

Cosmological implications of hidden scale invariance

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with Shelley Liang, Suntharan Arunasalam, Cyril Lager and Albert
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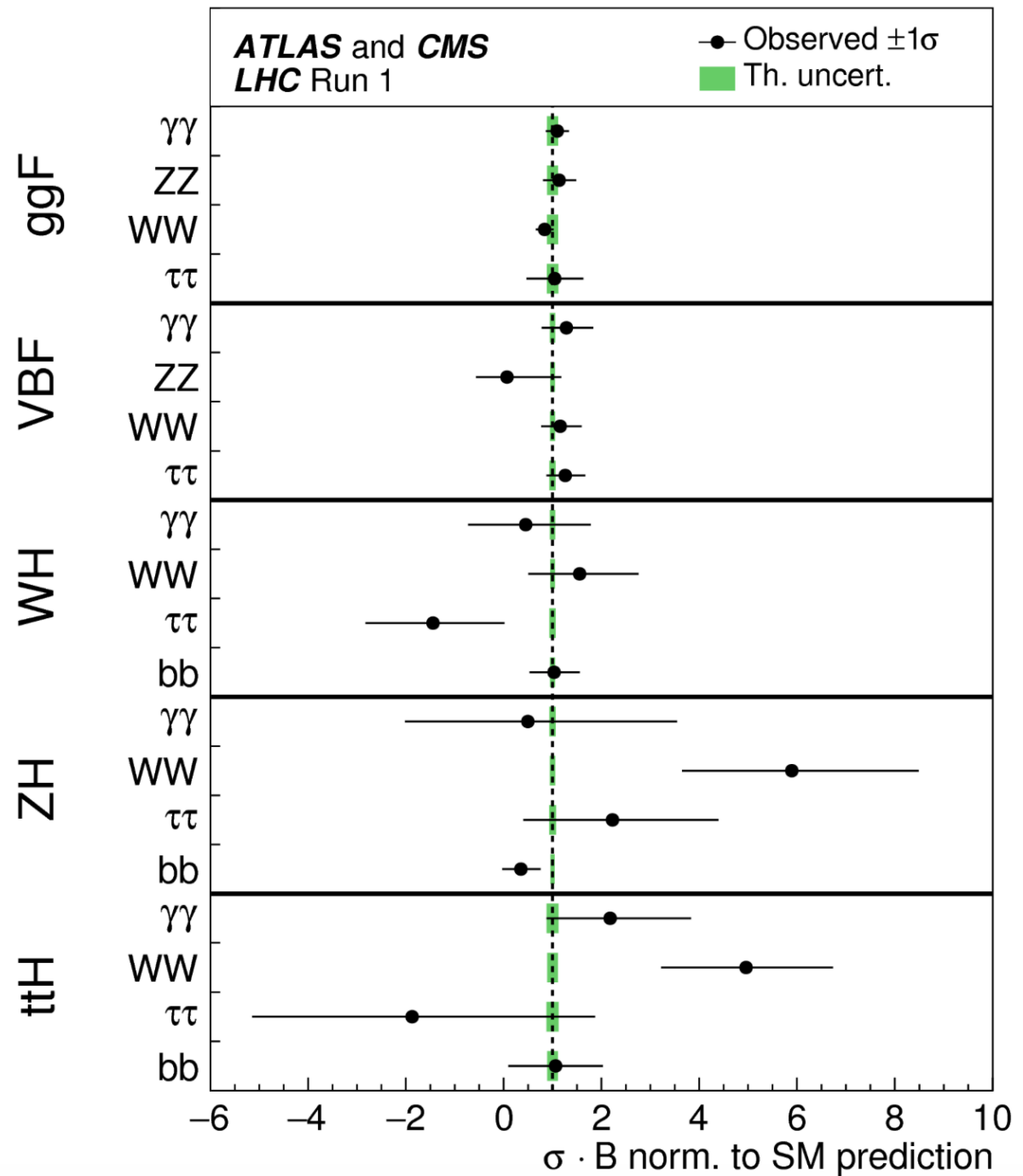
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Outline

