



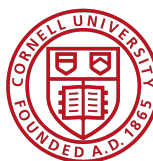
# Variable Gap Tapering for LCLS-II Undulators

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**SLAC**

NATIONAL  
ACCELERATOR  
LABORATORY



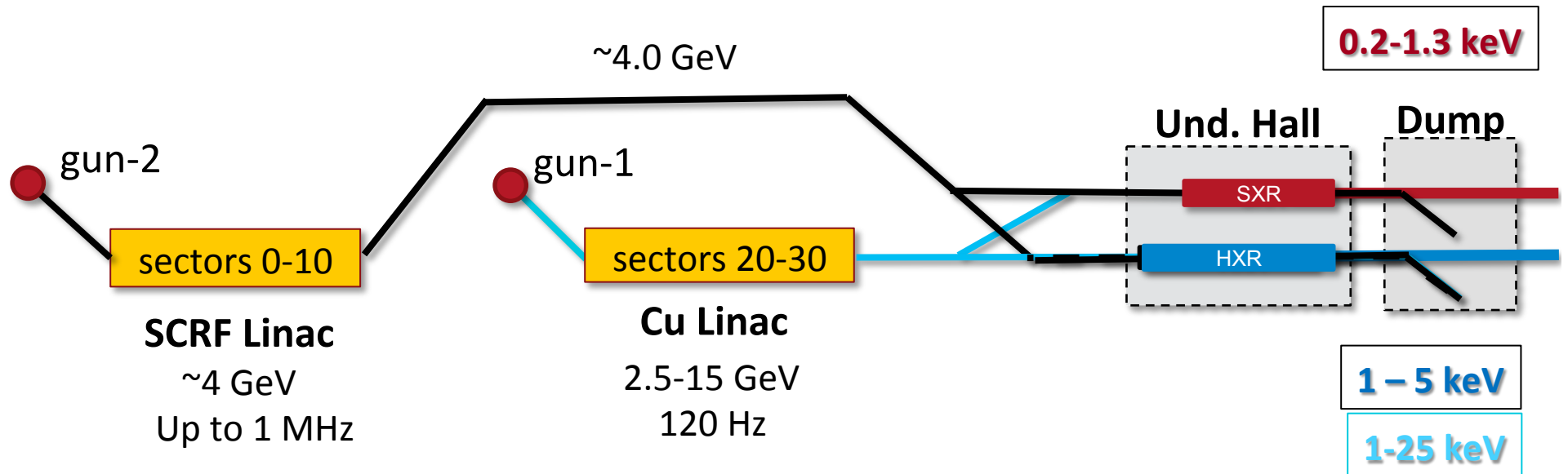
**Fermilab**

**Jefferson Lab**

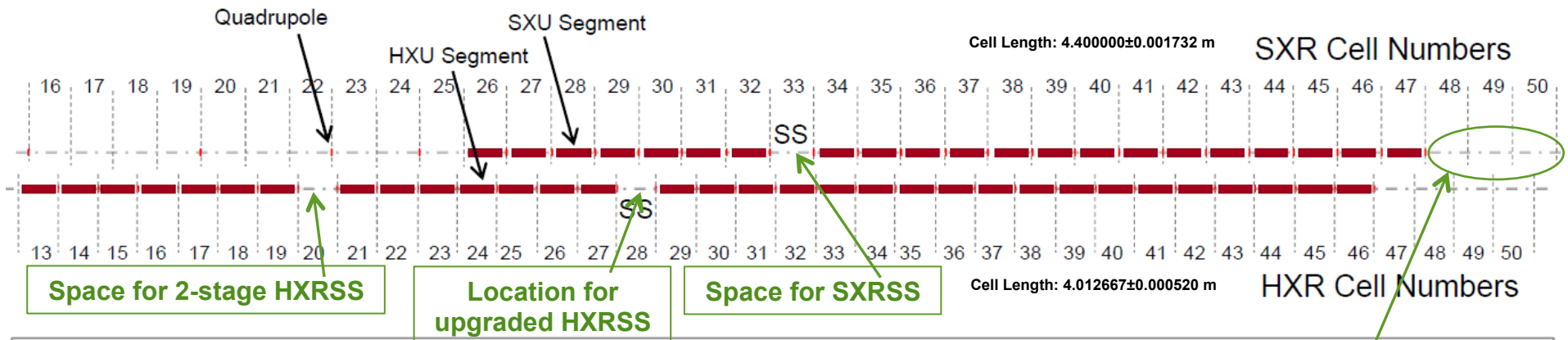


# Schematic Layout of LCLS-II

- New Soft X-ray FEL with adjustable-gap undulator line (SXR)
- New Hard X-ray FEL with adjustable-gap undulator line (HXR)



# LCLS-II SXR and HXR Component Layouts



## Component Summary:

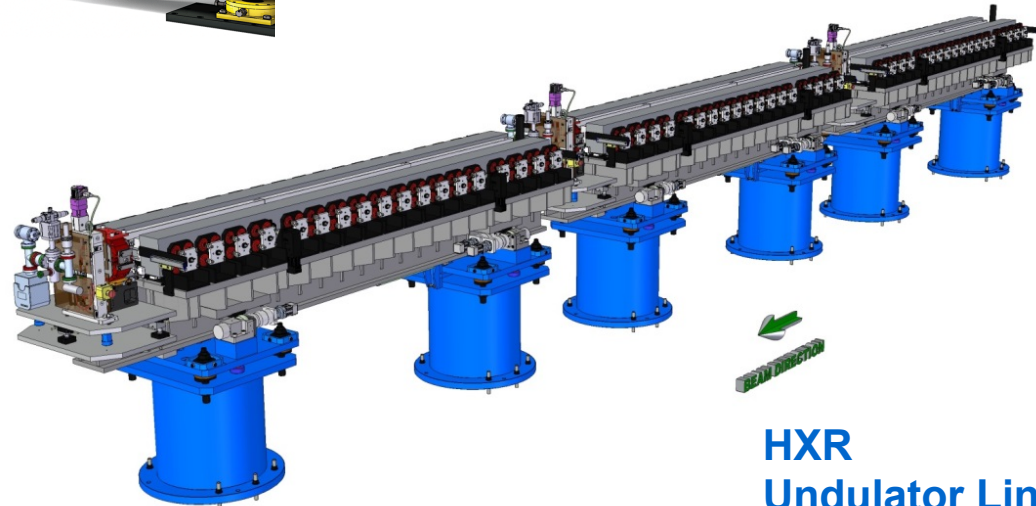
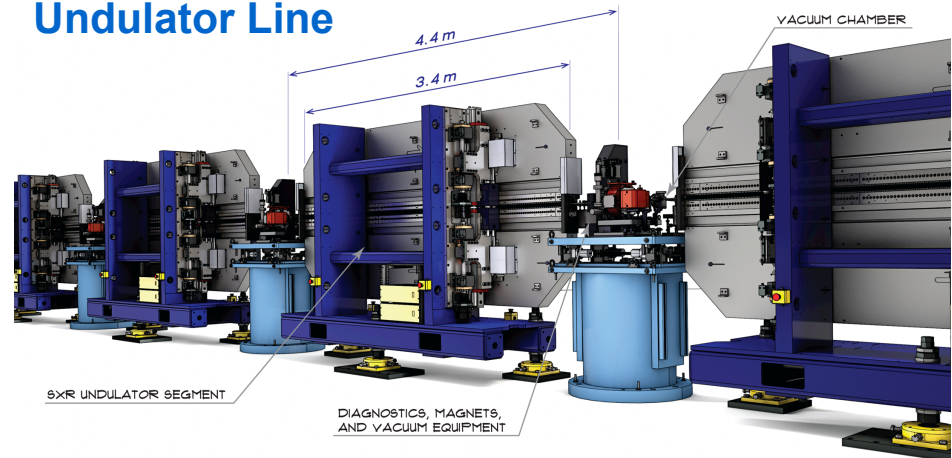
SXU	(#21)	: SXR26-SXR32; SXR34-SXR47
HXU	(#32)	: HXR13-HXR19; HXR21-HXR27; HXR29-SXR46
Quad <sup>+</sup>	(#60)	: SXR15; SXR19; SXR22; SXR24, SXR26-SXR47; HXR13-HXR46;
RFBPM <sup>++</sup>	(#60+2)	: SXR24; SXR25; SXR26-SXR47; (+1); HXR12; HXR13; HXR14-HXR46; (+1)
SXR-PS <sup>++</sup>	(#20)	: SXR26-SXR32; SXR34-SXR46
HXR-PS <sup>++</sup>	(#31)	: HXR14-HXR19; HXR22-HXR27; HXR29-HXR46
BLM <sup>+</sup>	(#53)	: SXR26-SXR32; SXR34-SXR47 ; HXR13-HXR19 ; HXR21-HXR27; HXR29-SXR46

