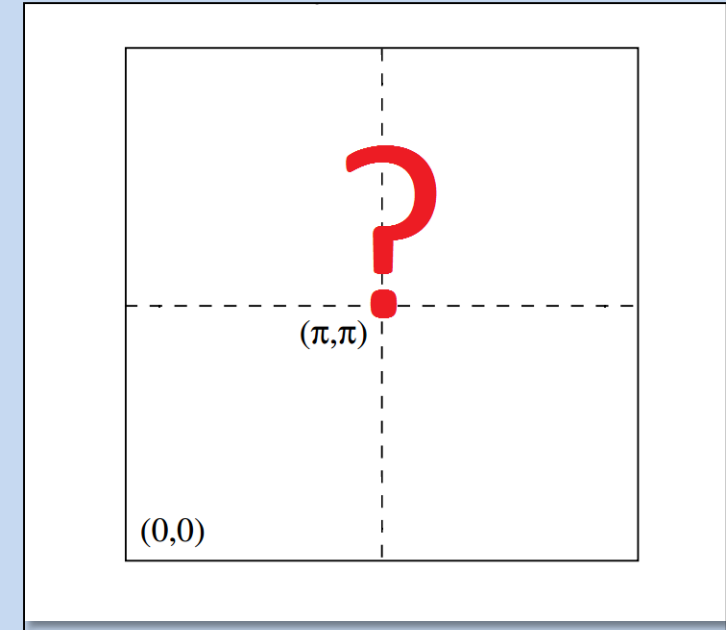
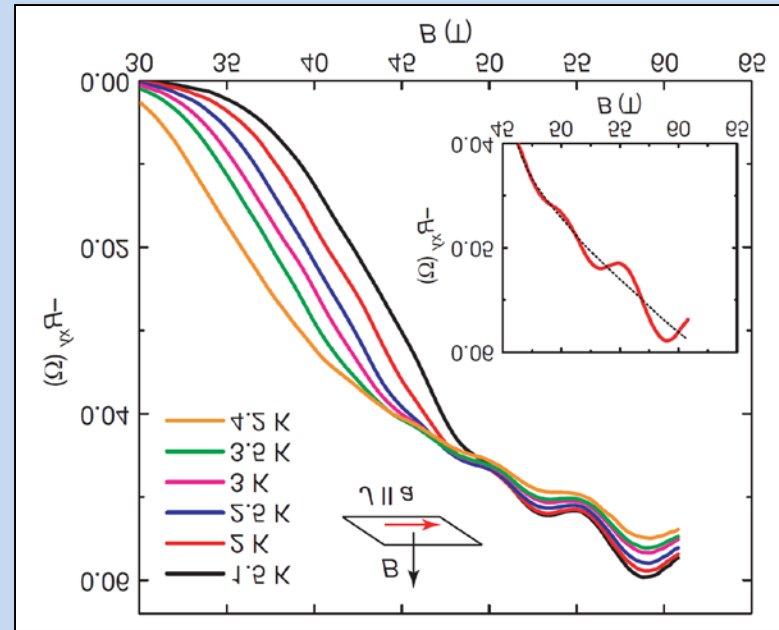
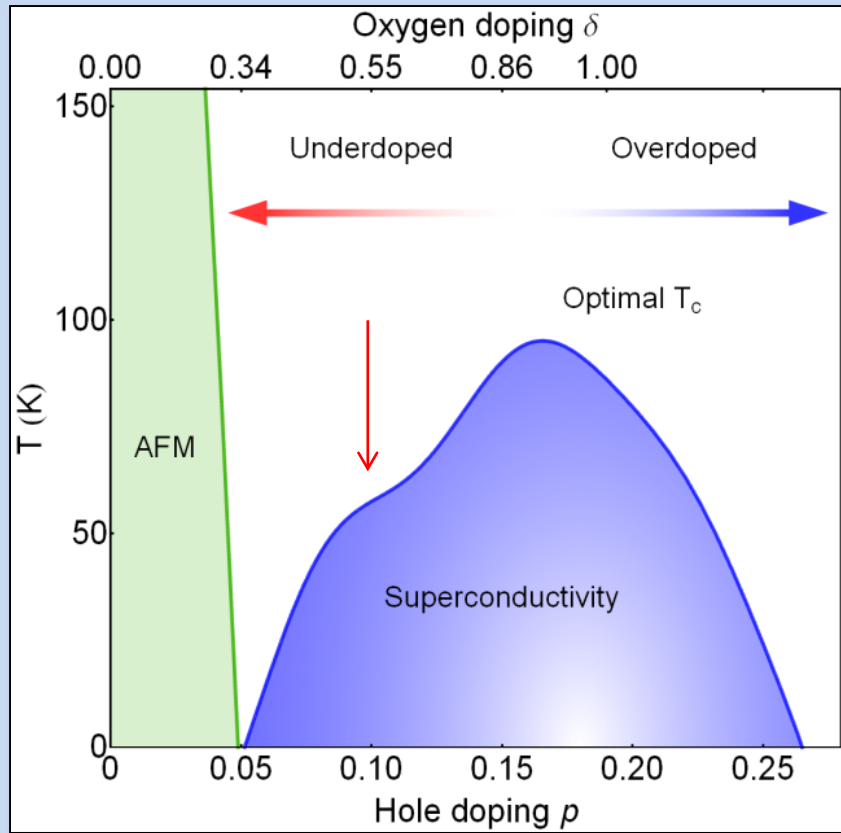
# Small Fermi Surface in $\text{YBa}_2\text{Cu}_3\text{O}_{6.52}$



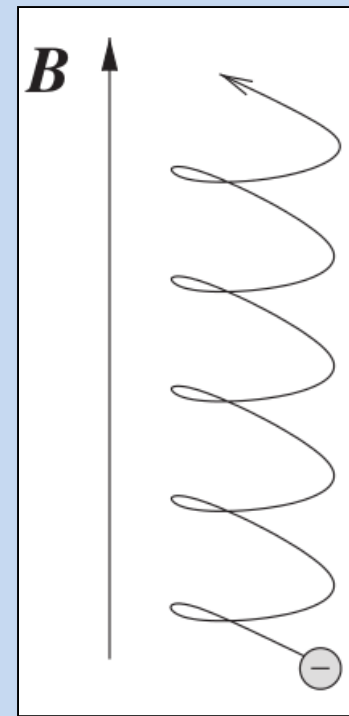
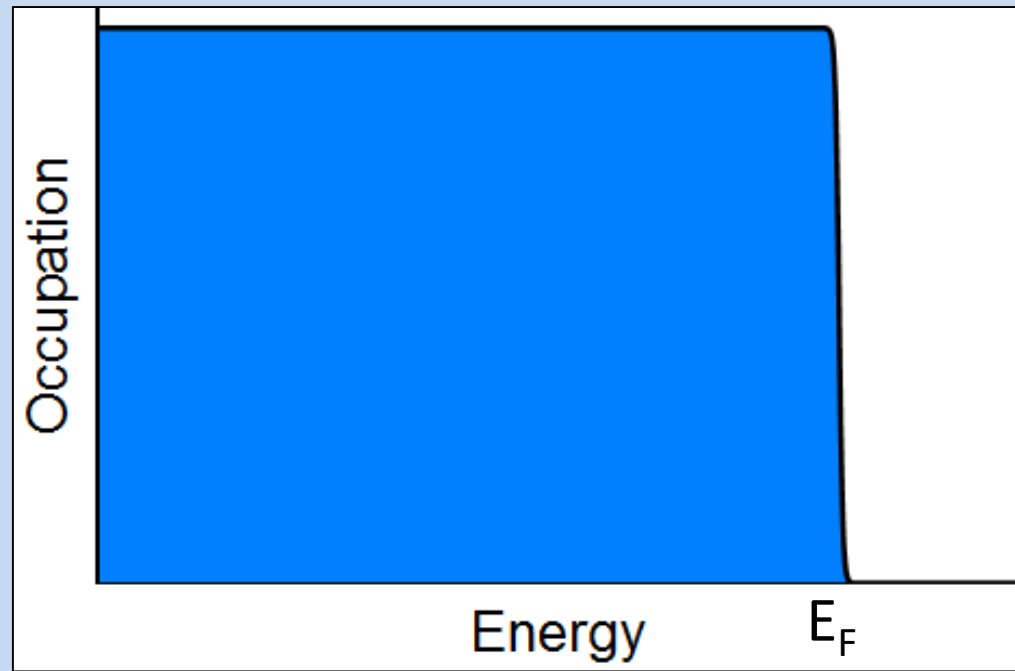
# Small Fermi Surface in $\text{YBa}_2\text{Cu}_3\text{O}_{6.52}$



# Electron Pocket in $\text{YBa}_2\text{Cu}_3\text{O}_{6.52}$

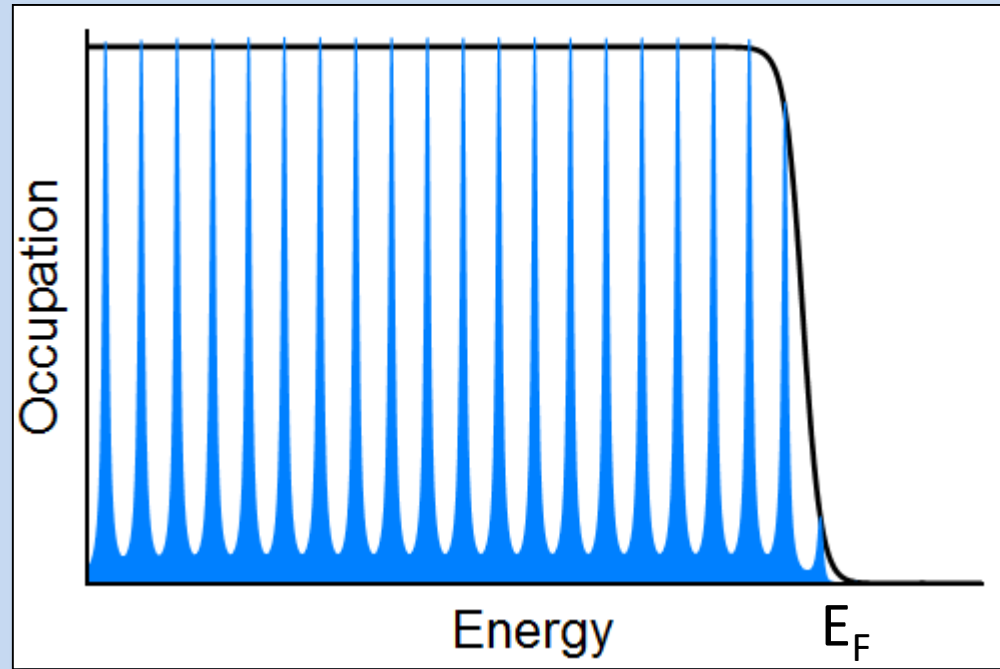


# Introduction to Quantum Oscillations

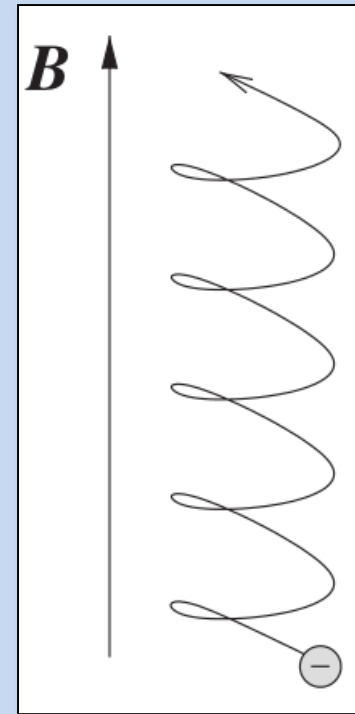




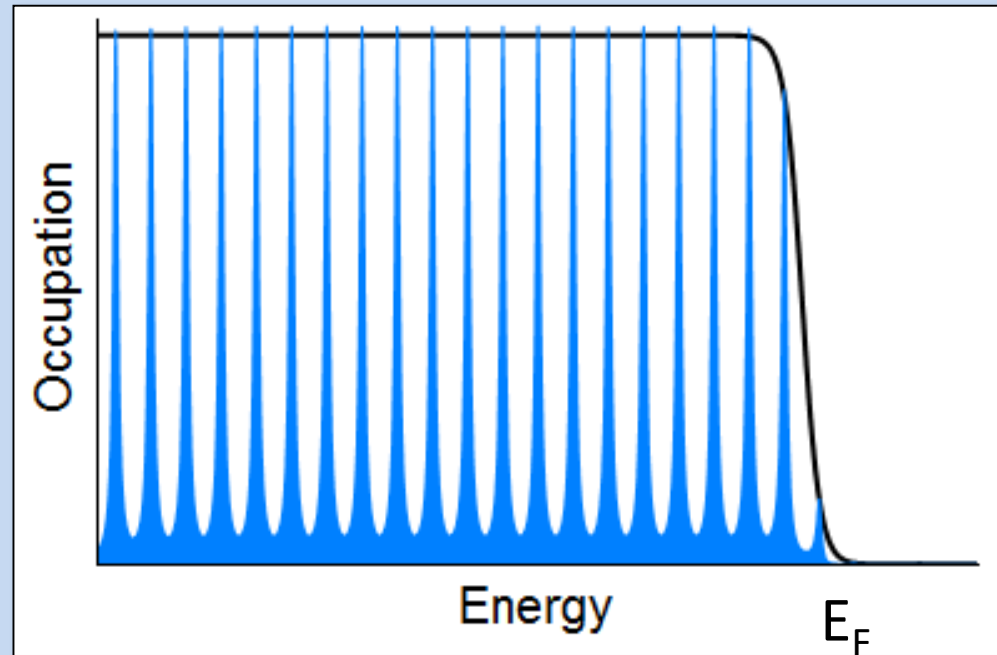
# Introduction to Quantum Oscillations



$$E_n = \hbar\omega_c \left( n + \frac{1}{2} \right)$$
$$\omega_c = \frac{eB}{m^*}$$

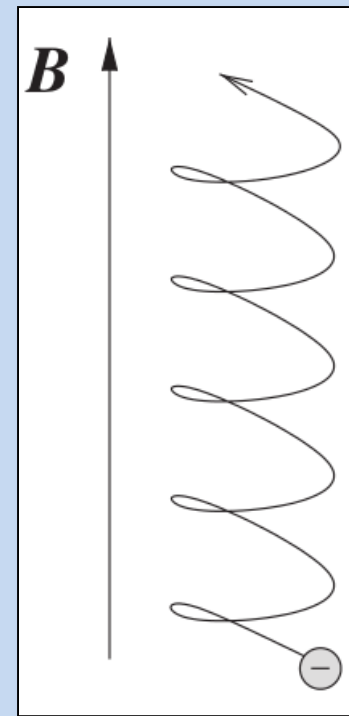


# Introduction to Quantum Oscillations

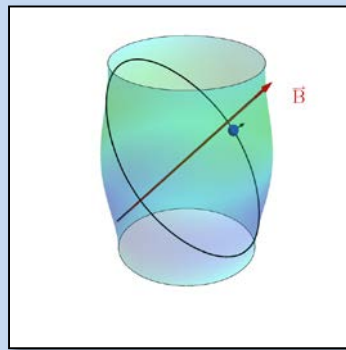
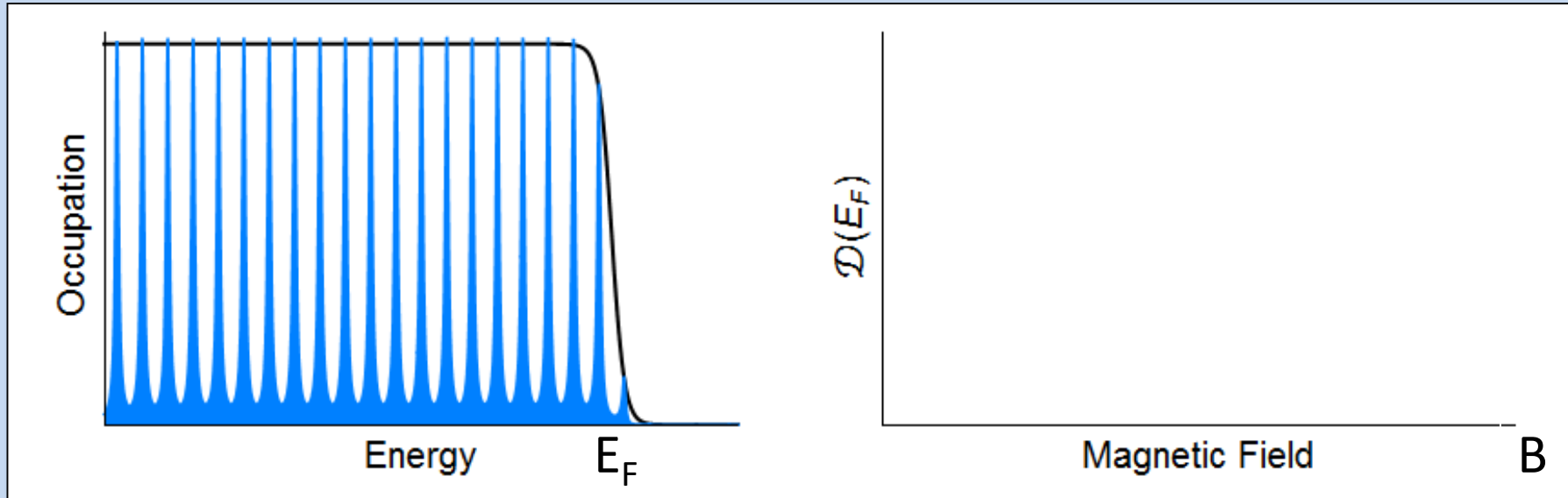