- Higgs and naturalness (again)
- Scale invariant Standard Model with light dilaton
- Electroweak phase transition in the Standard Model with light dilaton and its implications
- Conclusion

Higgs 2017

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Higgs and naturalness

- Higgs with $m_h=125$ GeV is somewhat heavy than in typical supersymmetric models and somewhat light than typical prediction of technicolour models.
- People started to question the validity of the naturalness principle.
- My personal point of view: The naturalness principle reflects our current understanding of basics of QFT. A failure of naturalness would mean that these basics must be fundamentally reviewed.

Higgs and naturalness

- P. Dirac was the first who recognized importance of naturalness in quantum physics. He asserted that all the dimensionless parameters of a theory must be of the same order of magnitude (**strong naturalness principle**) – why? – because in quantum theory all the parameters are related to each other via quantum corrections!
- Dirac's Large (Small) Number Hypothesis:

$$\text{Gravity/EM} \propto \left(\frac{m_e}{M_P} \right) \left(\frac{m_p}{M_P} \right) \approx 10^{-40} \quad \text{is} = \left(\frac{m_p}{M_U} \right)^{1/2} \approx 10^{-40}$$

Predicts time variation of Newton's constant, which turned out to be at odds with observations.

- **Lesson:** The principle applies to microscopic parameters. Macroscopic parameters, such as mass of the universe M_U can be random (maybe CC is the same?).

Higgs and naturalness

- G. 't Hooft: Dimensionless parameter can be small if it is supported by a symmetry (**technical naturalness**):

$$\left(\frac{m_e}{M_P}\right) \ll 1 - \text{chiral symmetry}$$

$$\left(\frac{m_p}{M_P}\right) \ll 1 - \text{dimensional transmutation in QCD, a.k.a. scale invariance}$$

- Higgs mass naturalness:

$$\left(\frac{m_h}{M_P}\right) \ll 1 - ???$$

Higgs and naturalness

- Consider an effective theory with a ‘physical’ cut-off Λ , which contains scalars, S, fermions, F, and vector fields, V.
- 1-loop scalar mass term:

$$m_S^2(\mu) = m_S^2(\Lambda) + \frac{1}{32\pi^2} \text{STr } g_A [\Lambda^2 - M_A^2 \ln(\Lambda^2/\mu^2)]$$

$$\text{STr} \equiv (-1)^{2J_A} (2J_A + 1)$$

- $m_S^2 \ll \Lambda^2$ requires fine-tuning and thus is unnatural
(hierarchy problem)
- According to ‘t Hooft we need a symmetry to remove quadratic dependence on UV scale

Higgs and naturalness

- Supersymmetry

Non-renormalisation theorem:

$$\text{STr } g_A = 0 \quad (\text{holds in for softly broken supersymmetry})$$

$$\text{STr } g_A M_A^2 = 0$$

Quadratic divergences are absent in softly broken supersymmetry!

- Scale invariance

$$m_S^2(\mu = \Lambda) = 0 \rightarrow \bar{m}_S^2(\Lambda) + \text{STr } g_A \Lambda^2 = 0$$

Classical scale invariance is broken spontaneously and explicitly by logarithmic quantum corrections,

$$T_\mu^\mu = \sum_i \beta_i \mathcal{O}_i \quad - \text{dimensional transmutation}$$

Scale invariant SM with light dilaton

- Consider SM as an effective Wilsonian theory with ‘physical’ cut-off Λ .

$$V(\Phi^\dagger \Phi) = V_0(\Lambda) + \lambda(\Lambda) [\Phi^\dagger \Phi - v_{ew}^2(\Lambda)]^2 + \dots,$$