<sup>+</sup> Same Cell as following segment

<sup>++</sup> Same Cell as previous segment

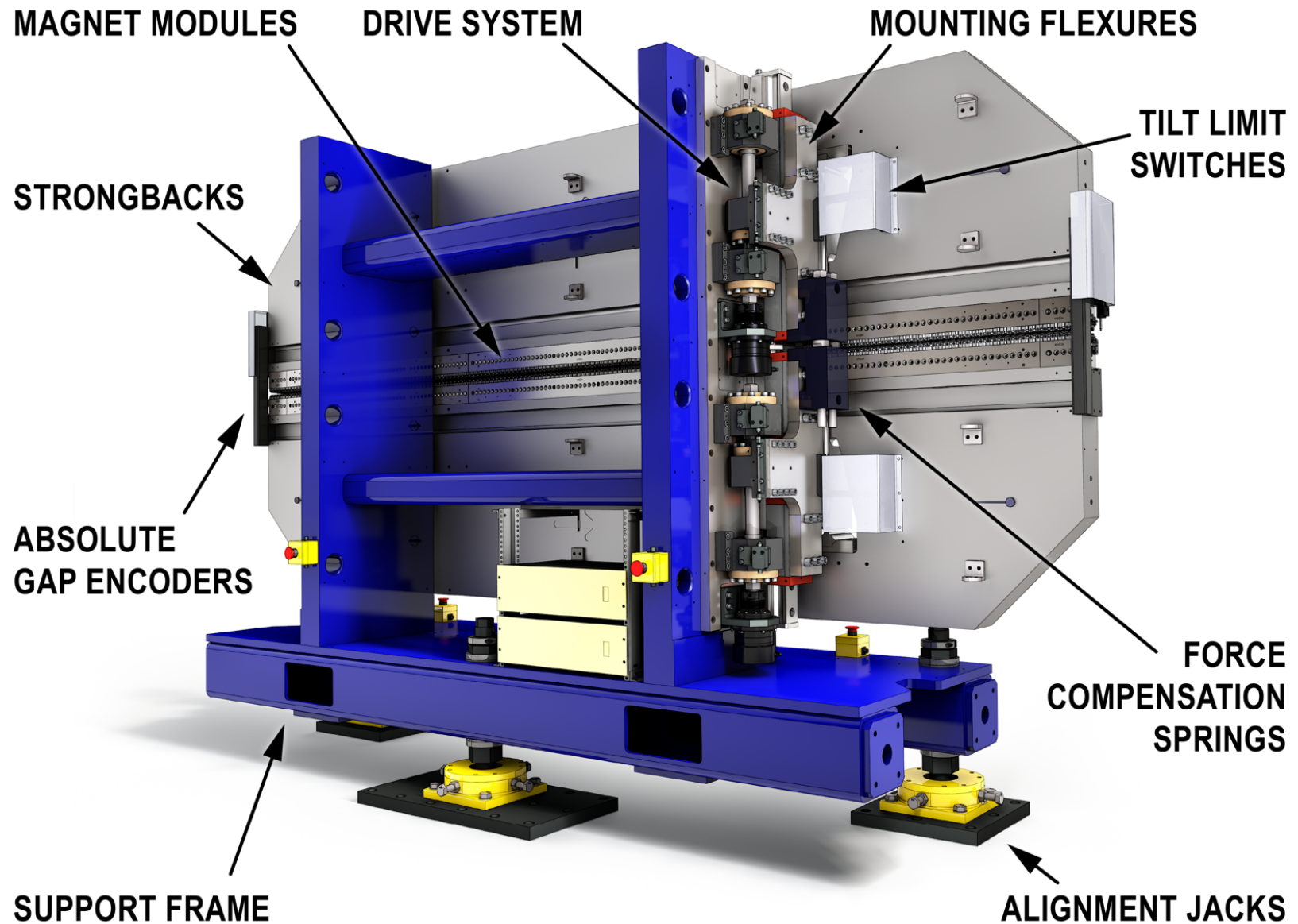
# Undulator System Layout

## SXR Undulator Line



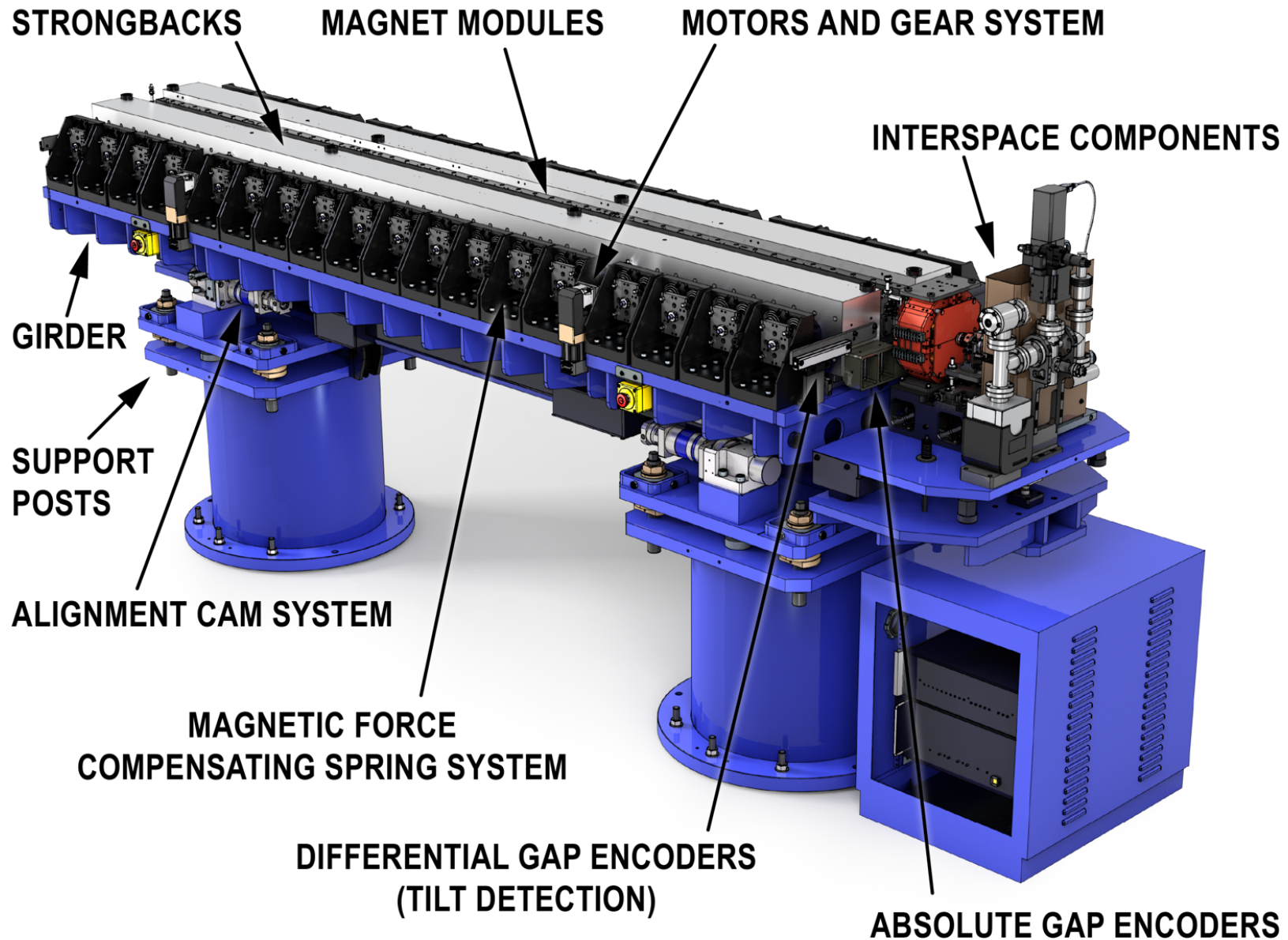
## HXR Undulator Line

# LCLS-II SXR Undulator (HPU)





# LCLS-II HXR Undulator (VPU)

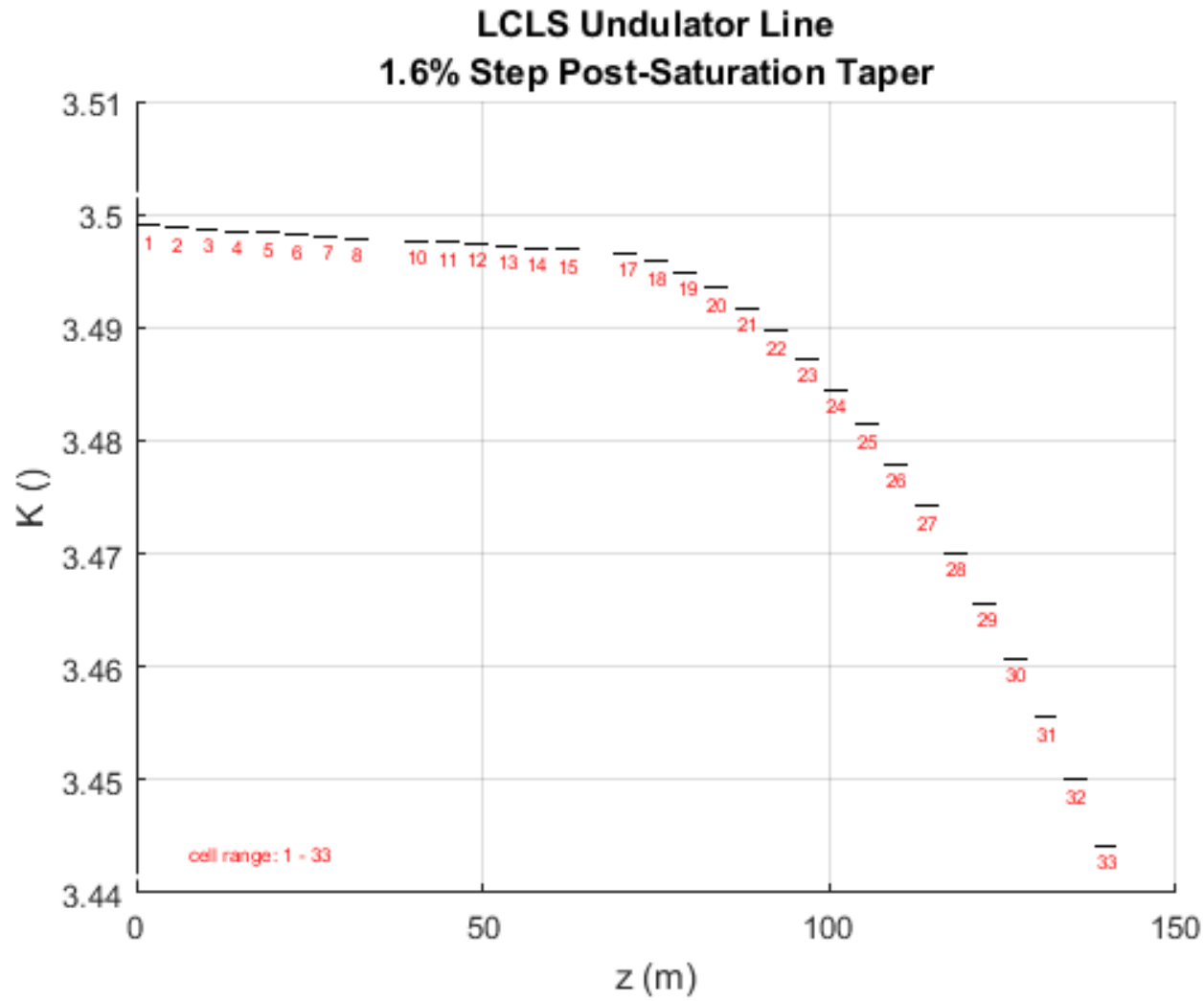


# LCLS-II Undulator Dimensions and Ranges

Parameter	SXU / SCRF	SXU / Cu	HXU / SCRF	HXU / Cu	Unit
Undulator period length	39		26		mm
Total segment length	3.4		3.4		m
Number of periods per strong back	87		130		
X-ray energy range, required*	0.2 – 1.3	0.2 – 10	1.0 – 5.0	1 – 25	keV
Undulator operational gap range	7.2 – 20	7.2 – 20	7.2 – 18	7.2 – 19	mm
Undulator parameter range, $K$	5.5 – 1.5	5.5 – 1.5	2.4 – 0.57	2.4 – 0.54	
Electron energy range, operational	3.6 – 4.0	2.5 – 9	3.3 – 4.0	2.5 – 15	GeV
Maximum gap taper	300		300		$\mu\text{m}$