$$E_n = \hbar \omega_c \left( n + \frac{1}{2} \right)$$

$$\omega_c = \frac{eB}{m^*}$$

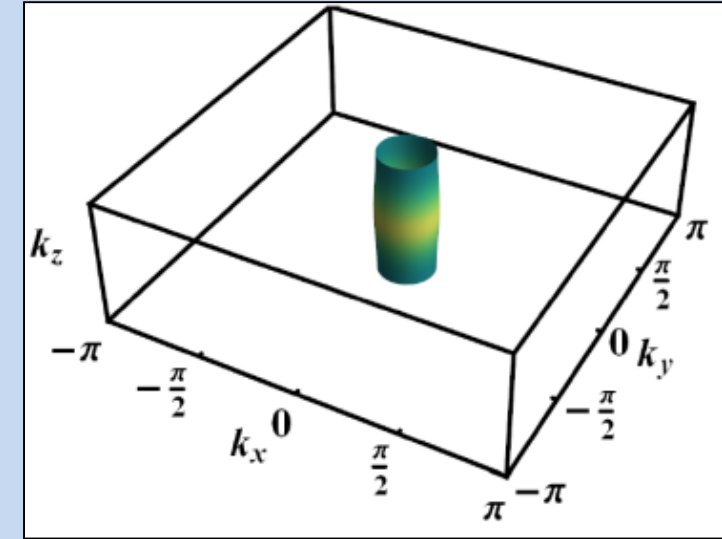
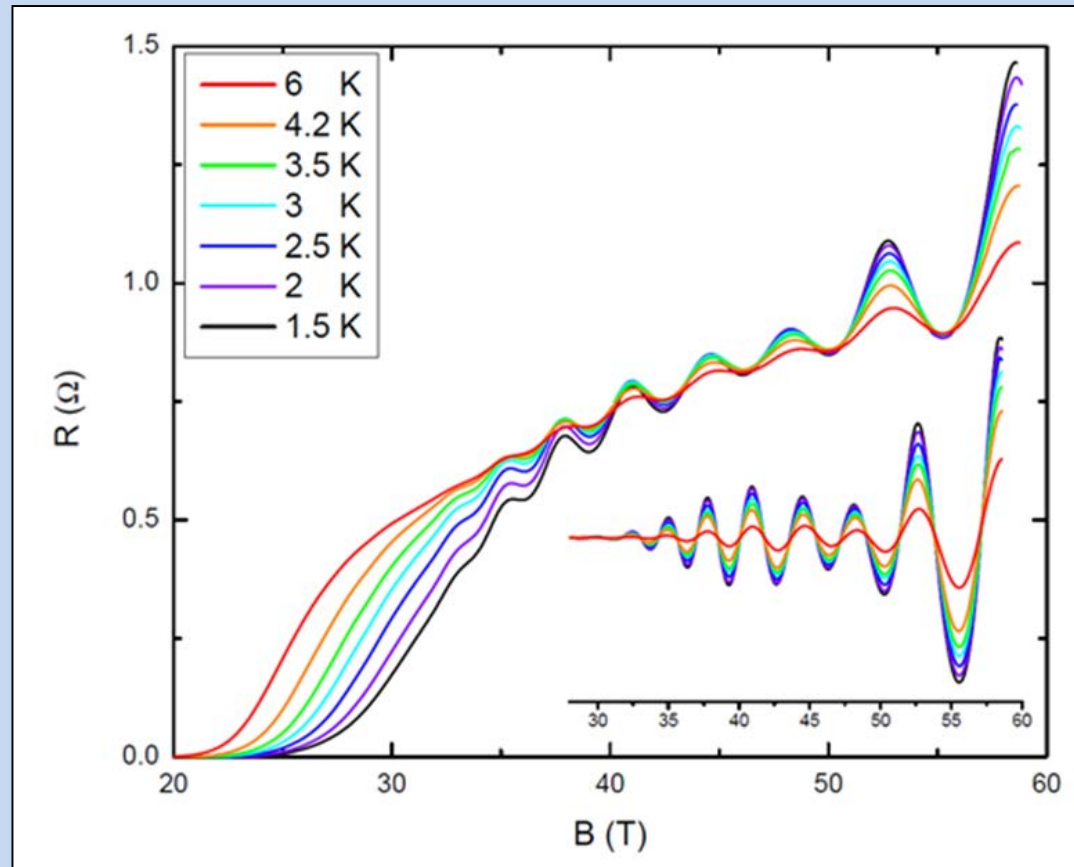
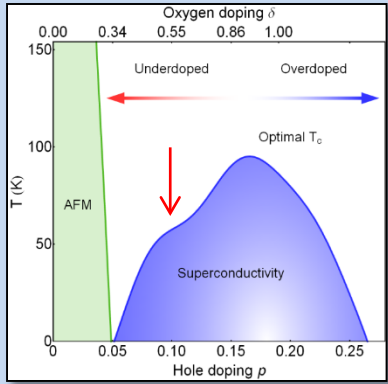


# Introduction to Quantum Oscillations



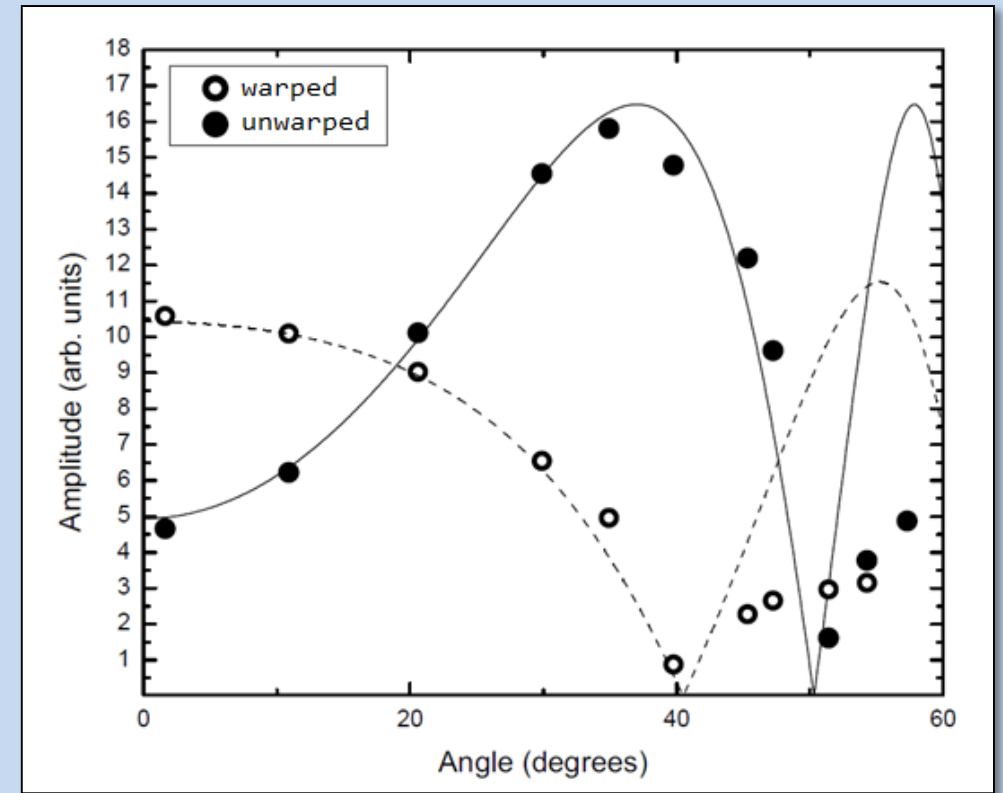
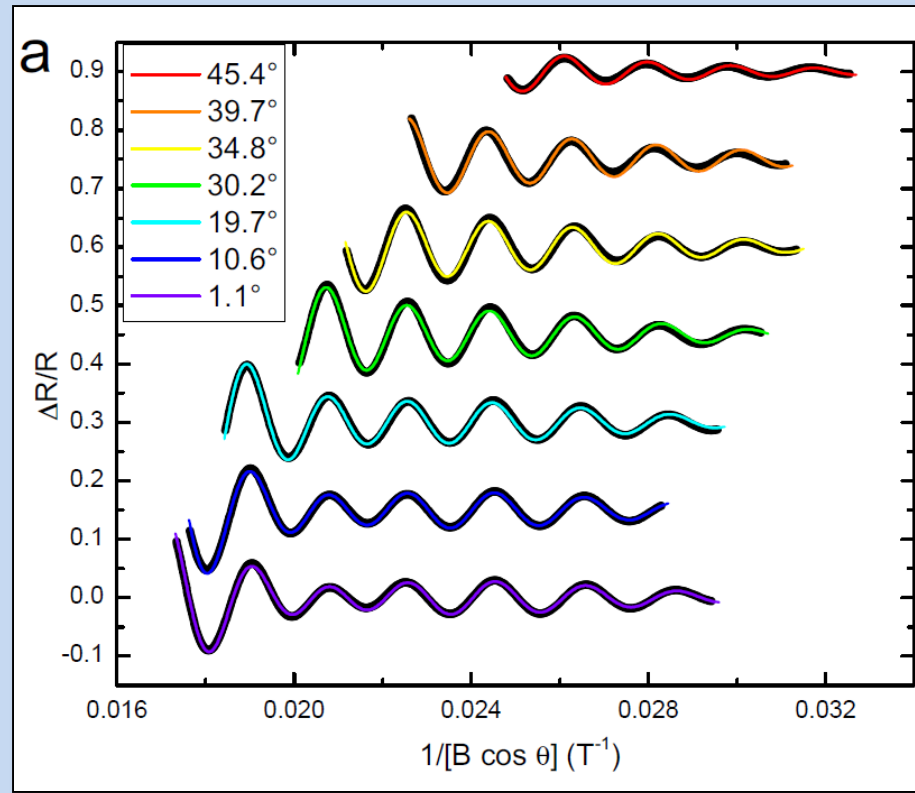
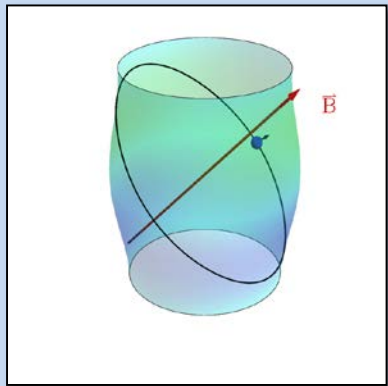
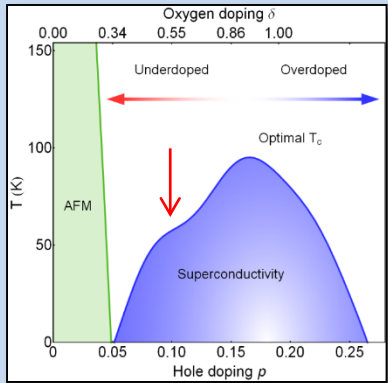
$$F = \frac{\hbar}{2\pi e} A_k$$

# Quantum Oscillations in $\text{YBa}_2\text{Cu}_3\text{O}_{6.59}$

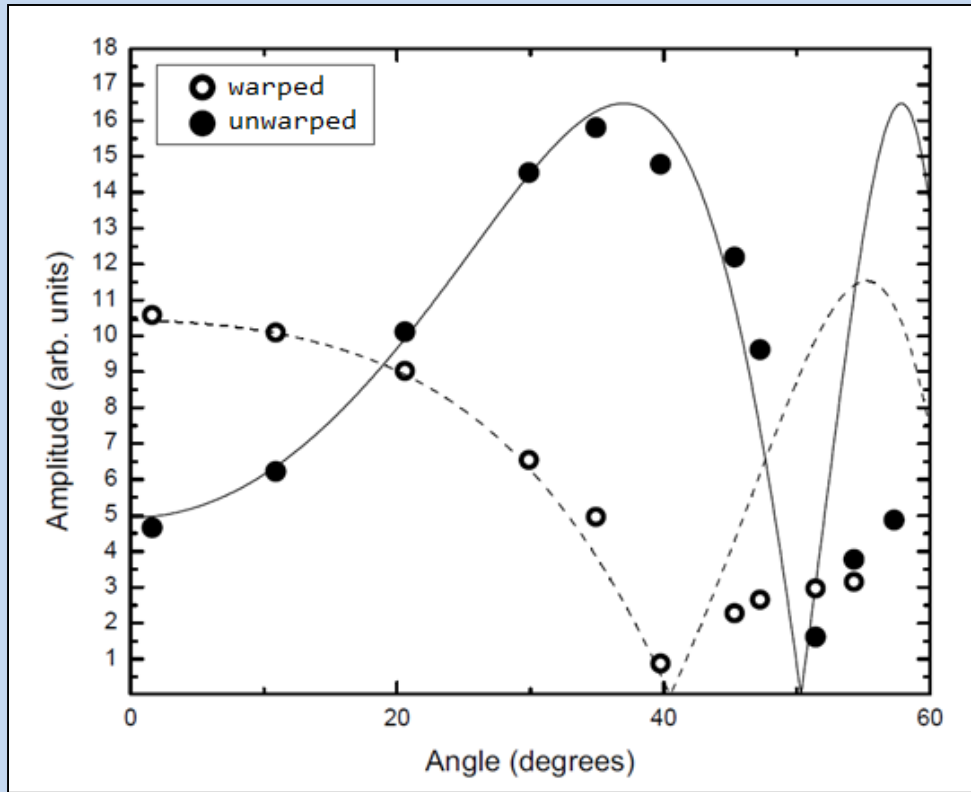
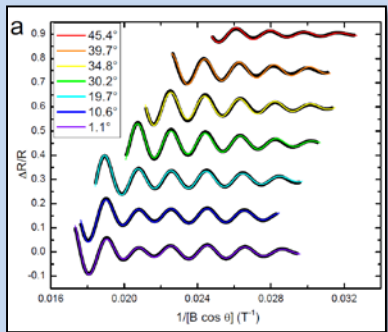
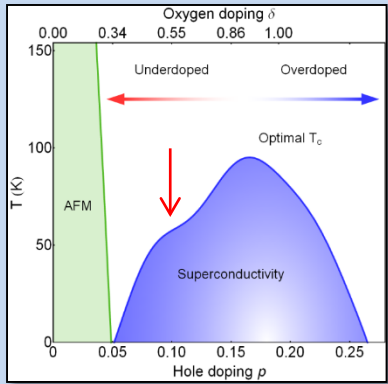


$$F = \frac{\hbar}{2\pi e} A_k$$

# Angle dependence of Quantum Oscillations

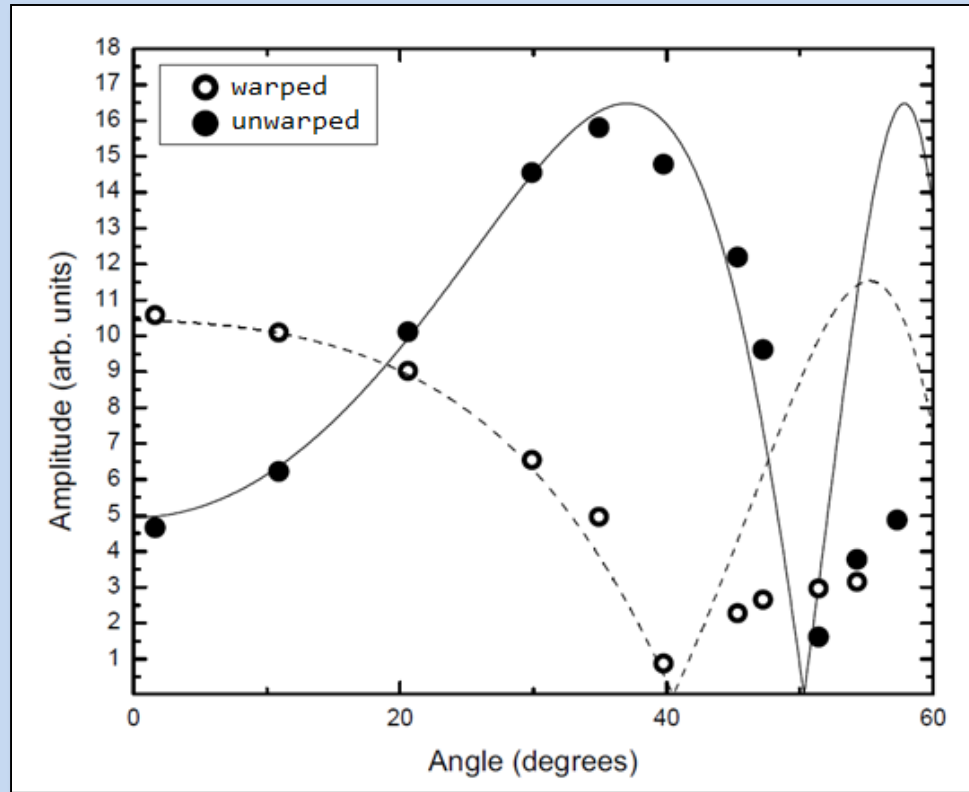
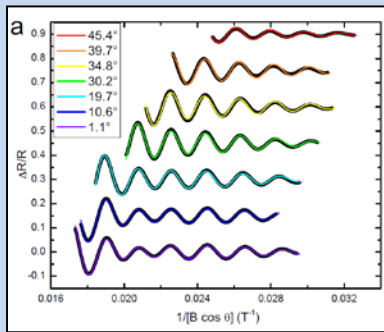
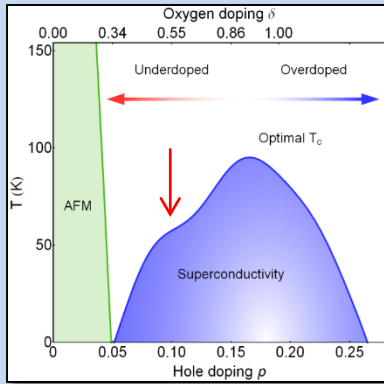