- Assume, the ‘fundamental’ theory exhibits conformal invariance, which is spontaneously broken down to the Poincare invariance,

$$SO(2, 4) \rightarrow ISO(1, 3)$$

Only one scalar (pseudo)Goldstone is relevant in the low energy theory, the **dilaton**, $\chi(x)$

- Promote all dimensionfull parameters in the low energy action to $\chi(x)$ [Coleman, 85’]:

$$\Lambda \rightarrow \Lambda \frac{\chi}{f_\chi} \equiv \alpha\chi, \quad v_{ew}^2(\Lambda) \rightarrow \frac{v_{ew}^2(\alpha\chi)}{f_\chi^2} \chi^2 \equiv \frac{\xi(\alpha\chi)}{2} \chi^2, \quad V_0(\Lambda) \rightarrow \frac{V_0(\alpha\chi)}{f_\chi^4} \chi^4 \equiv \frac{\rho(\alpha\chi)}{4} \chi^4$$

Scale invariant SM with light dilaton

- Theory becomes manifestly scale invariant (up to quantum anomaly):

$$V(\Phi^\dagger \Phi, \chi) = \lambda(\alpha\chi) \left[\Phi^\dagger \Phi - \frac{\xi(\alpha\chi)}{2} \chi^2 \right]^2 + \frac{\rho(\alpha\chi)}{4} \chi^4$$

$$\lambda^{(i)}(\alpha\chi) = \lambda^{(i)}(\mu) + \beta_{\lambda^{(i)}}(\mu) \ln(\alpha\chi/\mu) + \beta'_{\lambda^{(i)}}(\mu) \ln^2(\alpha\chi/\mu) + \dots,$$

$$\beta_{\lambda^{(i)}}(\mu) = \left. \frac{\partial \lambda^{(i)}}{\partial \ln \chi} \right|_{\alpha\chi=\mu} \sim \mathcal{O}(\hbar) , \quad \beta'_{\lambda^{(i)}}(\mu) = \left. \frac{\partial^2 \lambda^{(i)}}{\partial (\ln \chi)^2} \right|_{\alpha\chi=\mu} \sim \mathcal{O}(\hbar^2) , \dots$$

- At leading order dilaton-SM interactions are given by:

$$\mathcal{L}_{\chi-SM} \propto \frac{\chi}{f_\chi} T_\mu^\mu \text{ (SM anomaly)}$$

Scale invariant SM with light dilaton

- Find vacuum configuration + impose cancelation condition on vacuum energy:

$$\begin{aligned} \left. \frac{dV}{d\chi} \right|_{\Phi=\langle\Phi\rangle, \chi=\langle\chi\rangle} &= 0 & \rho(\Lambda) &= 0, \\ \left. \frac{dV}{d\Phi} \right|_{\Phi=\langle\Phi\rangle, \chi=\langle\chi\rangle} &= 0 & \beta_\rho(\Lambda) &= 0, \\ & \Rightarrow & \xi(\Lambda) &= \frac{v_{ew}^2}{v_\chi^2}. \\ V(v_{ew}, v_\chi) &= 0 \end{aligned}$$

- Scalar mass spectrum:
$$m_h^2 \simeq 2\lambda(\Lambda)v_{ew}^2,$$
$$m_\chi^2 \simeq \frac{\beta'_\rho(\Lambda)}{4\xi(\Lambda)}v_{ew}^2 \propto m_h^2\xi,$$
$$\sin\alpha \sim \sqrt{\xi}$$

