U.S.NAVAL RESEARCH LABORATORY **Understanding Space Plasmas Through** Laboratory Experiments

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Space-Time Ambiguity

Makes detection and characterization of a specific space plasma phenomenon tricky

Unsteady Plasma

- When orbiting sensors return to the position of the original measurement the plasma has evolved
- Meaningful statistical ensemble through repeated measurements not possible

Multiple Uncontrolled Variables

- Usually there are many variables and multiple forces operating simultaneously
- Difficult to pinpoint the causality of events and isolate a specific phenomenon for precise measurements for unambiguous characterization

Mitigation: Scaled Laboratory Experiments

- Controlled environment scaled to the appropriate space conditions
 - Anchor theory using laboratory experiments and then apply the validated model to space conditions
 - Compare laboratory experiments to space data





Space Plasma Processes Optimal for Laboratory Experiments

- Turbulence
 - Understand turbulence properties in the meso and micro scales
 - Kinetic effects
 - Turbulence pervades most plasma domains
 - Astrophysics, hemisphere, magnetosphere, ionosphere, tokamaks, etc.
 - Fundamental yet practical

Spatial Variability

- Understand the cause and effects of spatial variability in the background parameters
- Many space plasma phenomena associated with strong spatial inhomogeneities

Multi-Ion-Species Effects

Most space plasmas are multispecies

Astrophysical Plasma Processes

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Small Scale Turbulence Properties: Electrostatic or Electromagnetic?





Electrostatic \Rightarrow Electromagnetic: **Dispersive Properties of Whistler Branch Waves**

• Cold plasma dispersion relation for the whistler branch waves in $(\Omega_i < \omega < \Omega_e)$ frequency range

$$\omega^{2} = \left(\frac{\bar{k}_{z}^{2}}{(1+\bar{k}_{y}^{2})} + \mu\right) \frac{\bar{k}^{2} \Omega_{e}^{2}}{1+\bar{k}^{2}} \qquad \mu = m_{e} / m_{i}$$

$$\bar{k} = kc / \omega_{pe}$$

$$O(1) \qquad 0 \qquad O(1)$$

$$E_{x} = -ik_{x} \phi \left(1 + \frac{\bar{k}_{z}^{2}}{\bar{k}_{\perp}^{2}}\right) \qquad E_{y} = E / \frac{i\omega}{\Omega_{e}\bar{k}^{2}} \qquad E_{z} = -ik_{z} \phi \left(\frac{\bar{k}}{\bar{k}}\right)$$

$$E_{z} = -ik_{z} \phi \left(\frac{\bar{k}}{\bar{k}}\right) \qquad (1+\bar{k})^{2} \qquad (1+\bar{$$

Electrostatic if k >> 1 and $k_{\perp} >> k_{z}$

- **EM Whistlers** $\bar{k}_{y}^{2} < 1 \quad \bar{k}_{z}^{2} > \mu$ -
- **ES Lower Hybrid** $\overline{k}_y^2 > 1$ $k_z^2 / k_y^2 < \mu$ -
- **EM Magnetosonic** $\overline{k}_v^2 < 1$ $\overline{k}_z^2 < \mu$ -

- **ES Whistlers** $\overline{k}_y^2 > 1 \quad 1 > k_z^2 / k_y^2 > \mu$

[Ganguli et al., **PoP**, 2010]

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Magnetosphere





TRAJECTORY OF CHARGED PARTICLES

 $D(\omega, k, n(r), B(r)) = 0$

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Laboratory Validation of Nonlinear Conversion

Scattering rate by thermal electrons in EM limit

– Generalize Hasegawa and Chen 1976







• Wave-particle resonance can be easily met for any combinations of (k_|, k_) with ω ~ constant

NRL Space Chamber Validation

[Tejero et al., *Nature Scientific Reports*, 2015]

Evidence of Nonlinear Conversion by Scattering in Lightning Generated Whistlers

Changing Turbulence Character Critical in the Radiation Belt

Fate of lightning generated whistlers in the ionosphere

Standard Quasi-linear Picture

- Increasing $k_{\perp} \Rightarrow$ enhanced dissipation (~ k_{\perp}^2)
- Wave dissipates as $k_{\perp}c/\omega_{pe} > 1$
- $\tau_{int} \sim \tau_{prop}$, during which $k_{\perp}c/\omega_{pe} < 1$

Cyclotron resonance time (τ_{int}) given by ($\omega - k_{||}V_{||} - n\Omega_{e}(r)$) $\simeq 0$

- Weak Turbulence Picture
- Increasing $k_{\perp} \Rightarrow$ enhanced NL scattering (~ Wk_{\perp}^{6}) • $k_{\perp}c/\omega_{pe} < 1$ maintained by NL scattering
- $\tau_{int} \sim \tau_{turb} >> \tau_{prop}$, NL scatter keeps $k_{\perp}c/\omega_{pe} < 1$

[Ganguli et al., *GRL*, 2012; Crabtree et al., *PoP*, 2012]

Small Scale Turbulence Properties: Coherent or Incoherent?