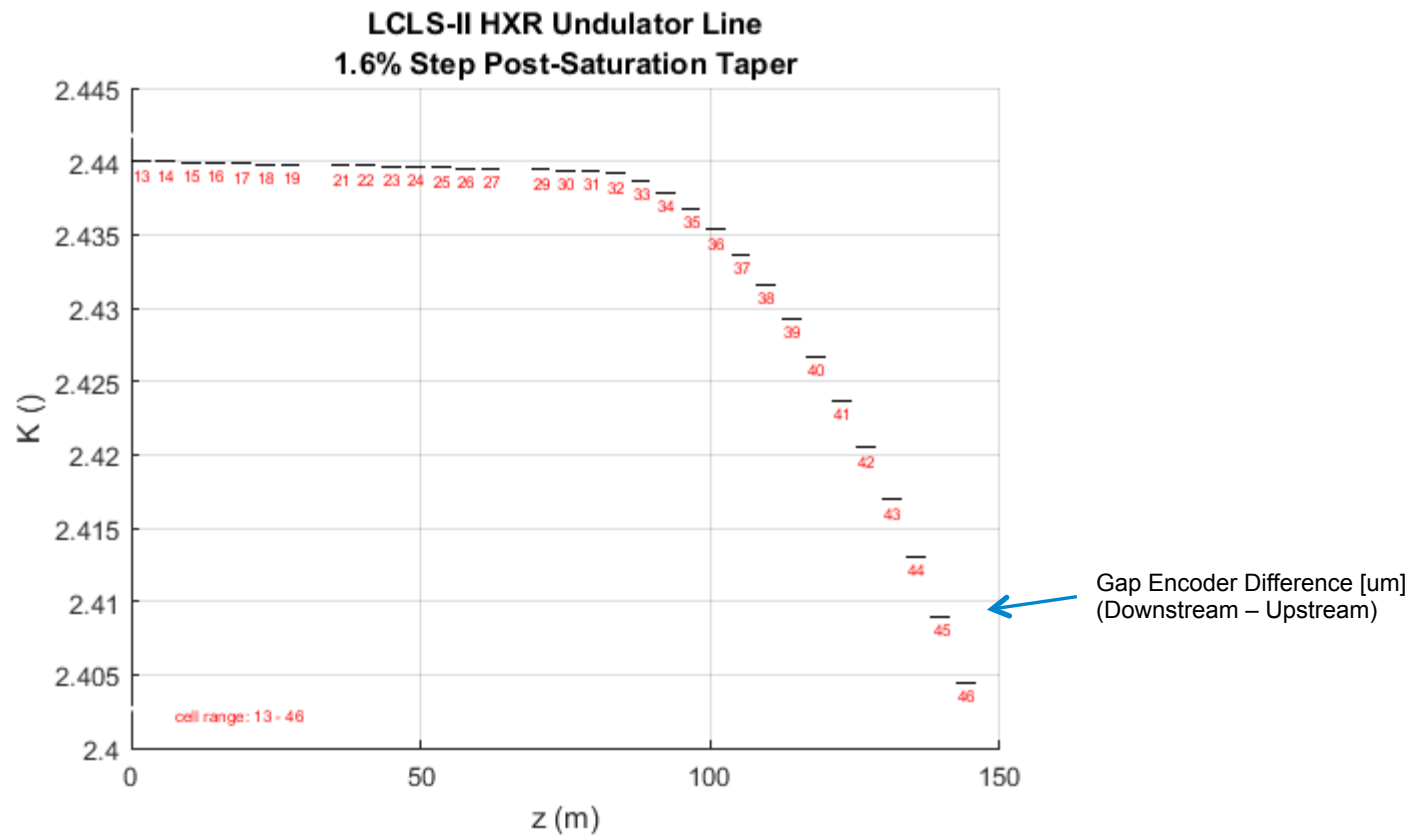
\*at 4.0 GeV, the lower limit is 0.25 and 1.5 keV, respectively

# LCLS Step Taper Only



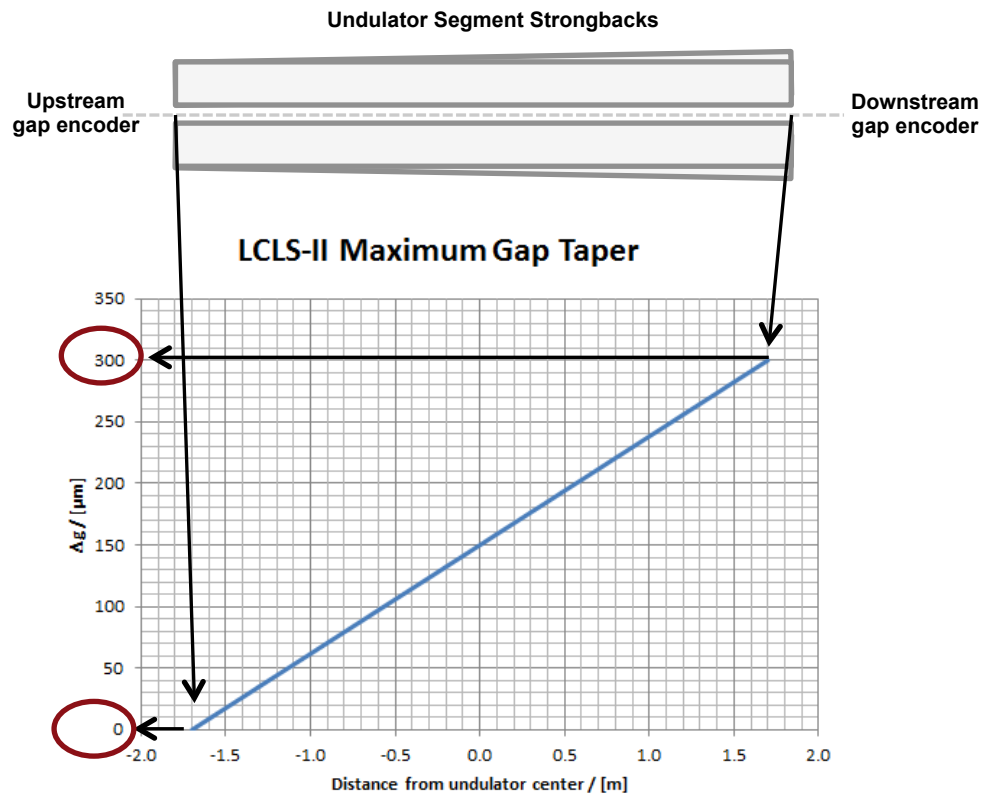


# LCLS-II Allows Continuous Taper



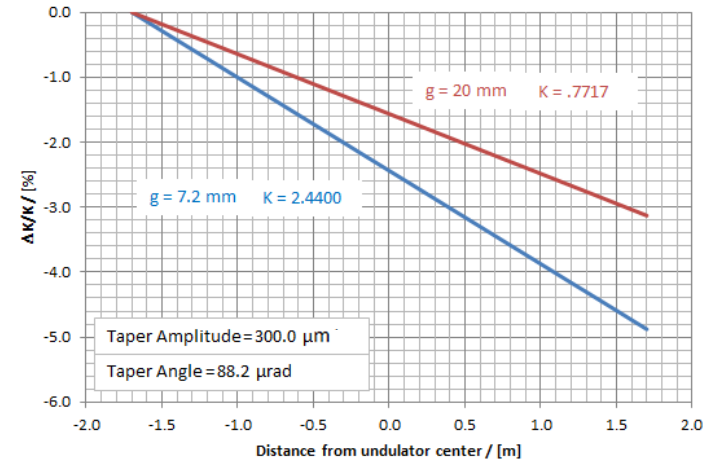
# LCLS-II Undulator Segment

300 μm taper over 3.4-m segment length (~88 μrad)