Scale invariant SM with light dilaton

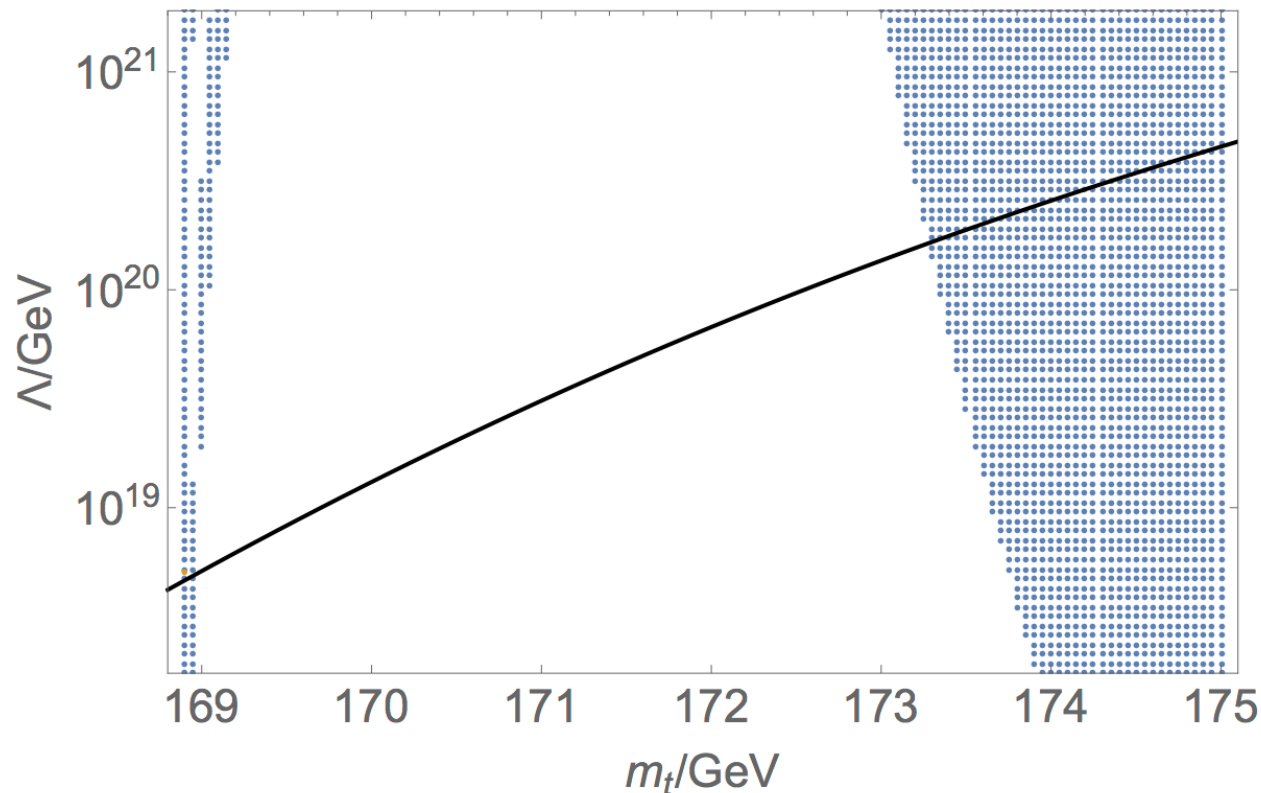


Figure 1: Plot of the allowed range of parameters (shaded region) with $m_\chi^2(v_{ew}) > 0$, i.e., the electroweak vacuum being a minimum. The solid line displays the cut-off scale Λ as function of the top-quark mass m_t for which the conditions in Eq. (6) are satisfied.

- If $\Lambda \sim 10^{19}$ GeV, $m_\chi \sim 10^{-8}$ eV!