# Angle dependence of Quantum Oscillations



$$\overline{DOS} \propto \cos\left(\frac{2\pi F}{B} - \varphi\right) \times R_T R_D$$

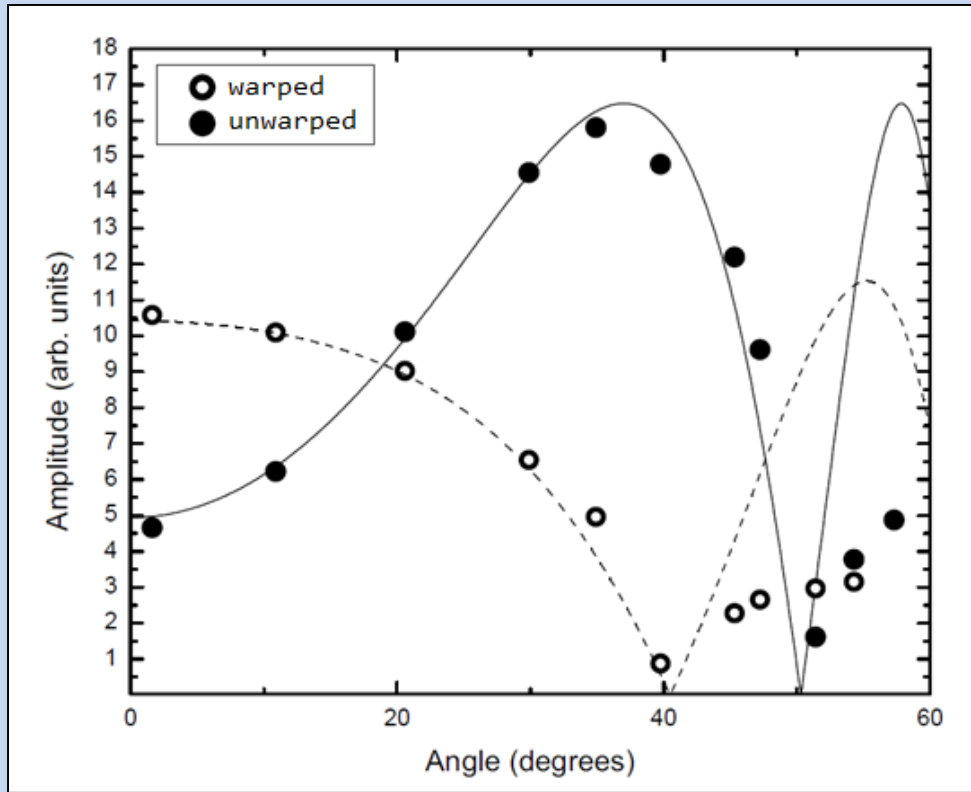
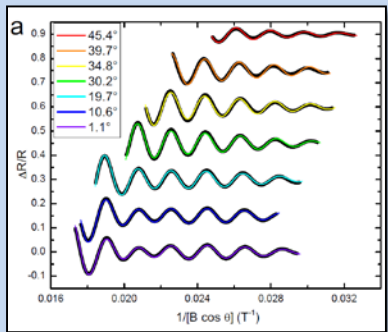
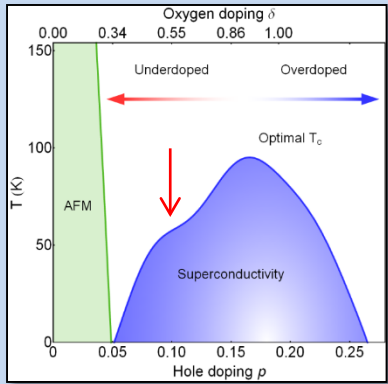
# Angle dependence of Quantum Oscillations



$$\overline{DOS} \propto \cos \left( \frac{2\pi\mu}{\hbar \frac{eB}{m^*}} - \varphi \right) \times R_T R_D$$

$$\mu_{\pm} = \mu_0 \pm g^* \frac{e}{2m_0} \frac{\hbar}{2} B$$

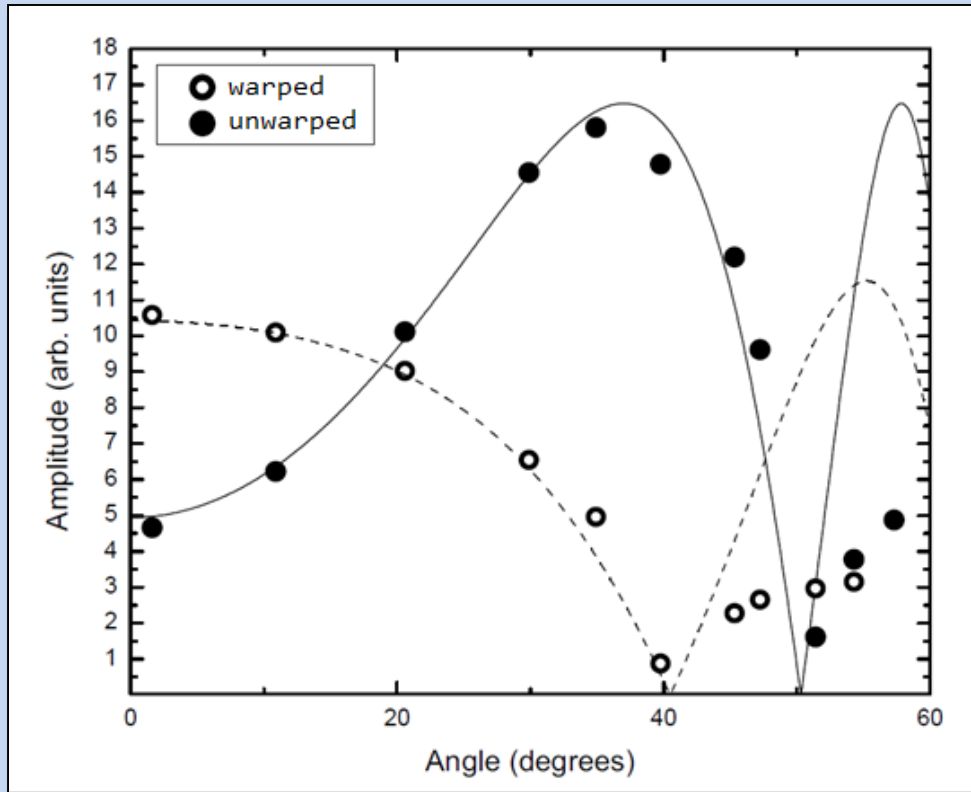
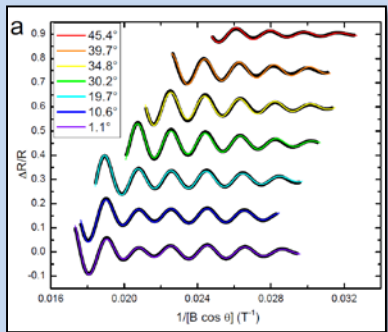
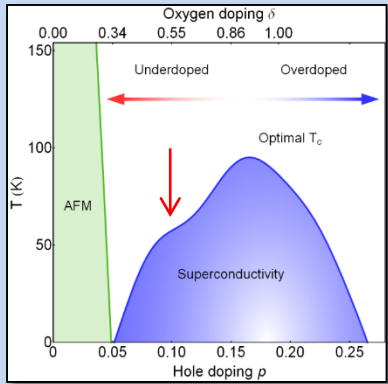
# Angle dependence of Quantum Oscillations



$$\overline{DOS} \propto \cos\left(\frac{2\pi\mu}{\hbar} \frac{eB}{m^*} - \varphi\right) \times \cos\left(\pi g^* \frac{m^*}{2m_0}\right)$$



# Angle dependence of Quantum Oscillations

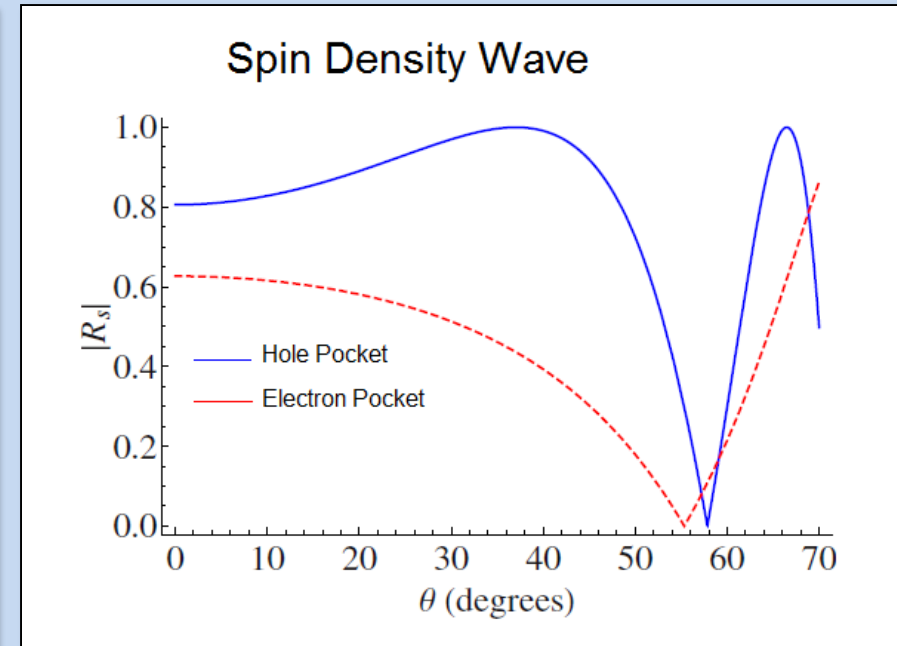
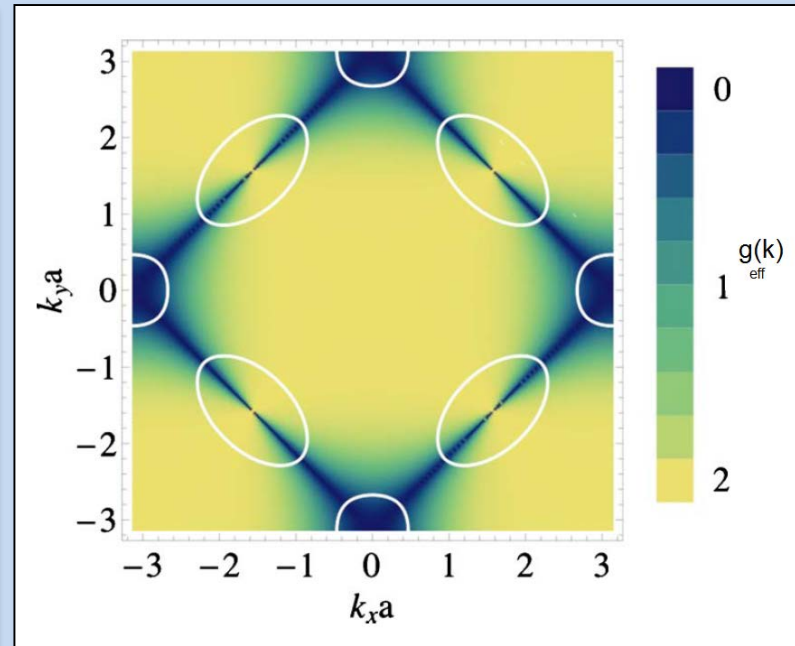
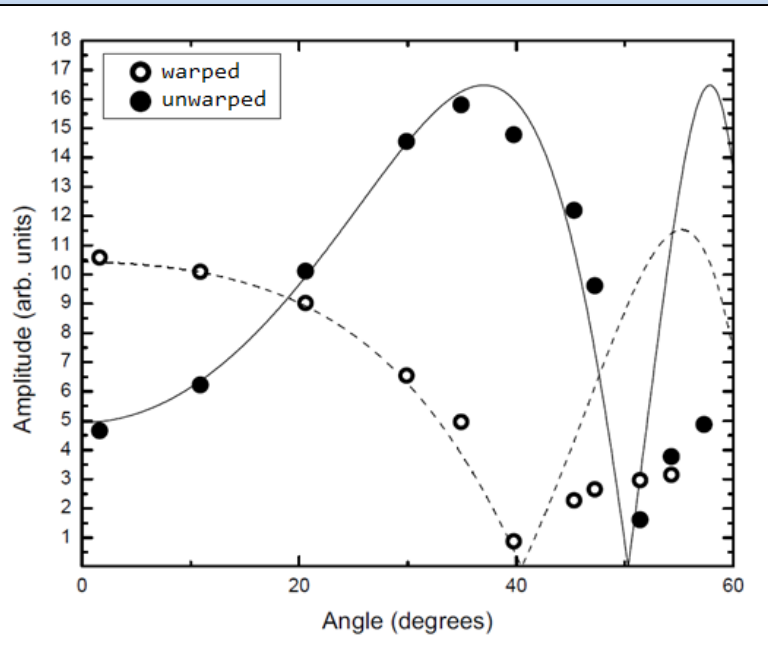


$$\overline{DOS} \propto \cos\left(\frac{2\pi\mu}{\hbar} \frac{eB}{m^*} - \varphi\right) \times \cos\left(\pi g^* \frac{m^*}{2m_0}\right)$$