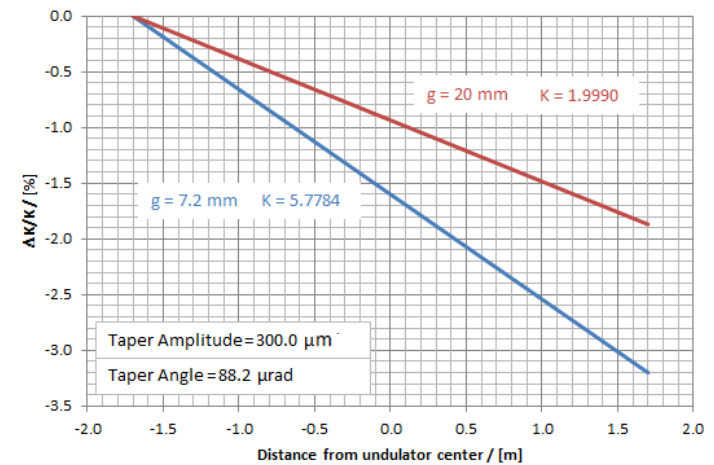


$$\Delta K/K \approx - (5.08 - 3.08 g/\lambda u) \Delta g/\lambda u$$

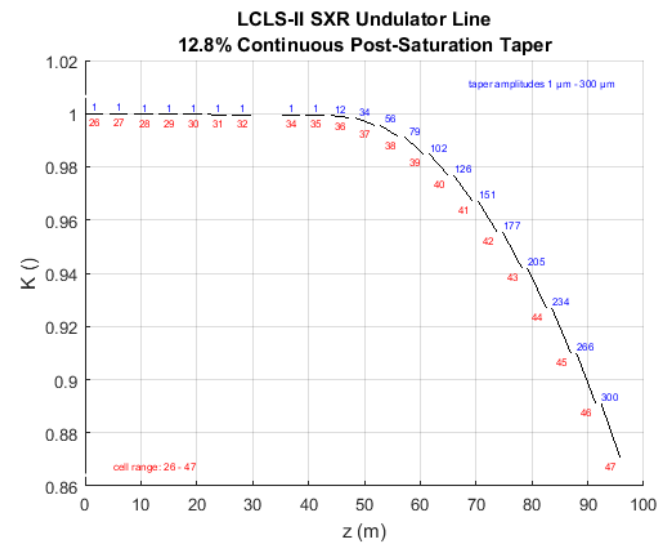
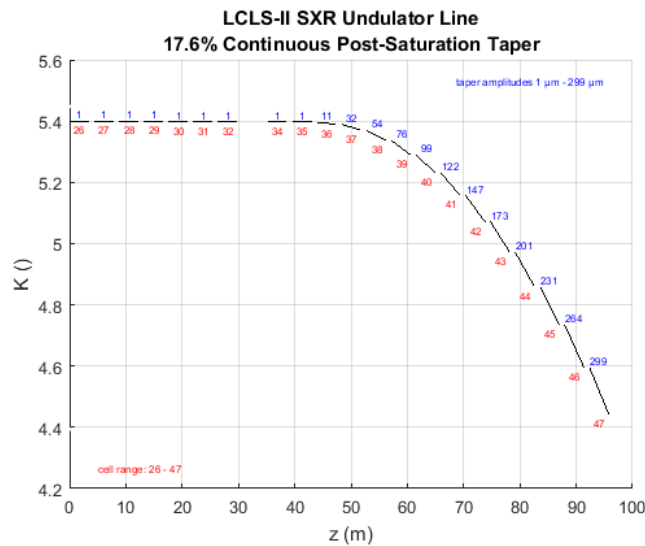
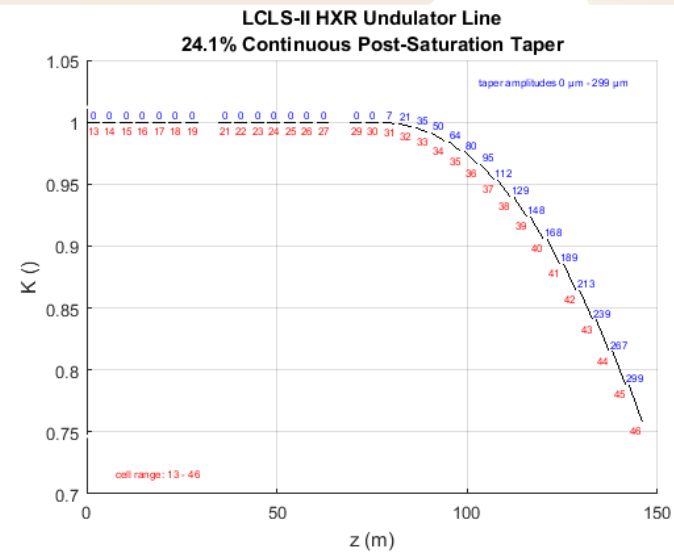
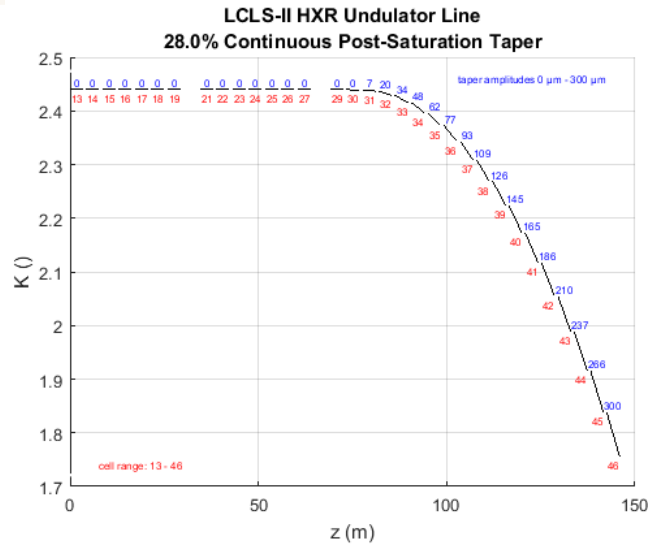
LCLS-II HXR Maximum Gap Taper