Scale invariant SM with light dilaton

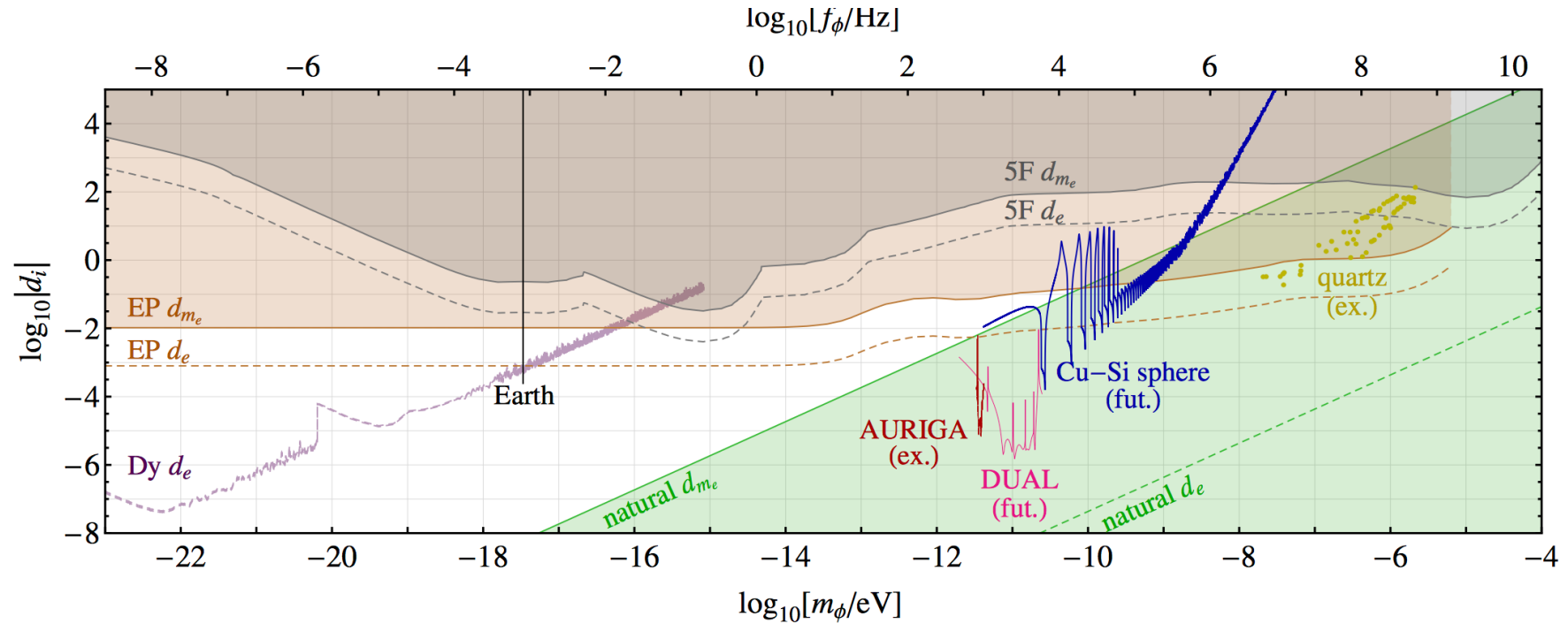


FIG. 1. Scalar field parameter space, with mass m_ϕ and corresponding DM oscillation frequency $f_\phi = m_\phi/2\pi$ on the bottom and top horizontal axes, and couplings of both an electron mass modulus ($d_i = d_{m_e}$) and electromagnetic gauge modulus ($d_i = d_e$) on the vertical axis. Natural parameter space for a 10 TeV cutoff is depicted in green, while the other regions and dashed curves represent 95% CL limits from fifth-force tests (“5F”, gray), equivalence-principle tests (“EP”, orange), atomic spectroscopy in dysprosium (“Dy”, purple), and low-frequency terrestrial seismology (“Earth”, black). The blue curve shows the projected SNR = 1 reach of a proposed resonant-mass detector—a copper-silicon (Cu-Si) sphere 30 cm in radius—after 1.6 y of integration time, while the red curve shows the reach for the current AURIGA detector with 8 y of recasted data. Rough estimates of the 1-y reach of a proposed DUAL detector (pink) and several harmonics of two piezoelectric quartz resonators (gold points) are also shown.