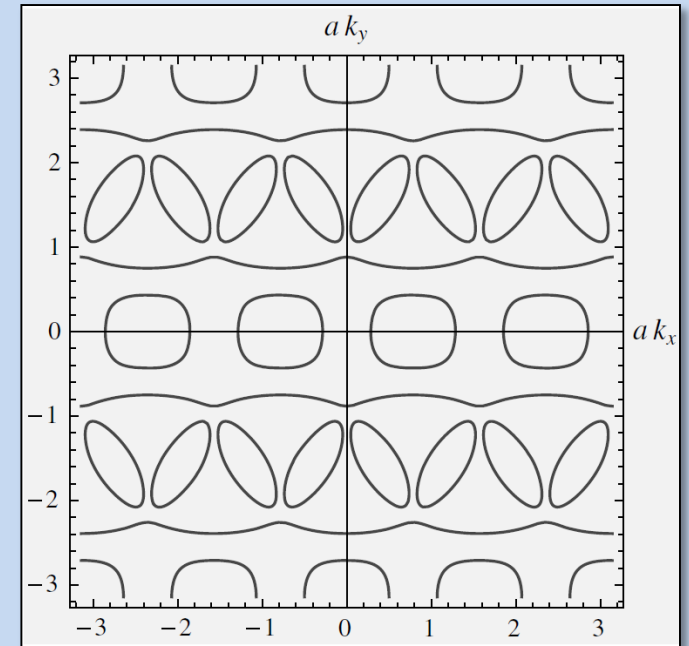
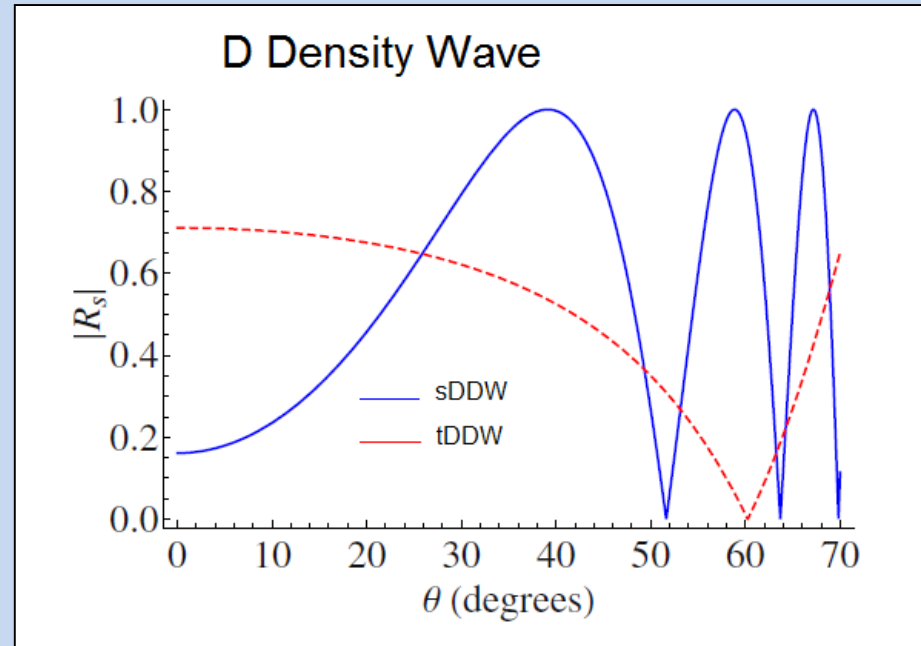
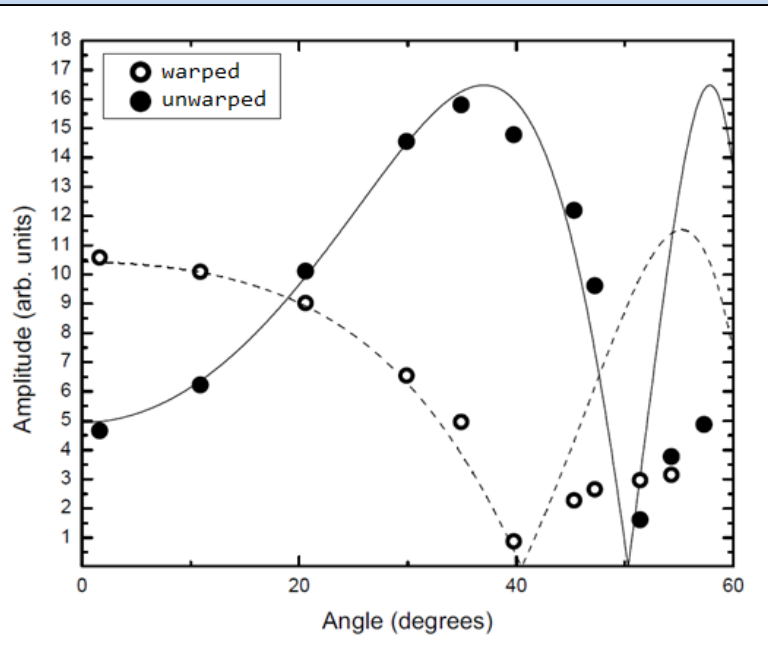
$$m^*(\theta) = \frac{m^*(\theta = 0)}{\cos(\theta)}$$

$$g^* \approx 2$$

# Fermi Surface Reconstruction, and the $g$ Factor

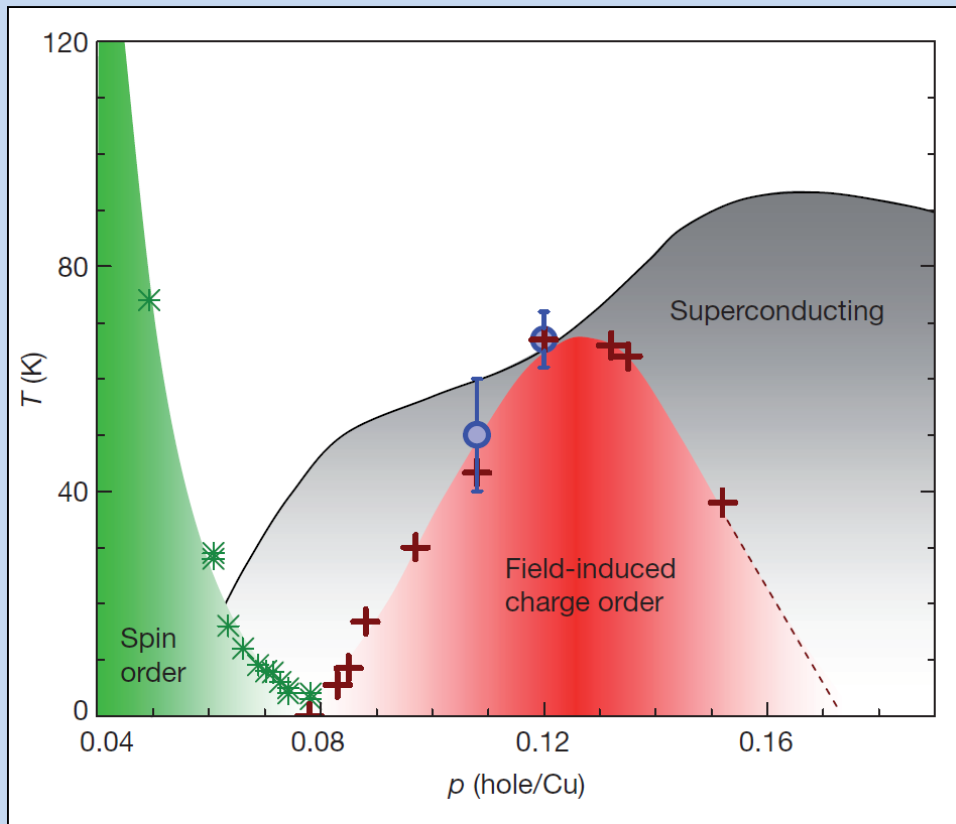


# Fermi Surface Reconstruction, and the $g$ Factor

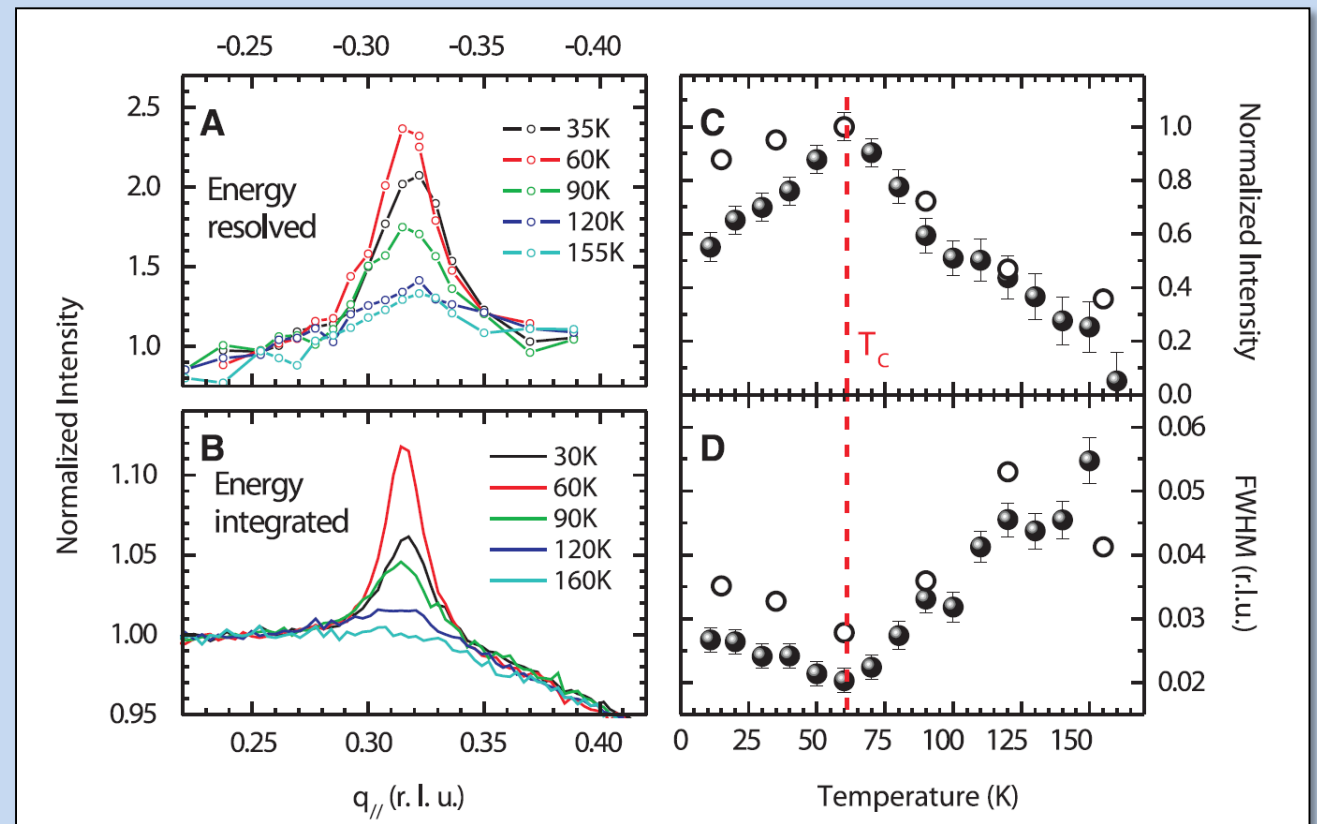


# Charge Density Wave Order

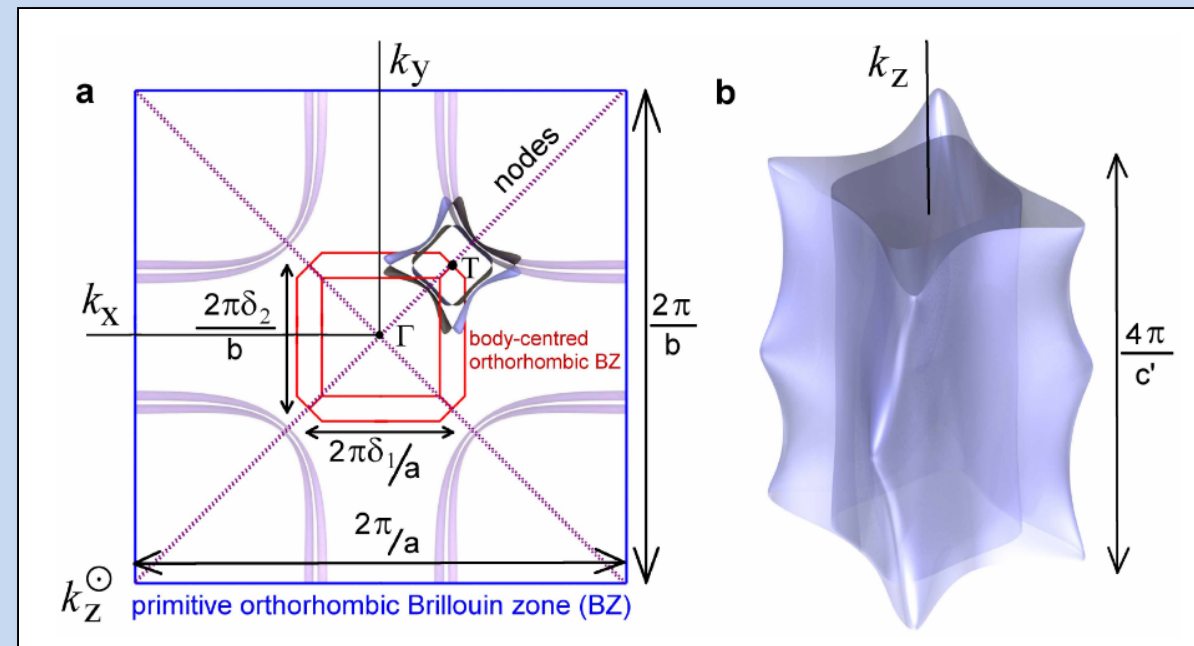
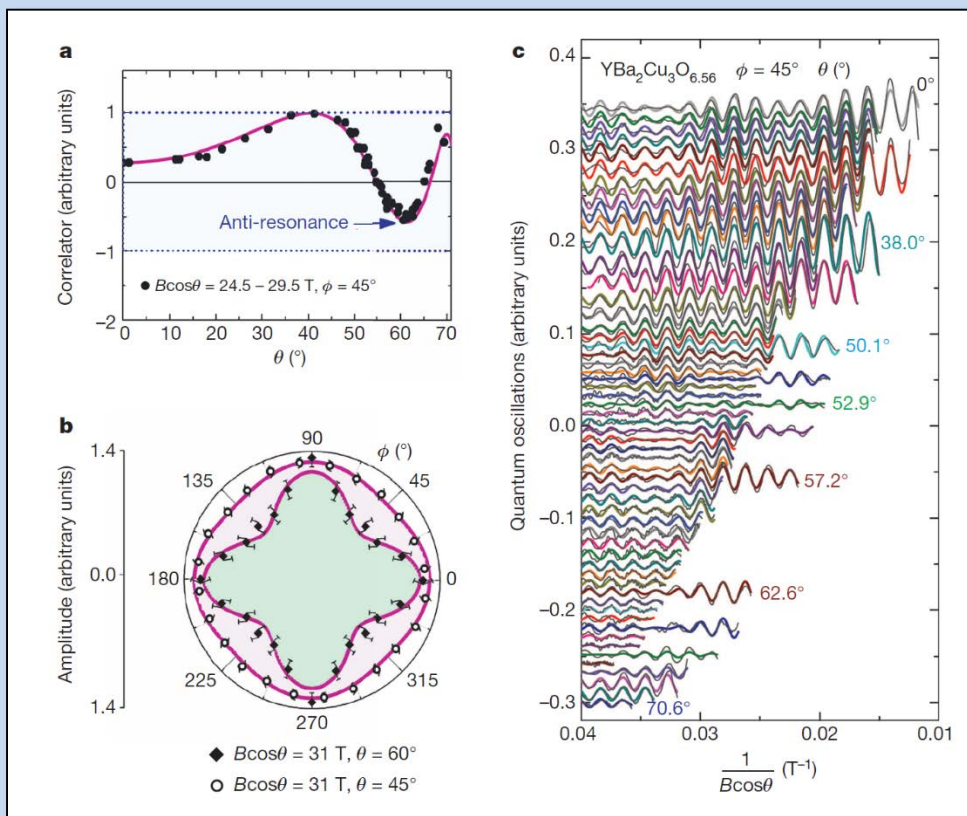
## NMR