LCLS-II SXR Maximum Gap Taper



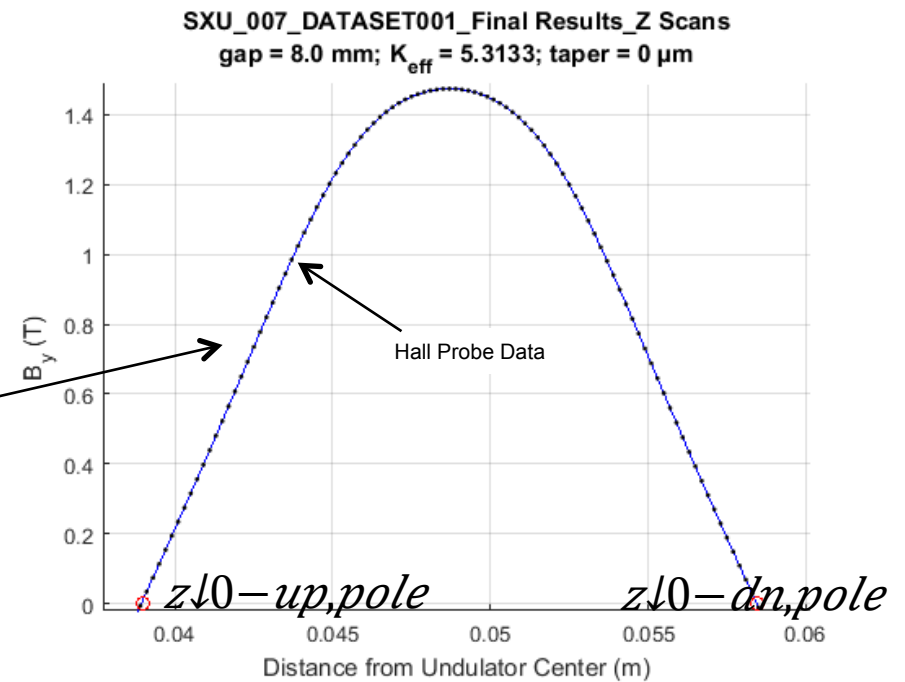
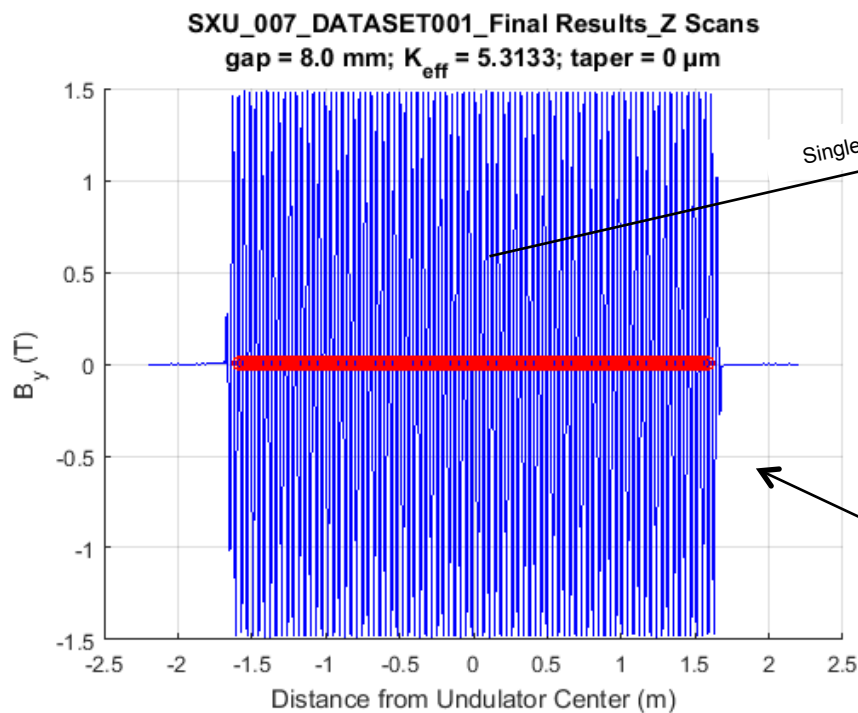
# Large Taper Ranges at LCLS-II



# SXU-007 Field Measurements: (1) Untapered

$$\langle K_{pole} \rangle = 5.3153 \pm 0.0006$$

$$K_{eff} = 5.3133 \pm 0.0001$$

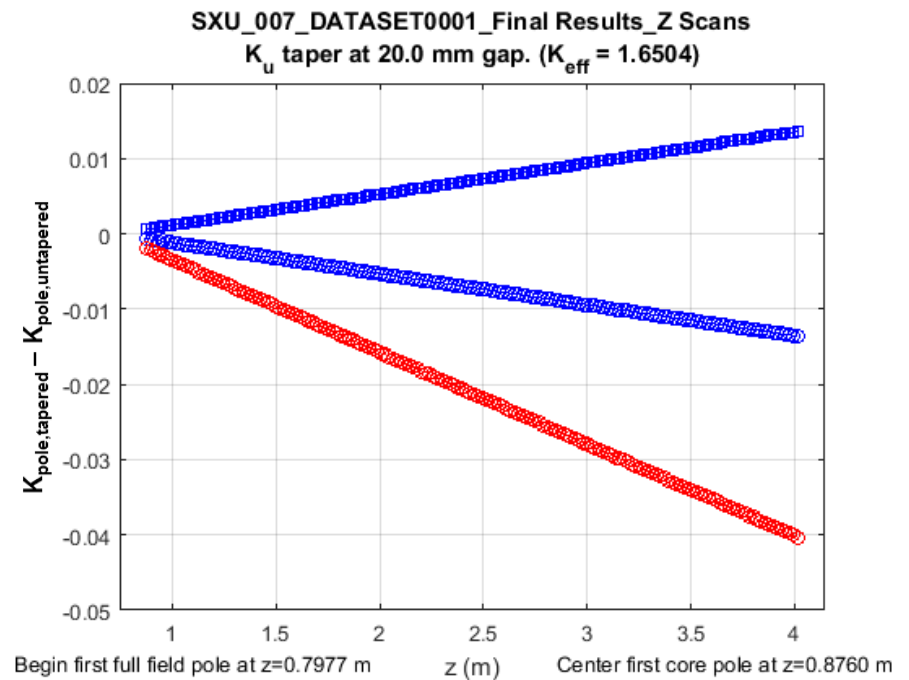
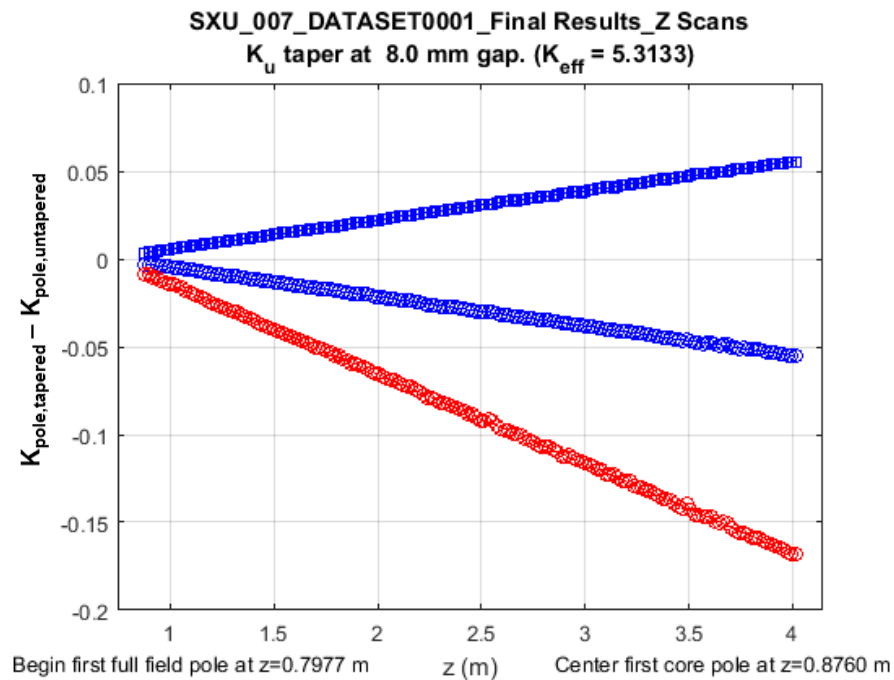