taken from [arXiv:1508.01798](https://arxiv.org/abs/1508.01798)

Cosmological electroweak phase transition

- Higgs-dilaton potential: the energy densities at the origin and at the electroweak vev are degenerate and are separated by a very small barrier (flat direction lifted by 2-loop quantum corrections).
- Thermal barrier is also generated which implies that the critical temperature of the transition is $T_c=0$.
- QCD condensates drive the electroweak phase transition! (Witten 81')

Cosmological electroweak phase transition

$$V_T(h, \chi) = \frac{\lambda(\Lambda)}{4} \left[h^2 - \frac{v_{ew}^2}{v_\chi^2} \chi^2 \right]^2 + \sum_i n_i (-1)^{2s_i+1} \left[\frac{m_i^4}{32\pi^2} \log \frac{\alpha\chi}{m_i} - \frac{1}{2\pi^2} T^4 J_i(m_i^2/T^2) \right]$$

- High temperature/small field expansion:

$$V_T(h, \chi) = \frac{\lambda(\Lambda)}{4} \left[h^2 - \frac{v_{ew}^2}{v_\chi^2} \chi^2 \right]^2 + c(h) \pi^2 T^4 - \frac{\lambda(\Lambda)}{24} \frac{v_{ew}^2}{v_\chi^2} \chi^2 T^2 + \frac{1}{48} \left[6\lambda(\Lambda) + 6y_t^2(\Lambda) + \frac{9}{2}g^2(\Lambda) + \frac{3}{2}g'^2(\Lambda) \right] h^2 T^2$$

- Solve for the dilaton field:

$$\chi^2 = \frac{v_\chi^2}{v_{ew}^2} h^2 + \frac{v_\chi^2}{v_{ew}^2} T^2$$

Cosmological electroweak phase transition

- The Higgs potential becomes:

$$V_T(h, \chi(h)) = \left[c(h)\pi^2 - \frac{\lambda(\Lambda)}{576} \frac{v_{ew}^2}{v_\chi^2} (2 + v_{ew}^2/v_\chi^2) \right] T^4 \\ + \frac{1}{48} \left[4\lambda(\Lambda) + 6y_t^2(\Lambda) + \frac{9}{2}g^2(\Lambda) + \frac{3}{2}g'^2(\Lambda) \right] h^2 T^2$$

- $4\lambda(\Lambda) + 6y_t^2(\Lambda) + \frac{9}{2}g^2(\Lambda) + \frac{3}{2}g'^2(\Lambda) > 0 \implies h=0$ is a local minimum for any T .
- If so, the universe would be trapped in symmetric vacuum $h=0$.

Cosmological electroweak phase transition

- In $h=0$ vacuum all quarks are massless. $SU(6) \times SU(6)$ chiral symmetry is broken at $T_c \sim 132$ MeV. The quark condensate breaks the electroweak symmetry as well.

$$\langle \bar{q}q \rangle_T = \langle \bar{q}q \rangle \left[1 - (N^2 - 1) \frac{T^2}{12N f_\pi^2} - \frac{1}{2} (N^2 - 1) \left(\frac{T^2}{12N f_\pi^2} \right)^2 + \mathcal{O}((T^2/12N f_\pi^2)^3) \right]$$
$$\langle \bar{q}q \rangle \approx -(250 \text{ MeV})^3$$

(Gasser & Leutwyler, 86')

- Higgs-quark Yukawa interactions: $y_q \langle \bar{q}q \rangle_T h / \sqrt{2}$
- $y_q \langle \bar{q}q \rangle_T / \sqrt{2} + \frac{\partial V_T}{\partial h} = 0 \rightarrow h=0$ is no more an extremum

Cosmological electroweak phase transition

- Quark condensate tips the Higgs field from the origin, which ‘runs down’ classically towards the electroweak minimum, smoothly and quickly completing the transition