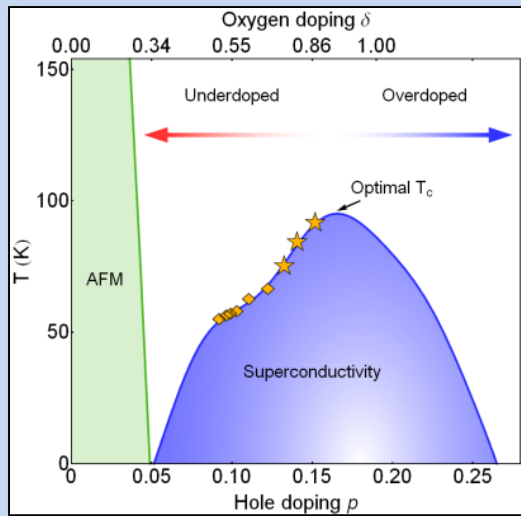
## X-rays



# Charge Density Wave Reconstruction (?)



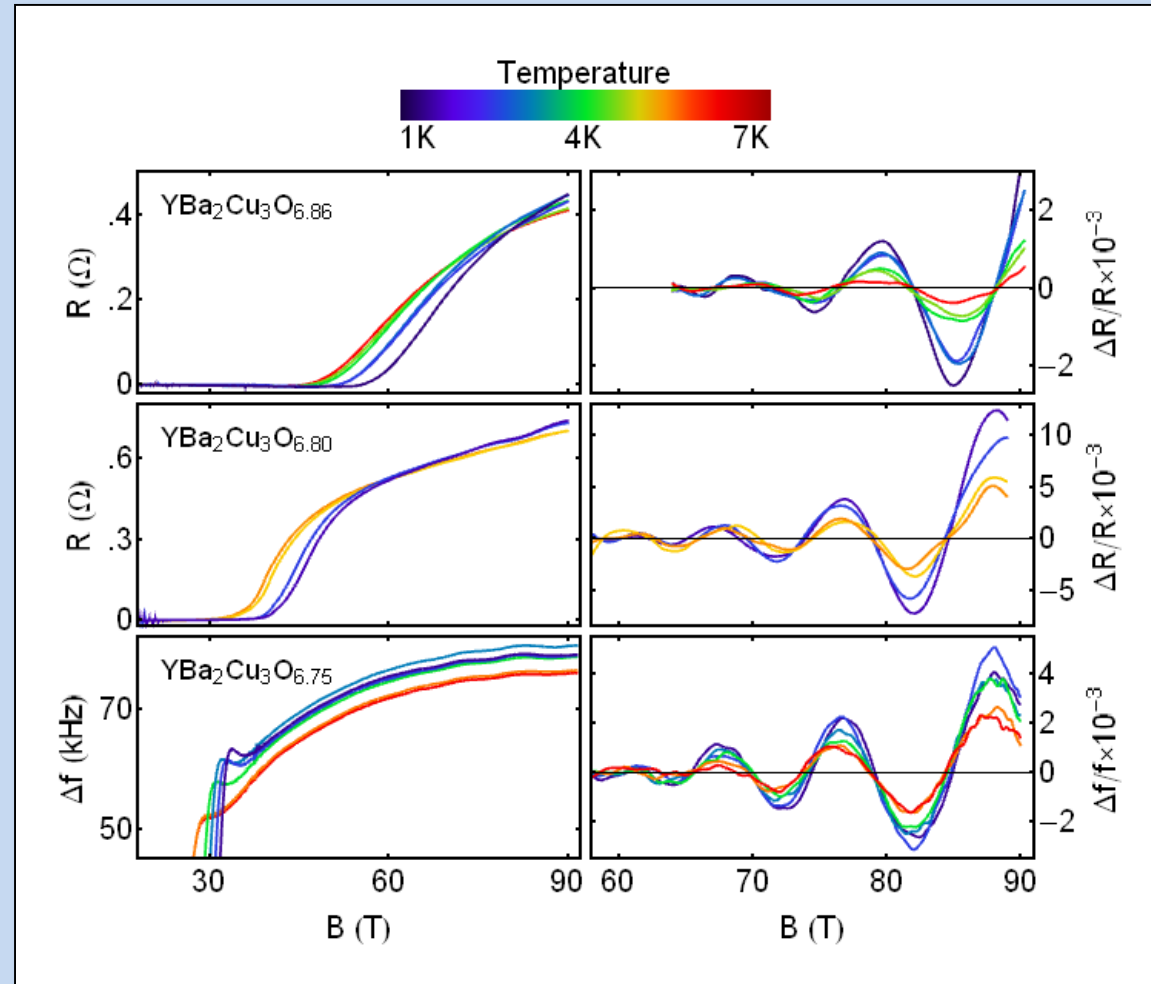
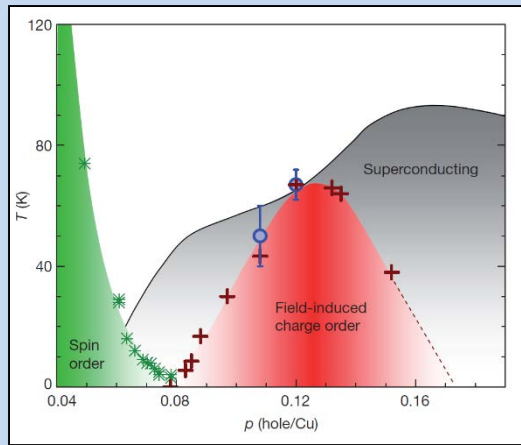
# Small Electron Pocket Ubiquitous to the CDW Region



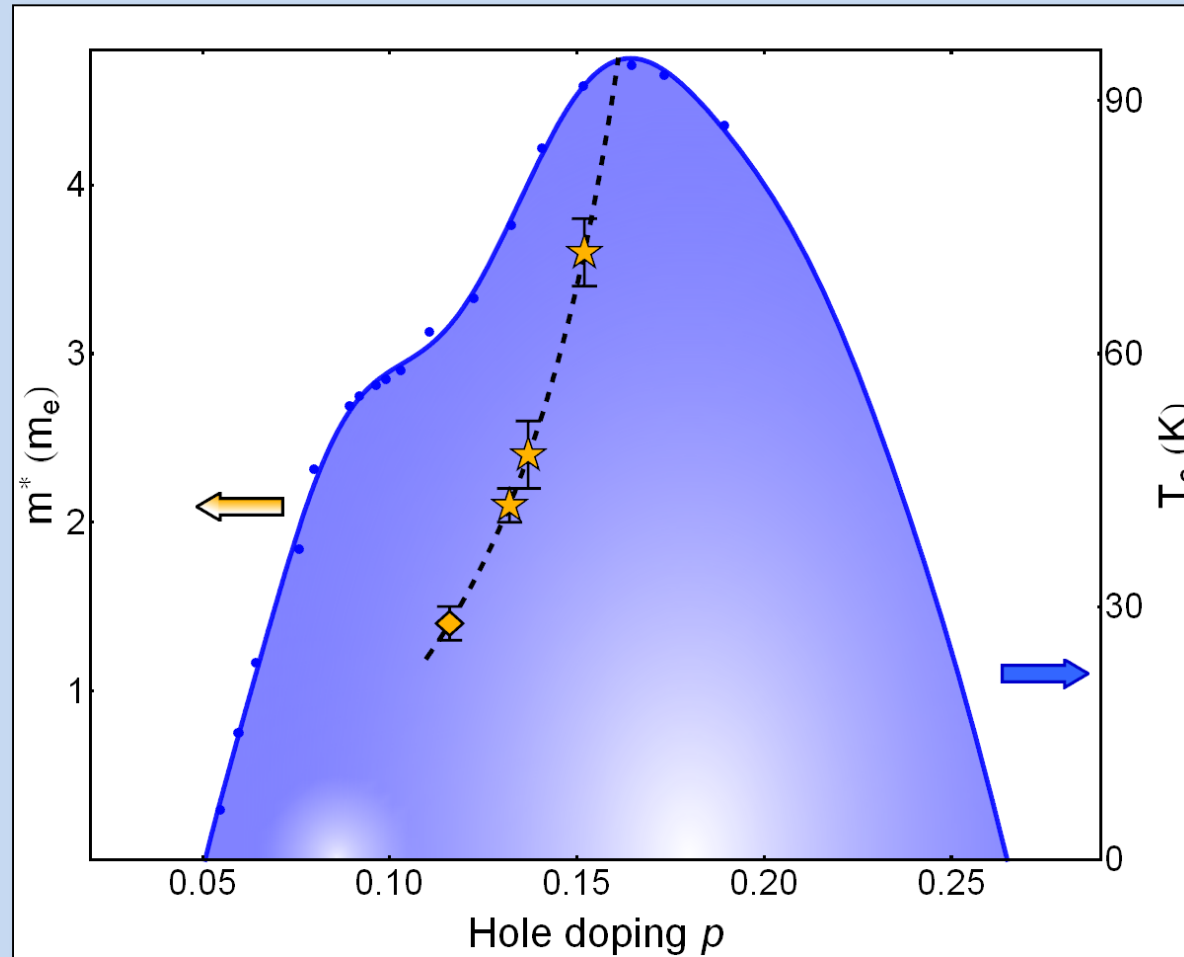
$T_c \sim 91\text{K}$

$T_c \sim 81\text{K}$

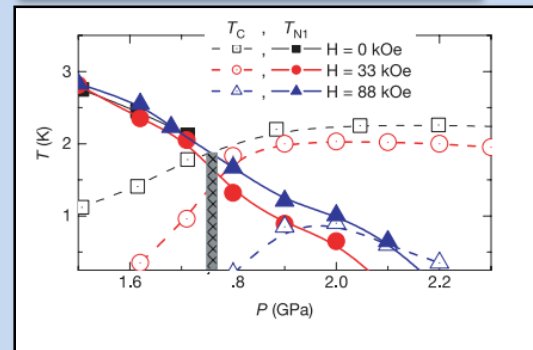
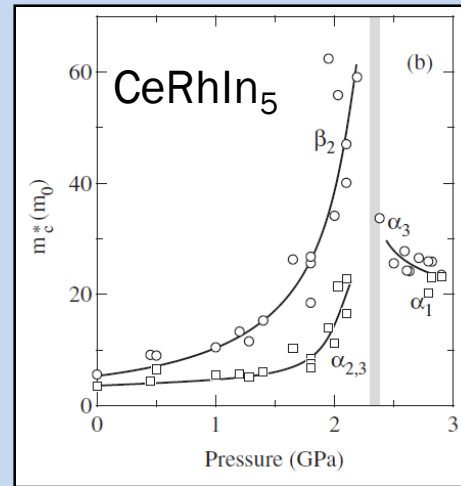
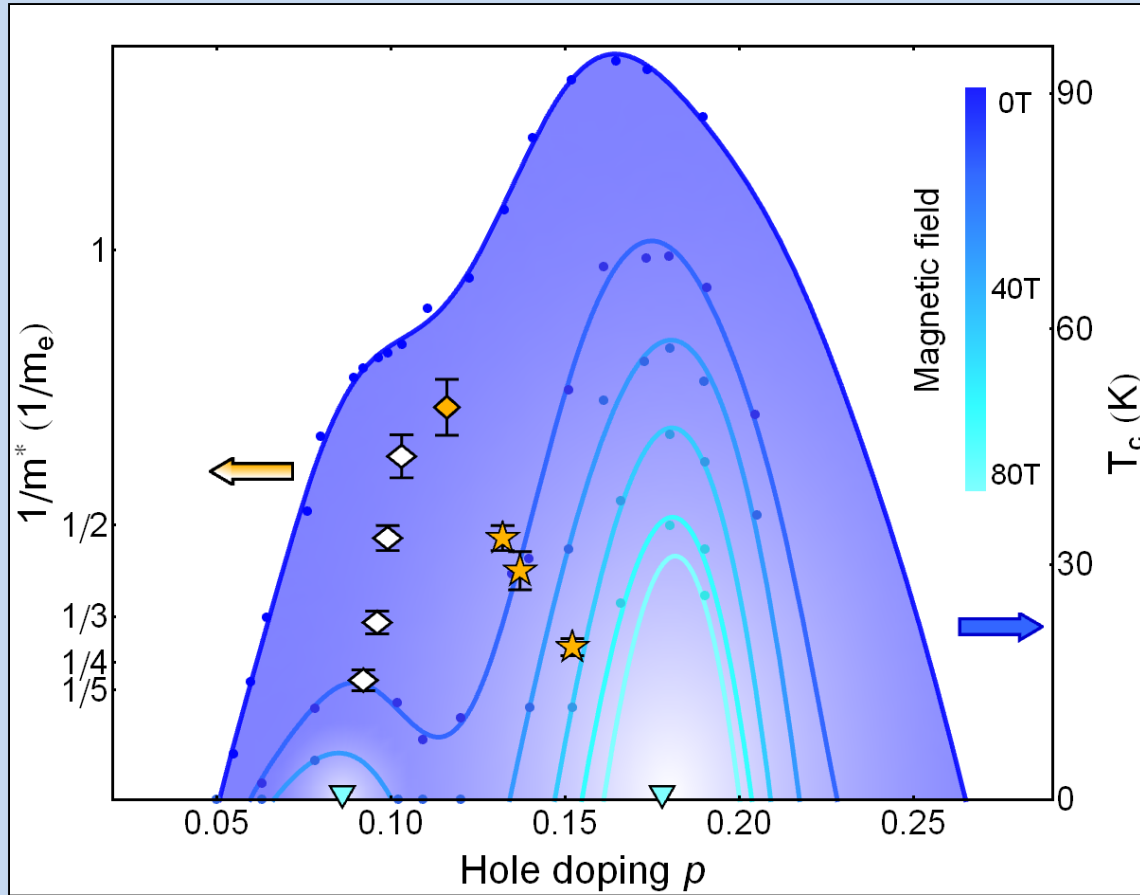
$T_c \sim 75\text{K}$



# Diverging Effective Mass



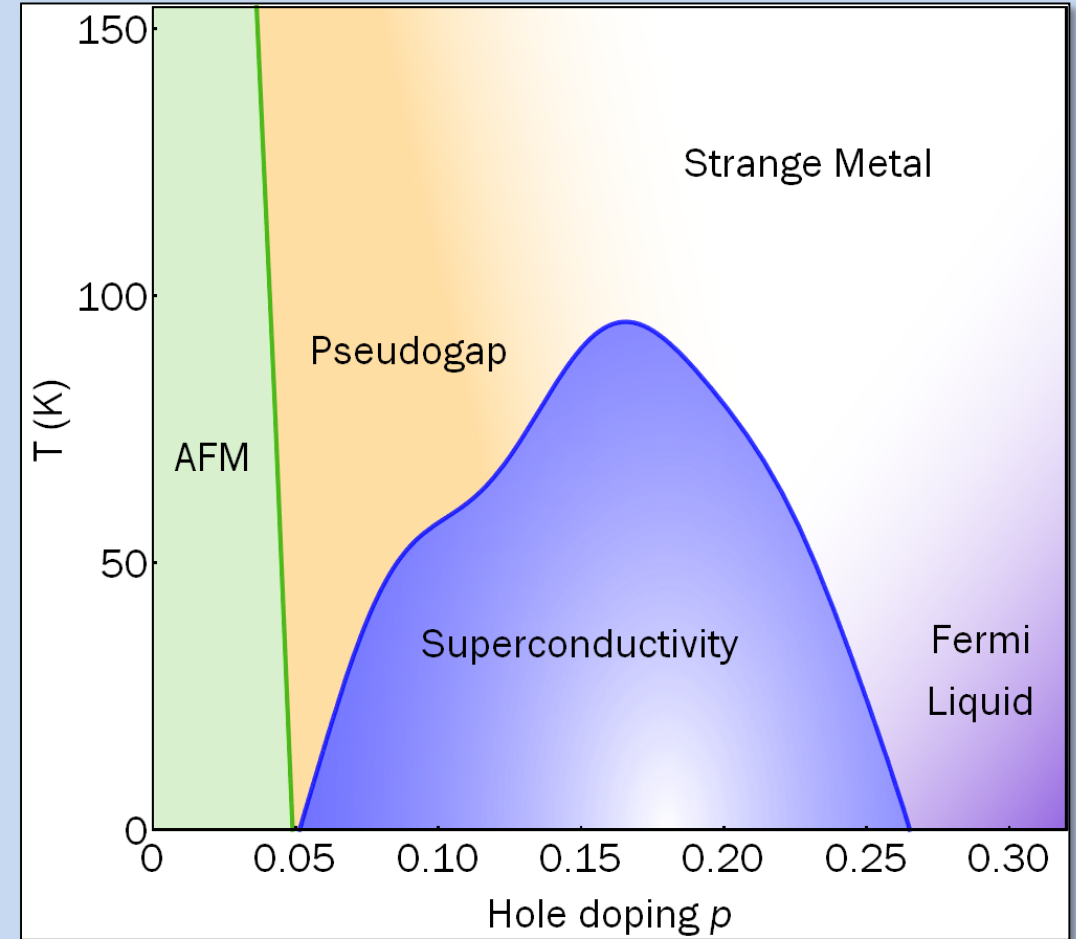
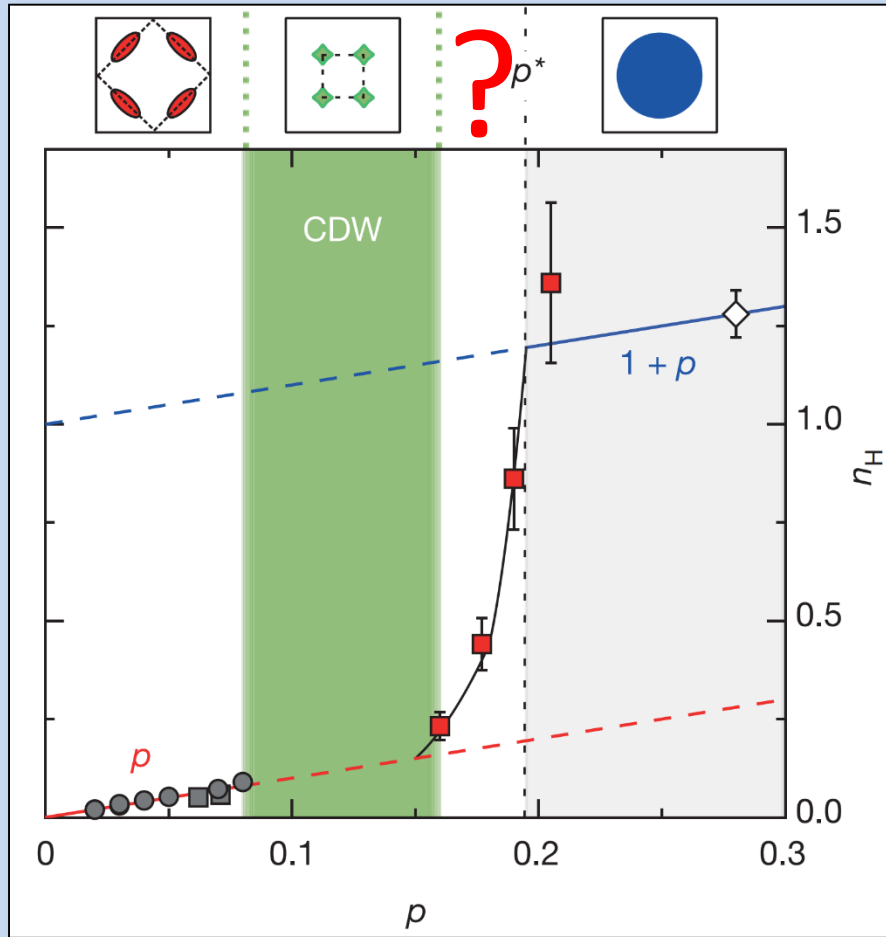
# Thermodynamic evidence for a Quantum Critical Point