$$K_{pole}(z_{pole}) = \Delta z_{pole} / 2\pi e / m_e c v$$

$$\Delta z_{pole} = z_{0-dn,pole} - z_{0-up,pole}$$

$$z_{pole} \approx 1/2 (z_{0-dn,pole} + z_{0-up,pole})$$

# SXU-007 Field Measurements: (2) Tapered

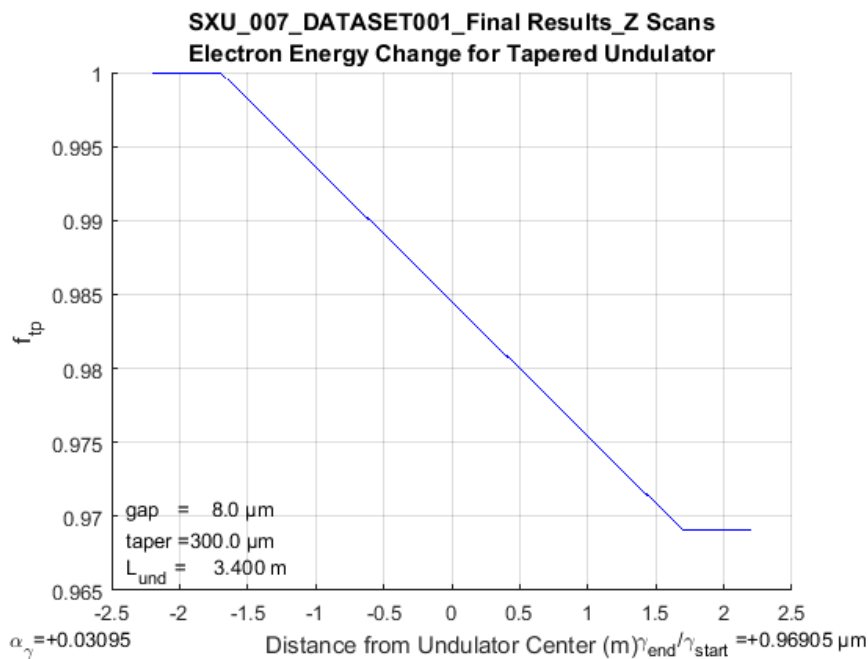


- Measured  $K_{pole}$  values for SXU tapers of +100  $\mu\text{m}$  and +300  $\mu\text{m}$  and reversed taper of -100  $\mu\text{m}$  at 8 mm and 20 mm gap.
- Difference between tapered and untapered  $K_{pole}$  values is only according to gap change.  
(No distortion at large tapers observed)



# Field Evaluations for Tapered Undulators

- Standard calculations of phase shake and total phase assume constant beam energy and can not be applied to tapered undulators.
- Instead assume that taper is necessary because of energy loss along undulator segment, i.e.,  $\gamma = \gamma(z) = \gamma_{start} (1 - \alpha z)$
- A value for  $\alpha$  can be found that minimizes the change of phase advance per period.



$$\gamma(z) = \gamma_{start} f_{tp}(z)$$

$$f_{tp}(z) = \begin{cases} 1 & \text{for } z < z_{u,start} \\ 1 - \alpha z & \text{for } z_{u,start} < z < z_{u,end} \\ \text{constant} & \text{for } z > z_{u,end} \end{cases}$$

# Phase Calculations

- The phase slippage for changing energy along undulator segment is

$$\Delta\phi_{\text{taper}}(z) = 2\pi/\lambda_{\text{u}} \left( 1 + \frac{1}{2} K(g_{\text{start}})^2 \right) \int_0^z \frac{1}{\beta_{\text{tp}}(z)^2} (1 - \dots)$$

- The field integrals are calculated as usual

$$\int_0^z B_x(z) dz \quad \int_0^z B_y(z) dz$$

- The slopes and trajectories are

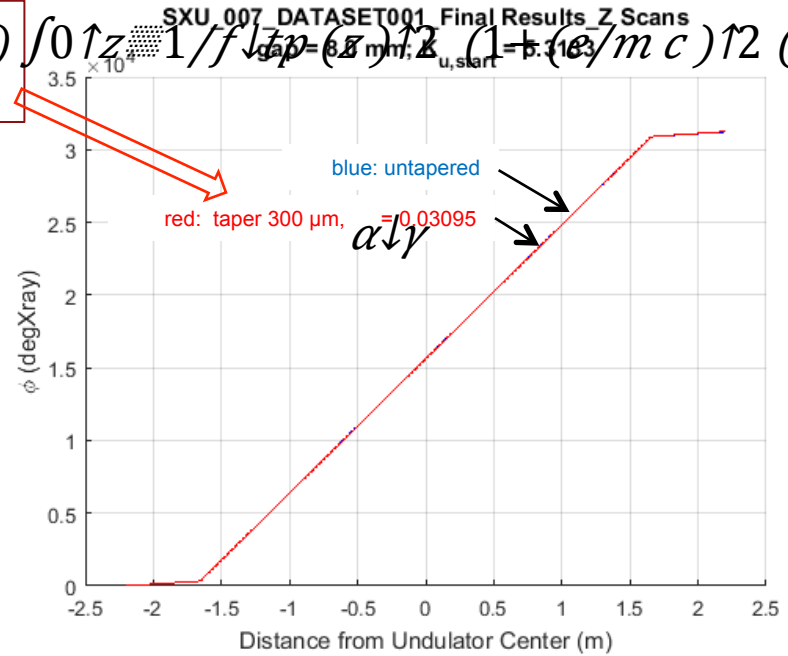
$$d/dz y(z) = -1/(B\rho)_{\text{start}} \int_0^z \frac{1}{\beta_{\text{tp}}(z)} dz$$