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• Analysis of in-situ data from NASA/Van Allen Probes

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Bayesian analysis of Van Allen Probe data

Bayesian Spectral Analysis of Chorus Element

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- Intensity corresponds to wave energy density
- Instantaneous frequency is plotted over time window
- Growth rate is used to adjust wave energy density over time window
- Color saturates at 10⁻¹¹ ergs

Small Scale Turbulence Properties: Strong or Weak Turbulence?

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- Observation in solar wind •
 - Turbulence energy spectrum non-Kolmogorov
 - Appearance of spectral steepening at $k_{\rho_i} \sim 1$
- Ongoing debate:

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- Origin of spectral steepening for shorter wavelengths
- Common belief: •
 - Spectral evolution dominated by Landau damping
 - Strong turbulence prevails at all scale sizes
- No good reason to reject weak turbulence for $k_{\rho_i} \ge 1$ in collisionless SW if Landau damping is negligible compared to NL rates
- Can Solar Wind Maintain Sufficiently Small $df_{0e}/dv_{||}$ to Ignore Landau Damping?

From Alexandrova et al. PRL, 2009, Cluster data

- Stable distributions can Landau damp waves and create plateau
- In SW Coulomb collision time and free path are long ($\sim 10^5$ sec, ~ 1 AU)
 - Can not thermalize within SW transit time
- Evolution of distribution function given by quasi-linear equation

Experimental Validation

Turbulence Onset

Efficiency

 $W_{scattered} \ \omega - \Delta \omega$

 $\gamma_{NL} \geq \gamma_L$

 $EM \Leftrightarrow ES$ conversion

 ∂W_{k_1}

25

20

15

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Effects of Spatial Variability

Origin of Strong of Spatial Variability in Near-Earth Space

- Plasma compression leads to strong spatial gradients, e.g.,
 - Boundary layers, dipolarization fronts, reconnection region, etc.
 - Scale sizes can become comparable to an ion gyro-radius or smaller
 - Kinetic treatment becomes necessary
- Use constants of motion to construct a distribution function H(r)

$$H_{\alpha} = mv^{2}/2 + e\Phi(x), \quad X_{g} = x + v_{y}/\Omega \qquad \qquad f_{o\alpha}(X_{g}, H_{\alpha}(x)) = \frac{N_{\alpha}}{(\pi v_{t\alpha}^{2})^{2}} Q_{\alpha}(X_{g}) e^{-\frac{H_{\alpha}(x)}{kT_{\alpha}}},$$

Guiding center distribution ٠

 X_{g1} X_{g2}

Obtain density

$$Q_{\alpha}(X_{g}) = \begin{cases} R_{\alpha} & , X_{g} < X_{g1} \\ R_{\alpha} + (S_{\alpha} - R_{\alpha}) \left(\frac{X_{g} - X_{g1}}{X_{g2} - X_{g1}} \right) & , X_{g1} < X_{g} < X_{g2} \\ S_{\alpha} & , X_{g} > X_{g2} \end{cases}$$

$$\int f_{0\alpha}(v, \Phi(x)) dv = n_{0\alpha}(\Phi(x)) dv$$

Use quasi-neutrality to determine the electrostatic potential

Effects of Transverse Electric Field Gradients

- Affects zeroth-order plasma dynamics
 - Particle orbits in a magnetized plasma are affected
 - Particles can move across magnetic field lines

$$\Omega \to \underbrace{\sqrt{\eta(\xi)}\Omega}_{\substack{\text{Re normalized}\\Gyro-frequency}}, \quad \eta(x) = 1 + \frac{1}{\Omega} \frac{dV_E(x)}{dx}$$

- Unique plasma distributions are created -
 - Temperature anisotropy in x and y directions possible

$$f_0(\xi, H) \approx \frac{n_0}{\sqrt{\eta(\xi)}} \left(\frac{\beta}{2\pi}\right)^{3/2} e^{-(\beta/2)(v_x^2 + \eta(\xi)(v_y - \langle v_y \rangle)^2)} e^{-(\beta/2)v_z^2}$$

- where

$$\xi = x + (v_y - V_E(\xi)), \quad \beta = 1 / v_{th}^2$$
$$V_E(\xi) = -cE(\xi) / B_0,$$

[Ganguli et al., Phys Fluids. 1988]