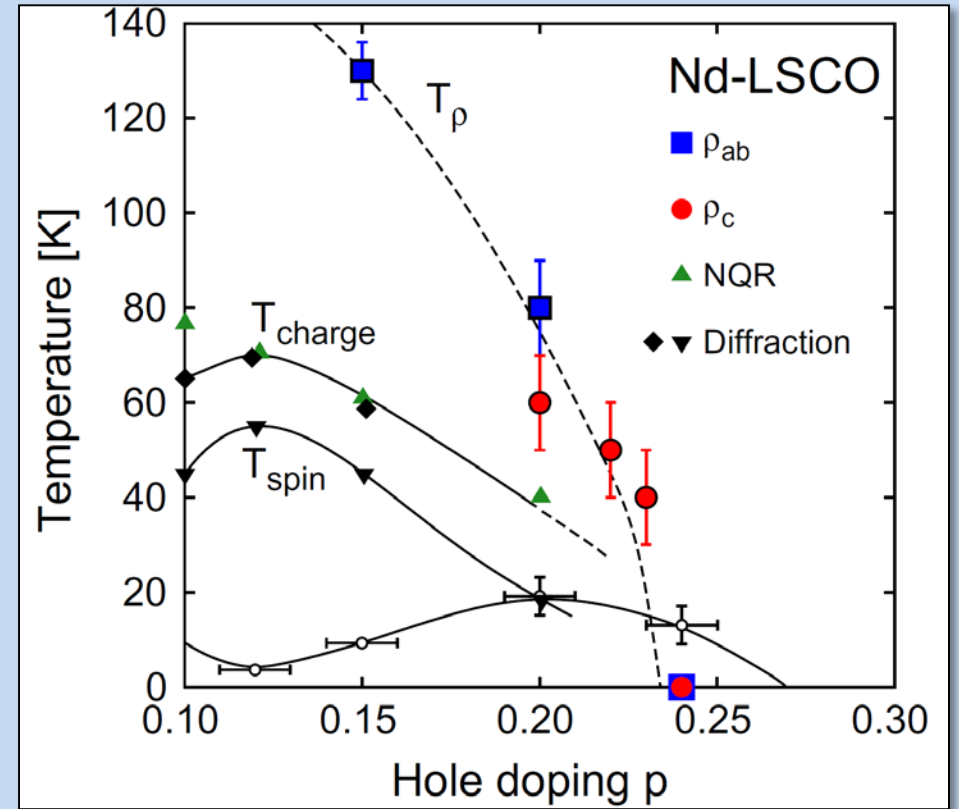
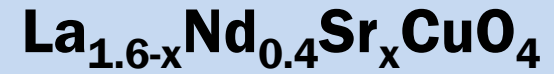
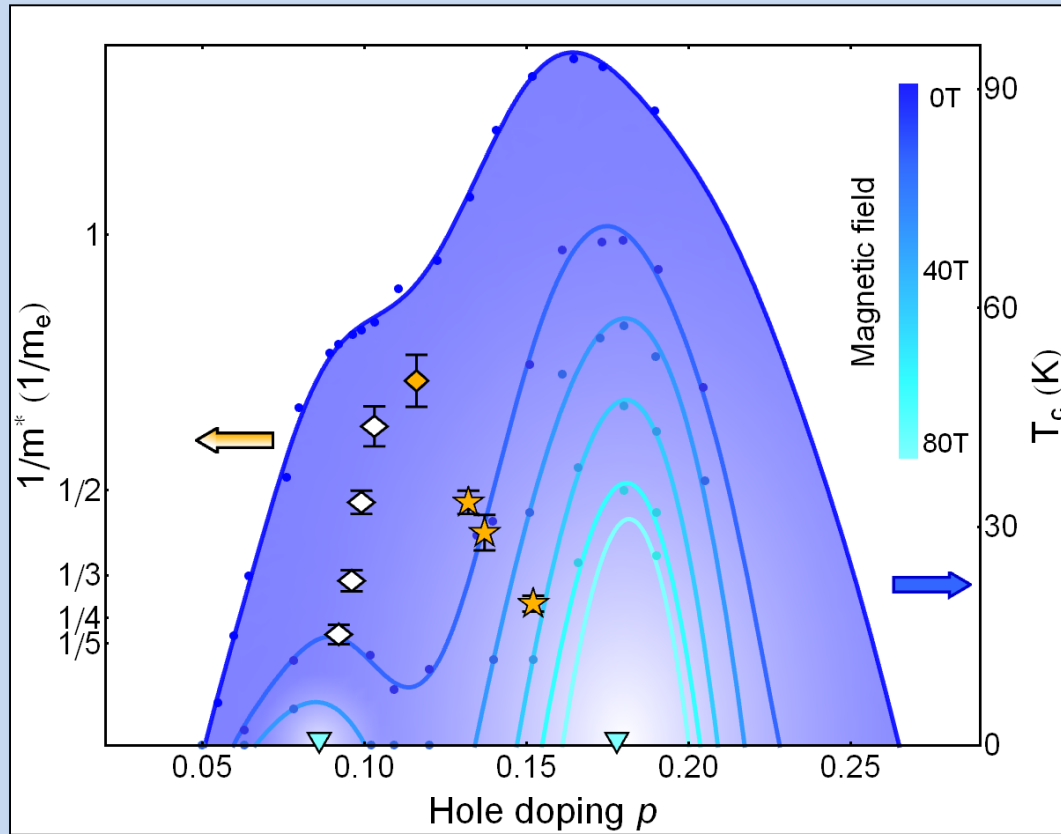
PHYSICAL REVIEW B, VOLUME 63, 094503  
**Hidden order in the cuprates**  
 Sudip Chakravarty,<sup>1</sup> R. B. Laughlin,<sup>2</sup> Dirk K. Morr,<sup>3</sup> and Chetan Nayak<sup>1</sup>



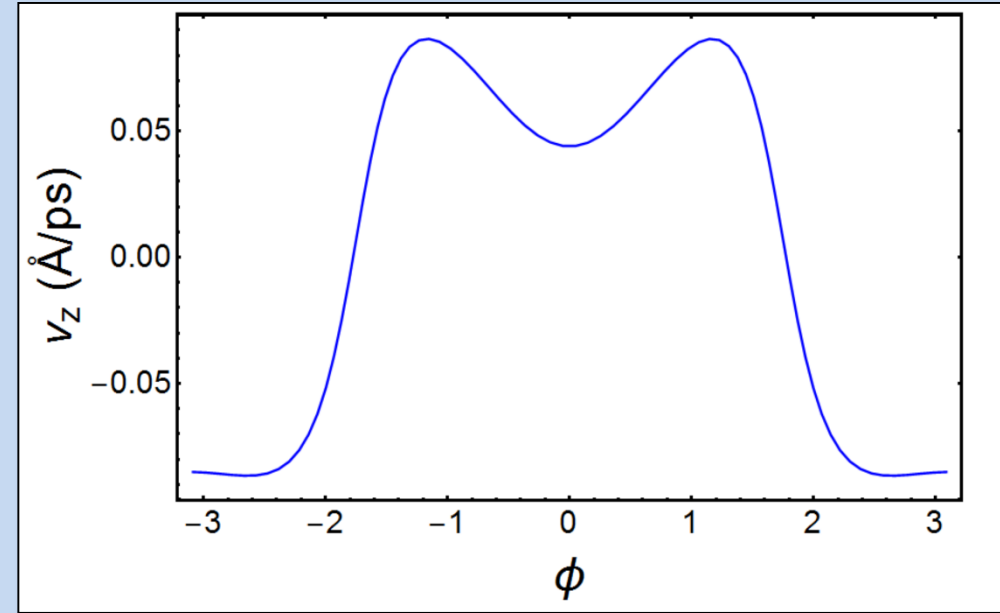
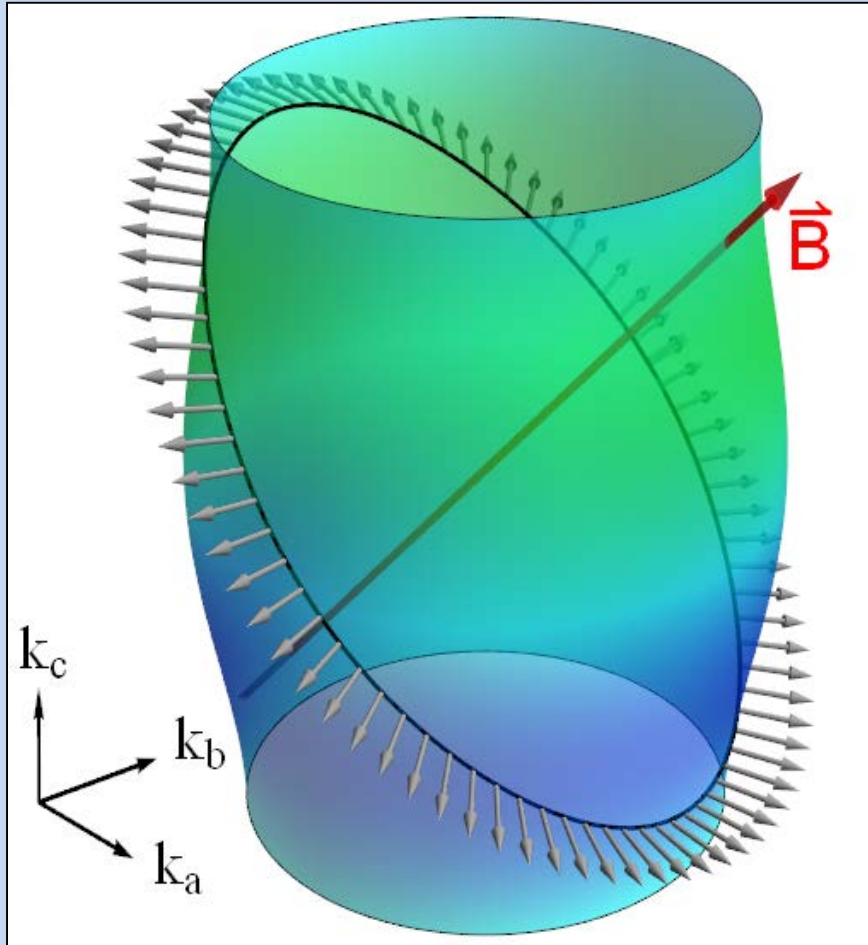
# From Insulator to Superconductor



# End of the Line for YBCO



# Angle-Dependent Magnetoresistance (ADMR)

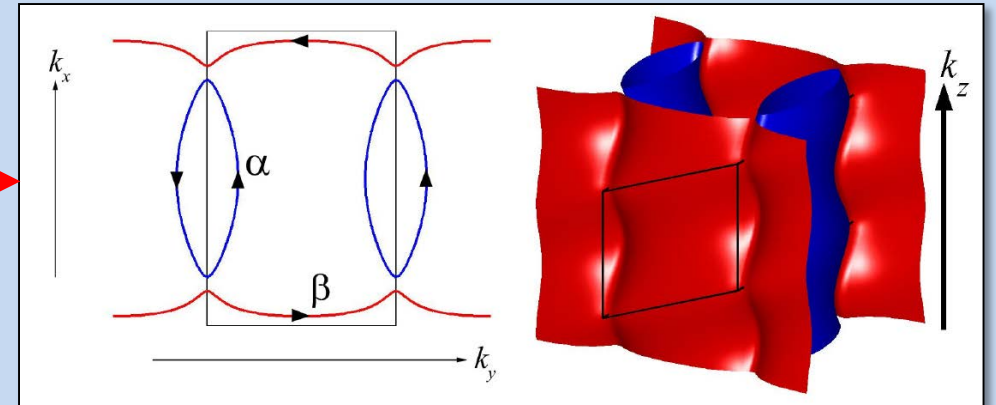
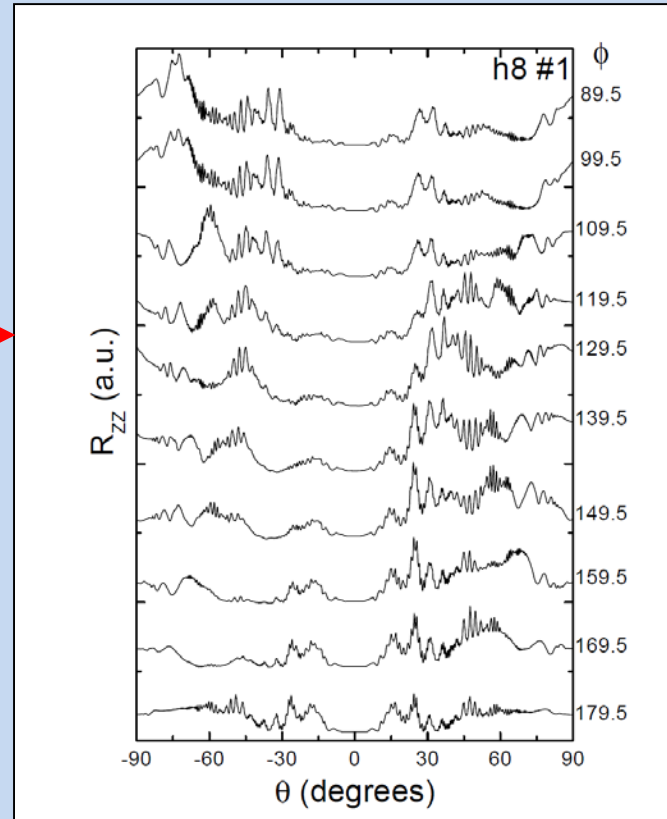
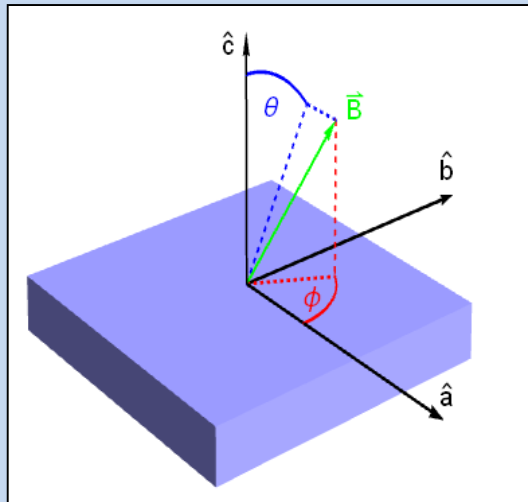
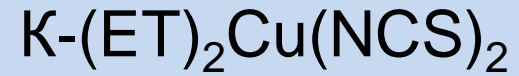


$$\sigma_{ij} = \frac{e^2}{4\pi^3} \int d^3k \left( -\frac{df_0}{d\epsilon} \right) v_i(t=0) \int_{-\infty}^0 dt v_j(t) e^{t/\tau}$$

$$v(k) = \frac{1}{\hbar} \nabla_k \epsilon(k)$$

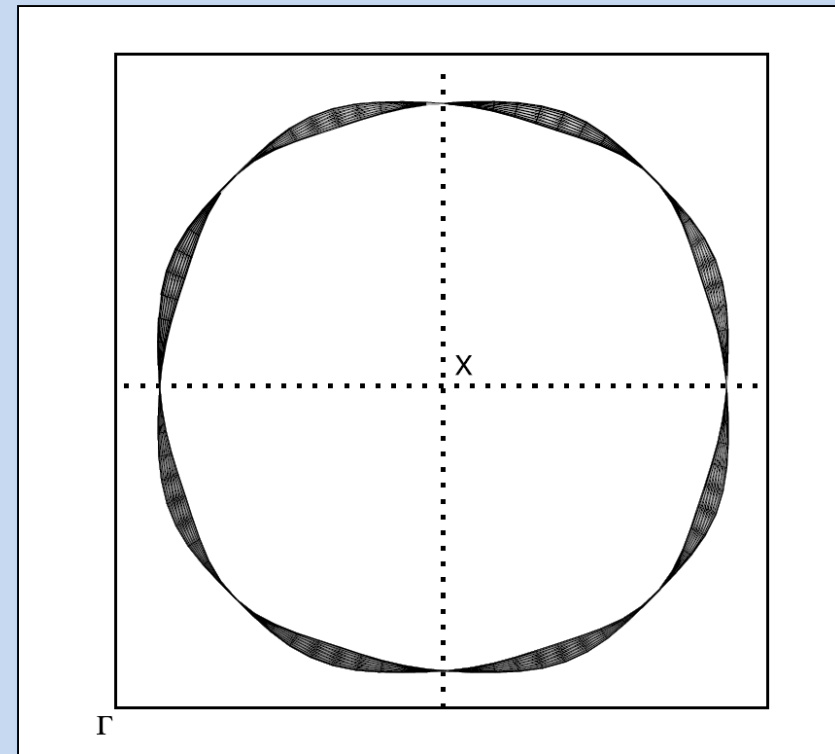
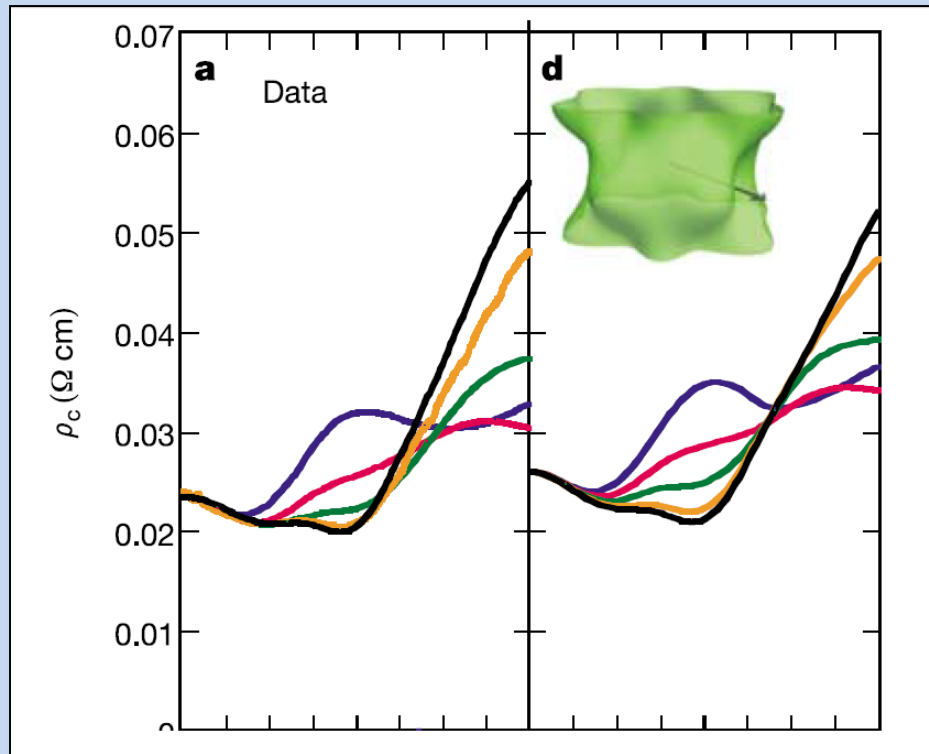
Can measure  $\epsilon(k)$