$$(B\rho)_{\text{start}} = \gamma_{\text{start}} m c/e$$

$$y(z) = -1/(B\rho)_{\text{start}} \int_0^z \frac{1}{\beta_{\text{tp}}(z)} dz$$

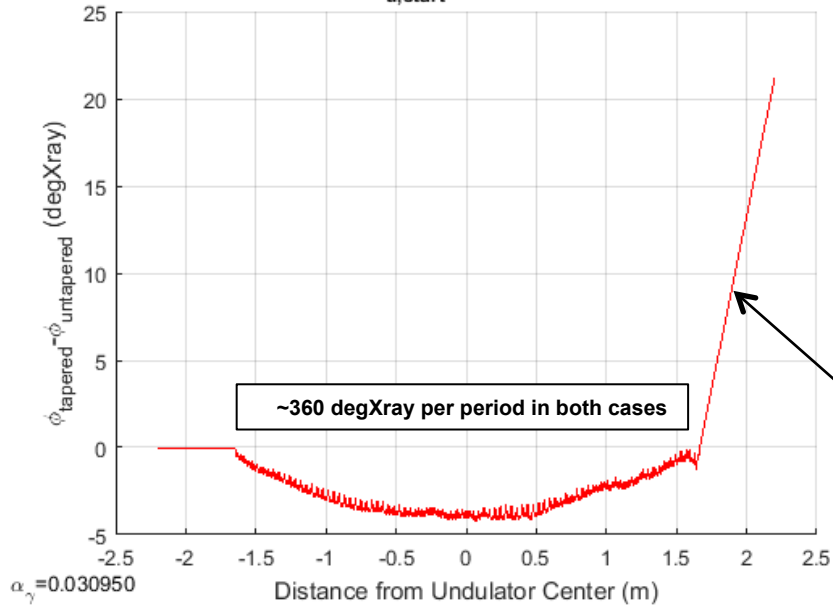
# Phase Measurements

$$\Delta\phi_{\text{taper}}(z) = 2\pi/\lambda \left[ u \left( 1 + \frac{1}{2} K(g_{\text{start}})^2 \right) \int_0^z \frac{1}{f_{\text{gap}}(z')} dz' \right] \left( 1 + \frac{e}{m c} \right)^2 (1/x(z))$$



Difference

SXU\_007\_DATASET001\_Final Results\_Z Scans  
gap = 8.0 mm;  $K_{u,\text{start}} = 5.3133$ ; taper = 300  $\mu\text{m}$



During free space travel after undulator, phase advance per unit length is longer for larger regular tapers due to lower electron energies.

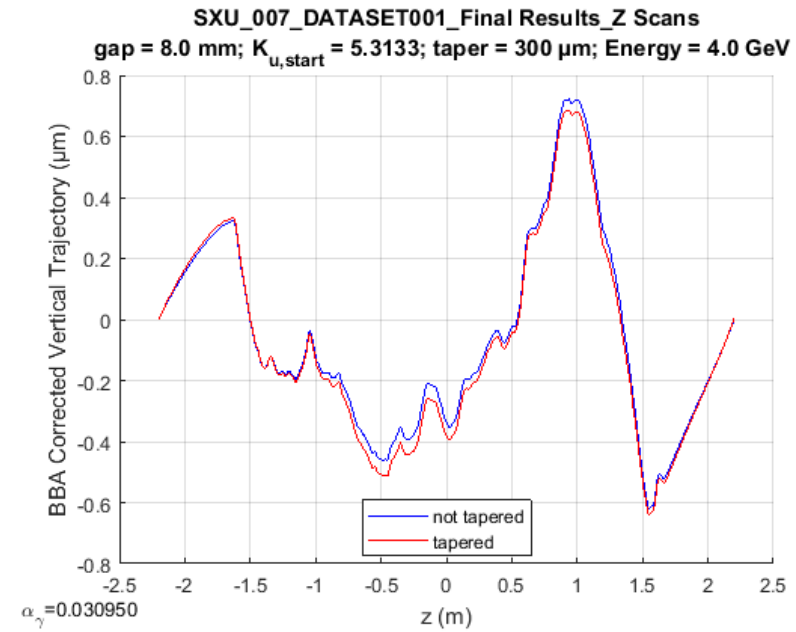
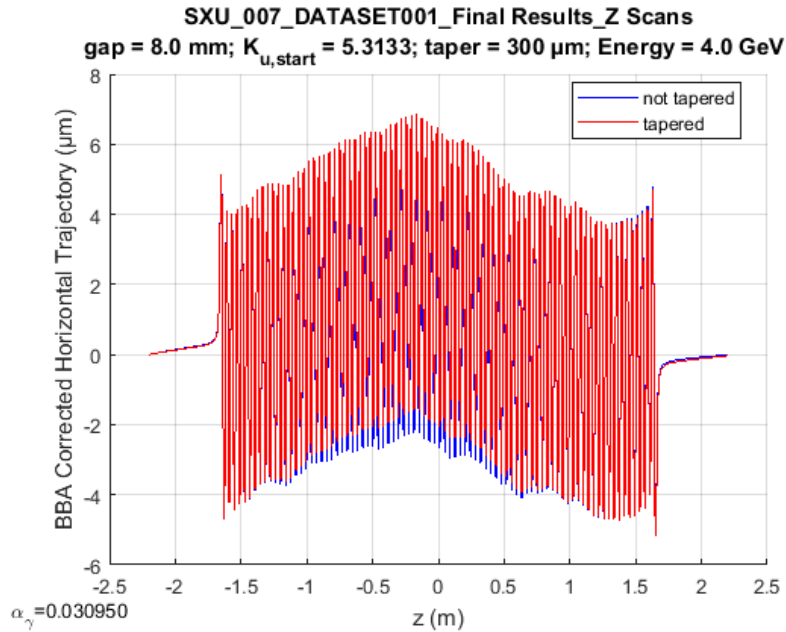
$$d/dz (\phi_{\text{tapered}} - \phi_{\text{untapered}}) = 360/\lambda \left[ u \left( 1 + \frac{1}{2} K(g_{\text{start}})^2 \right) \right] \left( 1 + \frac{e}{m c} \right)^2$$

For SXU-007, at 300  $\mu\text{m}$  taper and 8 mm gap

$$d/dz (\phi_{\text{tapered}} - \phi_{\text{untapered}}) = 38.6 \text{ degXray / m}$$

This will be corrected with a phase shifter.

# SXU-007 Trajectories



- BBA corrected horizontal and vertical trajectories for +300  $\mu\text{m}$  SXU taper based on field measurements.
- Only insignificant deviation from untapered trajectories observed.

# Summary

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- The LCLS-II undulators allow continuous gap tapering
- Limits are  $\pm 300 \mu\text{m}$  over segment length ( $\sim \pm 88 \mu\text{rad}$ )
- SXU taper measurements look promising:
- If adjusted to compensate for energy loss, tapering
  - will mostly change the downstream phase advance
  - will only slightly increase overall phase shake
  - will not significantly steer the electron beam
- HXU (vertically polarizing undulator) taper measurements will follow soon



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**Thank you for your  
attention!**