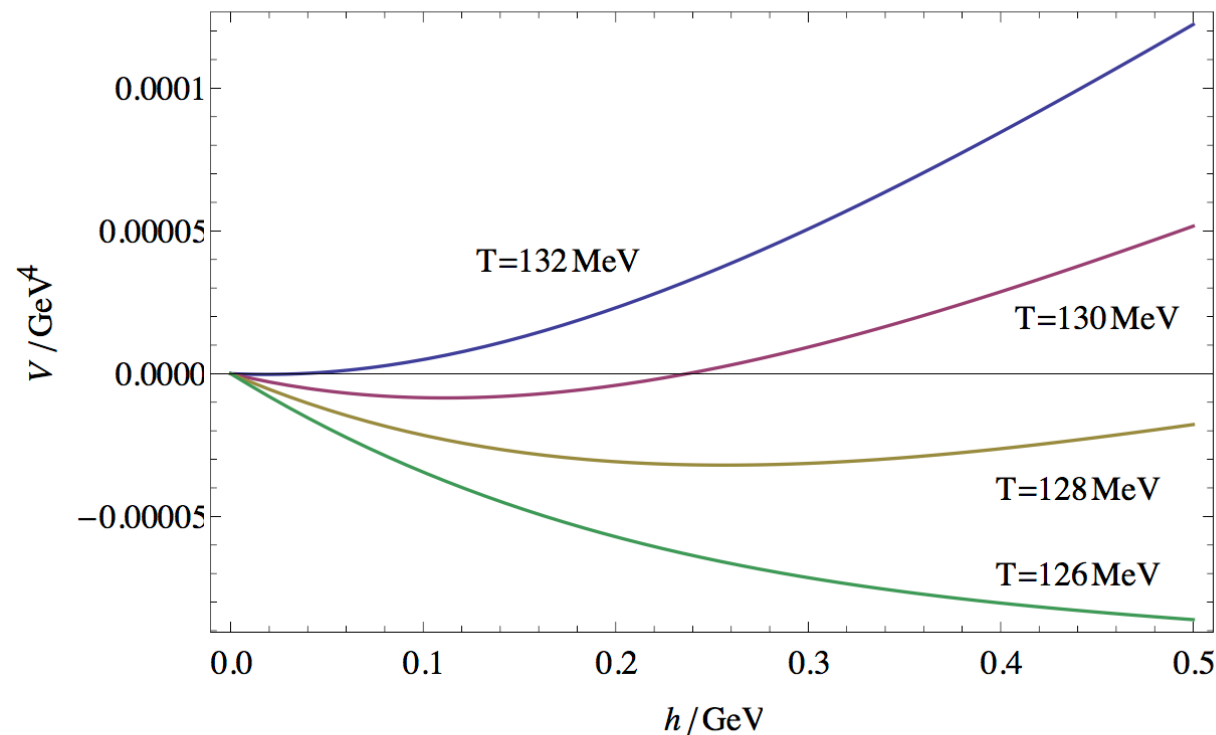


Figure 2: $V_T(h) - V_T(0)$ for different temperatures below the chiral phase transition.

Cosmological electroweak phase transition

- QCD with $N=6$ quarks undergoes first-order phase transition, unlike the standard case with $N=3$.
- Gravitational waves with peak frequency $\sim 10^{-8}$ Hz, potentially detectable by means of pulsar timing (EPTA, SKA...)
- Production of primordial black holes with mass $M_{bh} \sim M_{\odot}$
- QCD baryogenesis(?)

Conclusion

- Scale invariant theories predict a light feebly coupled dilaton.
- Electroweak phase transition driven by the QCD chiral phase transition and occurs at $T \sim 130$ MeV.
- QCD phase transition could be strongly first order => gravitational waves, black holes, cold baryogenesis.
- Detection of a light scalar particle + the above astrophysical signatures will provide strong evidence for the fundamental role of scale invariance in particle physics and cosmology.