# Angle-Dependent Magnetoresistance (ADMR)



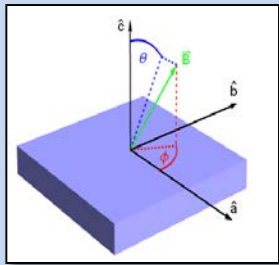
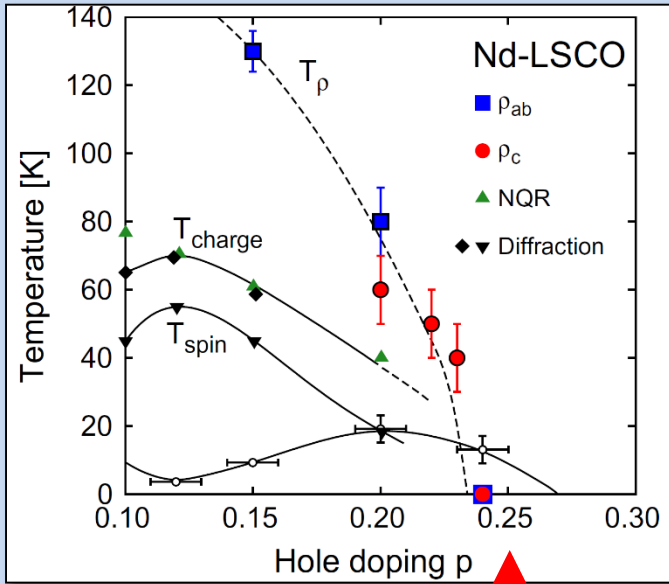
# Angle-Dependent Magnetoresistance (ADMR)

TI-2201

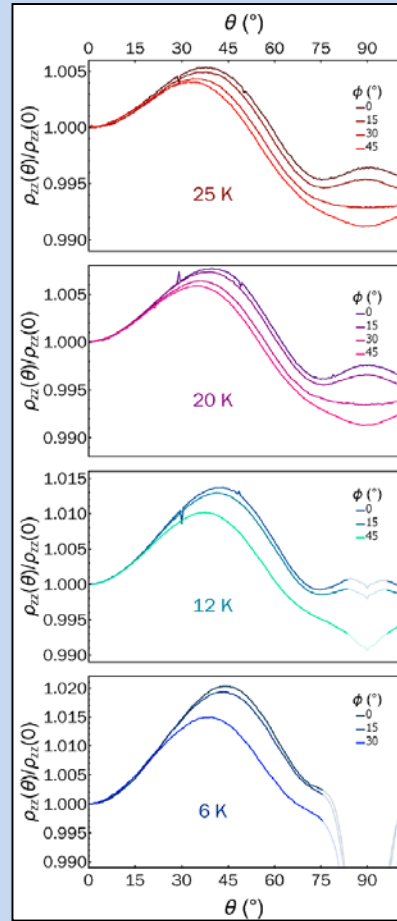


# ADMR of $\text{La}_{1.6-0.25}\text{Nd}_{0.4}\text{Sr}_{0.25}\text{CuO}_4$

## $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$

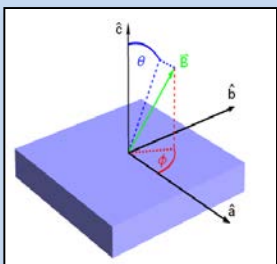
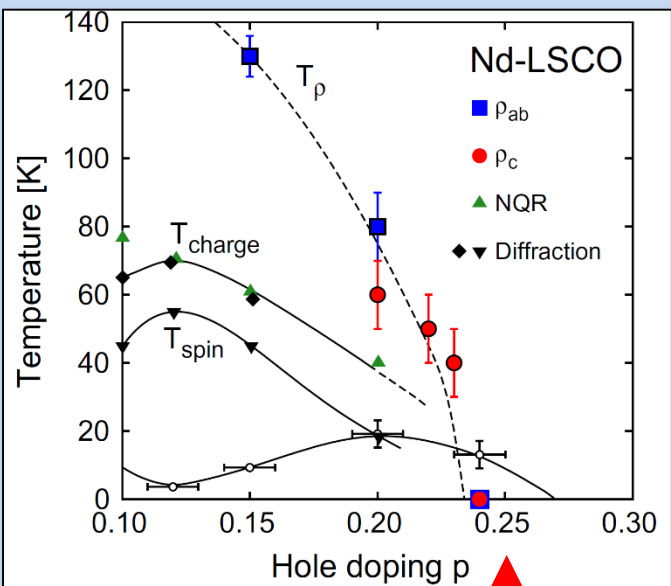


## Data



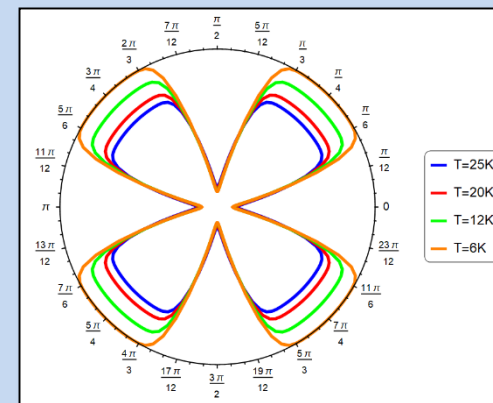
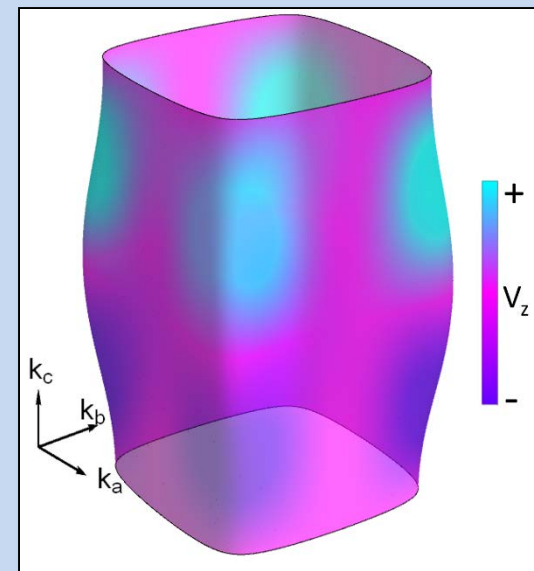
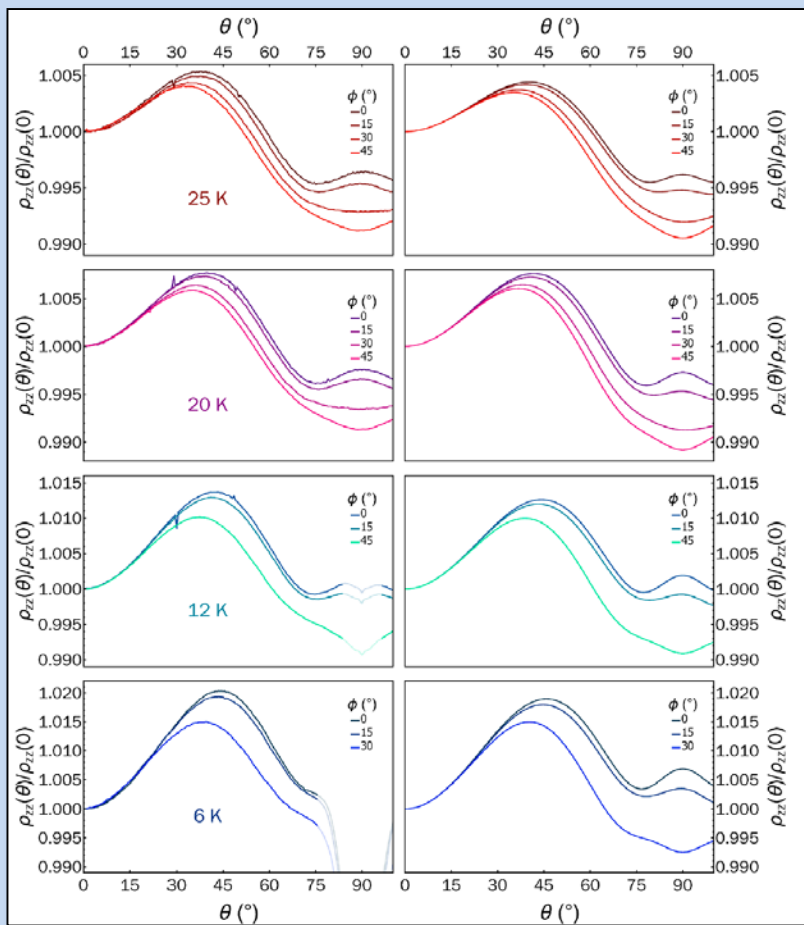
# ADMR of $\text{La}_{1.6-0.25}\text{Nd}_{0.4}\text{Sr}_{0.25}\text{CuO}_4$

## $\text{La}_{1.6-x}\text{Nd}_{0.4}\text{Sr}_x\text{CuO}_4$

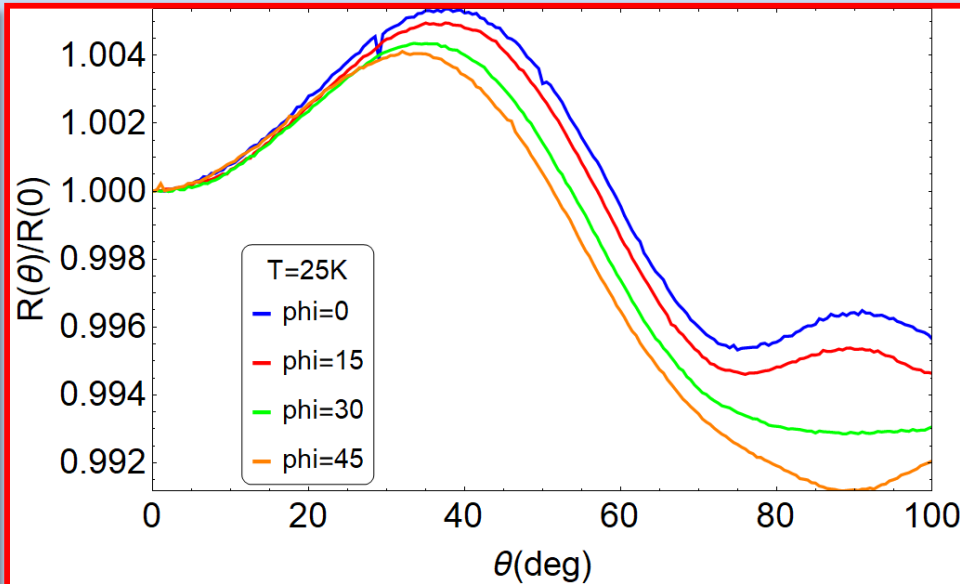
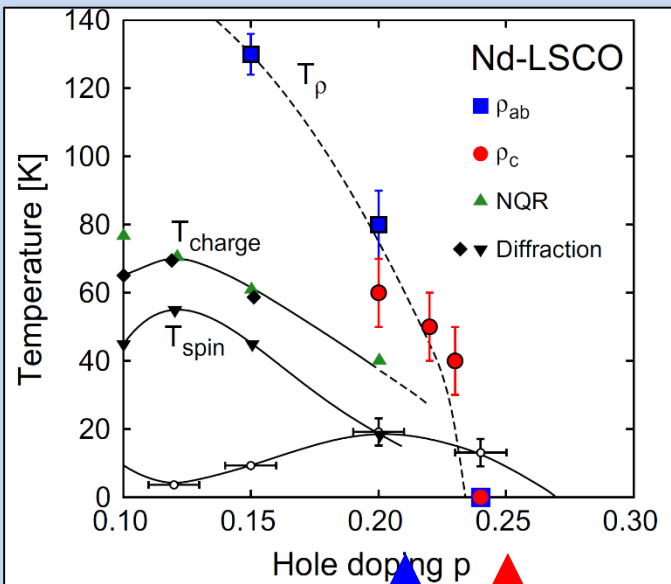
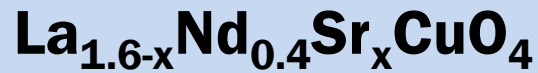


## Data

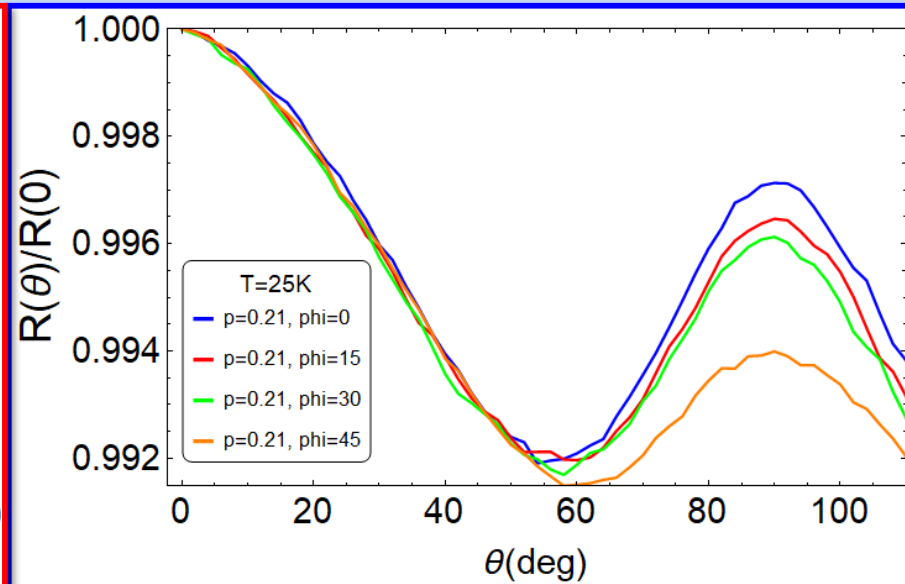
## Simulation



# ADMR of $\text{La}_{1.6-0.21}\text{Nd}_{0.4}\text{Sr}_{0.21}\text{CuO}_4$



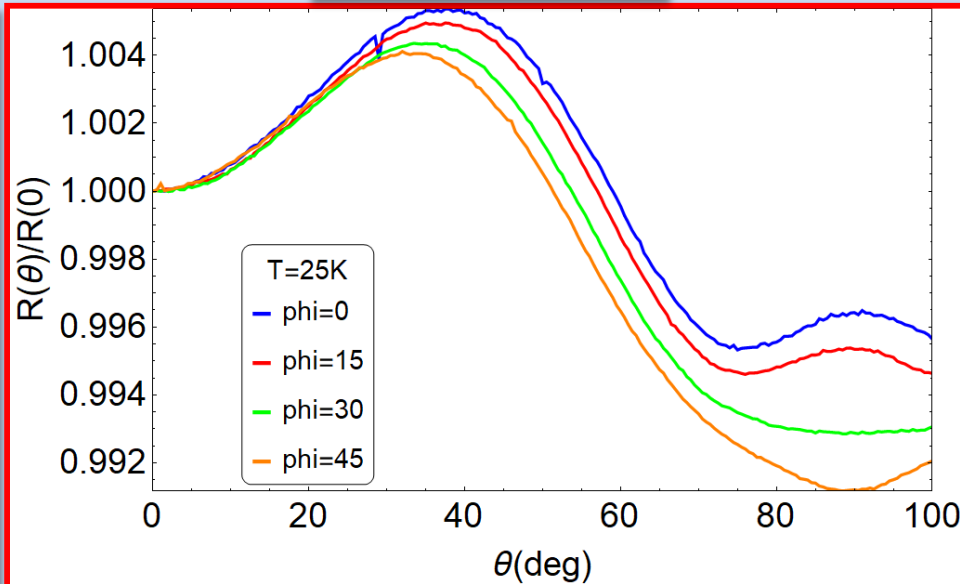
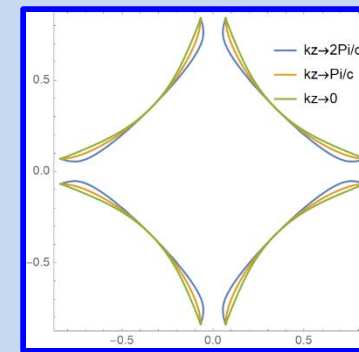
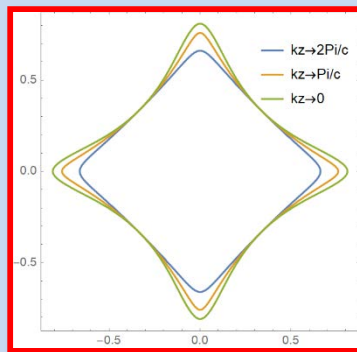
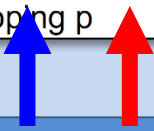
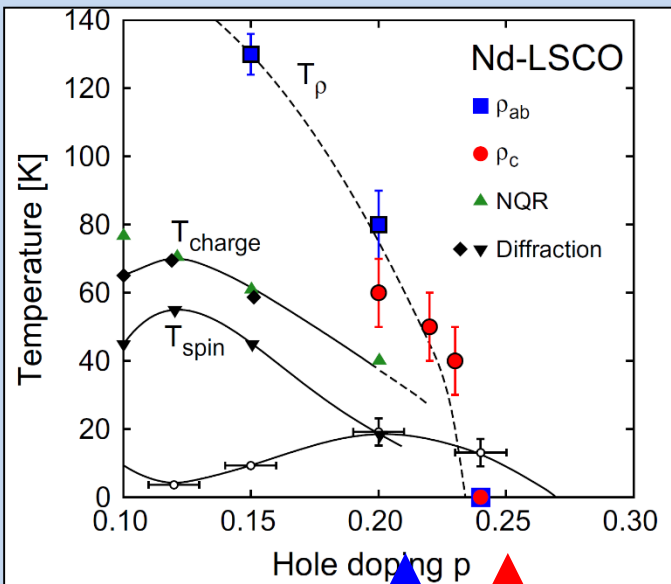
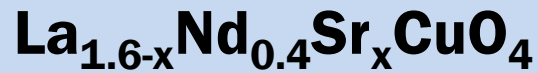
$p = 0.25$



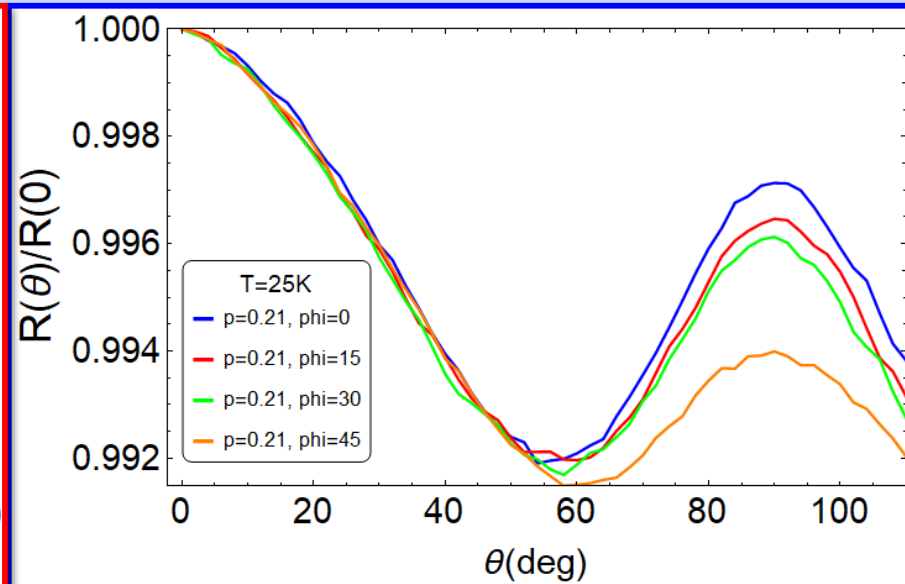
$p = 0.21$



# ADMR of $\text{La}_{1.6-0.21}\text{Nd}_{0.4}\text{Sr}_{0.21}\text{CuO}_4$

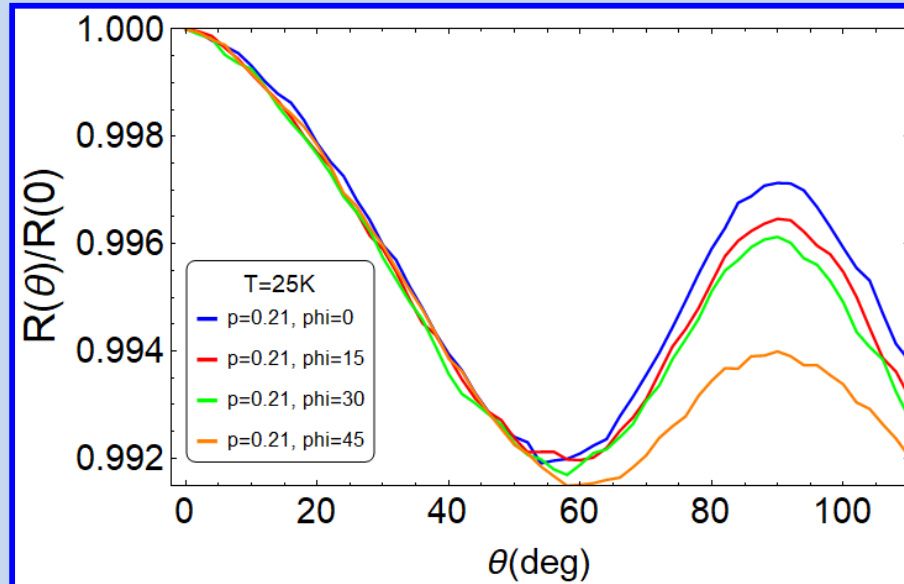
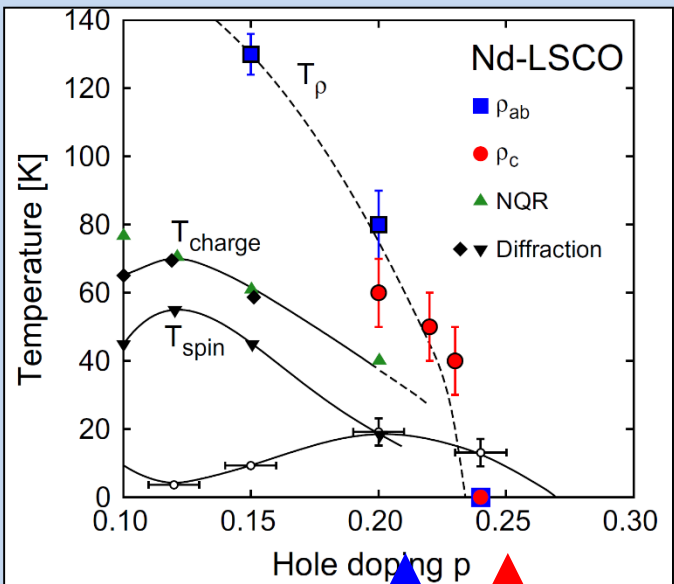
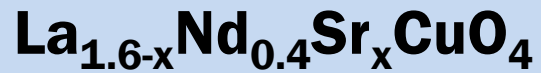


**$p = 0.25$**

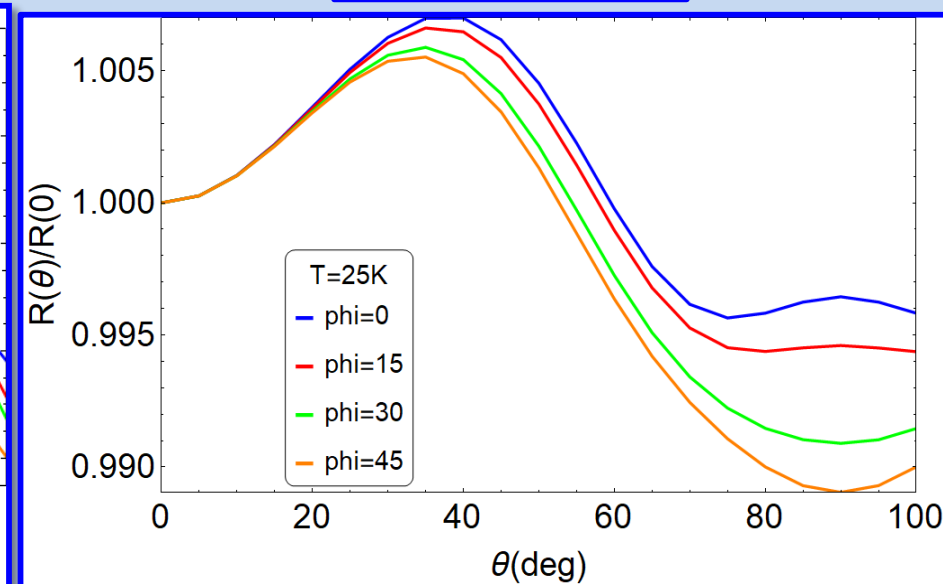


**$p = 0.21$**

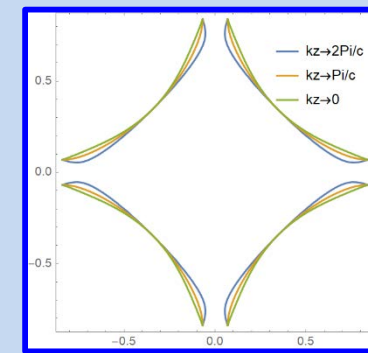
# ADMR of $\text{La}_{1.6-0.21}\text{Nd}_{0.4}\text{Sr}_{0.21}\text{CuO}_4$



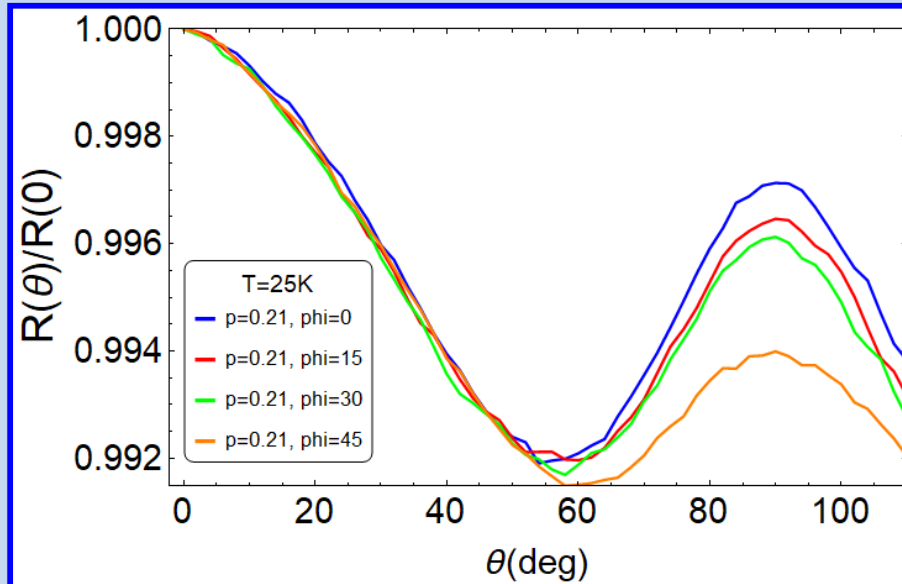
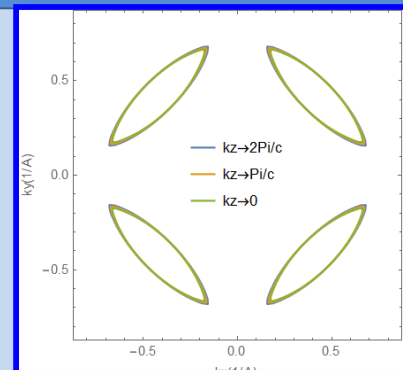
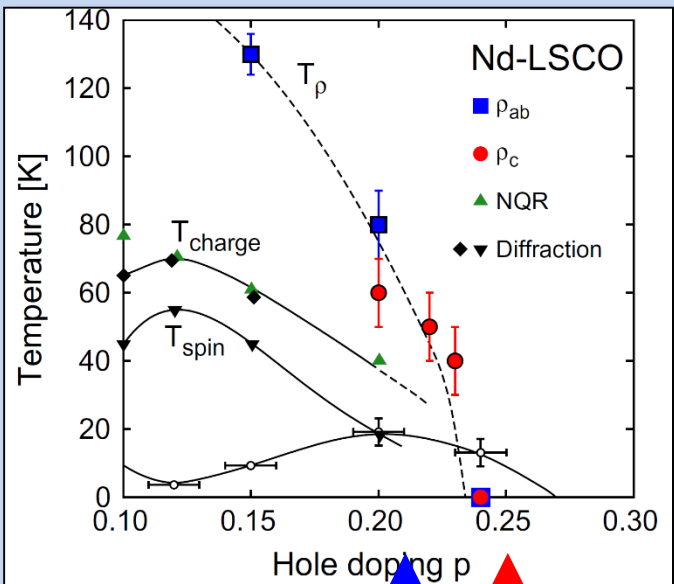
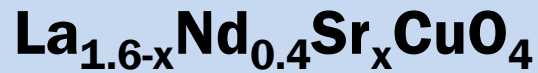
$p = 0.21$  - Data



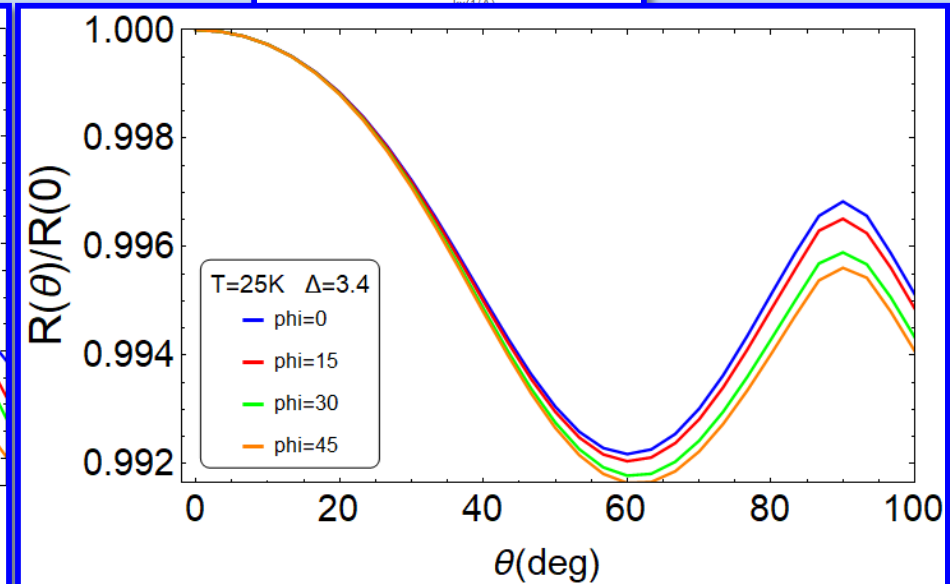
Simulation



# ADMR of $\text{La}_{1.6-0.21}\text{Nd}_{0.4}\text{Sr}_{0.21}\text{CuO}_4$



$p = 0.21$  - Data



Simulation

# Conclusions

- ‘New’ technique to measure the Fermi surface for  $p < p^*$ .
- Doesn’t look like arcs or charge order.
- ADMR may give us access to the normal-state Fermi surface across the phase diagram.
- Doesn’t need a Fermi liquid, just Fermi surface.
- Can extract the  $k$ -dependent lifetime.
- High  $T$  in YBCO? Low doping “metal”?