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Kelvin-Helmholtz $(\omega - k_v V_E) \ll \Omega_i, k_v \rho_i \ll 1$

$$\left(\frac{d^2}{dx^2} - k_y^2 + \frac{k_y V_E^*}{\omega - k_y V_E}\right)\phi_1(x) = 0$$

$$\left(\frac{\partial}{\partial t}\int dx \left(\frac{|E_1|^2}{8\pi} + \frac{n_{0i}m_i}{2}\frac{|cE_1|^2}{B_0^2} + \frac{n_{0i}m_i}{2}\frac{|x_1|^2 V_E(x)V_E^*(x)}{2}\right) = 0$$

$$\frac{V_E^2(x)}{No Waves} - \left(\frac{V_E(x + x_1)}{With Waves}\right)^2 = -|x_1|^2 V_E(x)V_E^*(x) + O(1/L^3)$$

$$\frac{\mathbf{IEDDI}}{No Waves} \left((\omega - k_y V_E) \sim n\Omega_i, k_y \rho_i \ge 1$$

$$U = \frac{\partial \omega D}{\partial \omega} \propto \omega (\omega - k_y V_E)$$

$$\frac{\partial \omega D}{\partial e^{-k_y V_E}} = -\frac{V_g U_H A_{y,z}}{Doppler-Shifted}$$

$$\frac{V_E(x)}{V_E(x + x_1)} = \frac{V_E(x)}{V_E(x + x_1)} = -\frac{V_E(x)}{V_E(x + x_1)} = -\frac{V_E(x)}{V_E(x + x_1)}$$

[Ganguli, *PoP*, 1997]

Laboratory Study of Compressed Plasma Layer

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21/2 D PIC simulation of EIH mode for $\rho_e < L < \rho_i$

Contours of electrostatic potential

LHDI x/L_x

 $\omega_{s} / \omega_{LH} = 0$ 0.5 0.75 0.5 1

 x/L_x [Romero and Ganguli, Phys. Fluids, 1993; GRL, 1994]

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Laboratory Study of Dipolarization Fronts

Dipolarization 0.3 w/w_{ce} 0.2 - \cdot k c / $\omega_{pe} \approx 3$ OLAR WIND 0.1 - $\Delta r_{\rm FWHM}$ 0.3 -EARTH ω/ω ce $k c / \omega \approx 6$ 0.2 -0.1 -**Electrostatic Potential** Densitv 2.4 (b) (a) Δr_{FWHM} 0.8 0.3 -^{1.6} θφ(x)/μ^e 0.8 200 n(x)/Ñ ω/ω ce 0.2 -0.4 $k_{\perp}c$ / $\omega_{pe} pprox$ 13 0.1 -0 4 0 2 0 4 6 x/p; x/p; r/r_s³ 0 $E_{x} = -ik_{x}\phi\left(1 + \frac{\overline{k}_{z}^{2}}{\overline{k}_{\perp}^{2}}\right)E_{y} = E_{x}\frac{i\omega}{\Omega_{e}\overline{k}^{2}} \qquad E_{z} = -ik_{z}\phi\left(\frac{\overline{k}^{2}}{1 + \overline{k}^{2}}\right)$

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Laboratory Data from

EMFISIS Burst Mode Waveform Data from Van Allen Probes

Seconds after 2012-11-14 05:40:32.437892

Ionospheric Plasma Phenomena: Auroral Region

Good agreement with resonance condition

[Ganguli et al, *JGR*, 1994]

J. Bonnell, Ph.D. thesis, Cornell U, 1996]

Physics of Multi-Ion Species Plasma

Since $E_0 = 0$, $J_0 = 0$, Quasi-neutral plasma with $k_7 = k_y = 0$;

$$J_{1x} = -en_{0i}\frac{i\omega}{\Omega_i}\frac{cE_{1x}}{B_0} + Zen_{0d}\frac{cE_{1y}}{B_0}$$

$$\nabla \cdot J_1 = 0 \Longrightarrow ik_x J_{1x} = 0$$

$$\frac{E_{1x}}{E_{1y}} = -i\left(\frac{Zn_{0d}}{n_{0i}}\right)\left(\frac{\Omega_i}{\omega}\right) = -i\left(\frac{n_{0e}}{n_{0i}}\right)\left(\frac{\Omega_r}{\omega}\right) \approx -i\left(\frac{\Omega_r}{\omega}\right) \qquad \Omega_r = \frac{Zn_d}{n_e}\Omega_r$$

Near resonance ($\omega \approx \Omega_0$): $E_{1x} = -iE_{1y}$

- Important differences:
 - only a mean fluid rotation
 - $\omega \approx \Omega_{\gamma}$ implies a wave resonance, k $\rightarrow \infty$, wave predominantly ES
 - $\omega \approx \Omega_0$ implies a wave cut-off, k $\rightarrow 0$, wave predominantly EM

Energy Density of the Rotation Waves

$$\varepsilon_{w} = \frac{\left\langle B_{1}^{2} \right\rangle}{\underbrace{8\pi}_{field-energy}} + \underbrace{m_{i}n_{i}}_{kinetic-energy} \frac{\left\langle V_{1}^{2} \right\rangle}{2} = \frac{\left\langle B_{1}^{2} \right\rangle}{8\pi} \left(1 + \frac{\omega^{2}}{\omega^{2} - \Omega_{r0}^{2}}\right)$$

- Near ($\omega \approx \Omega_r$) most of the wave energy is kinetic energy of light ion rotation
- Unlike classical 2-component MHD, the ions can possess a lot of energy
- A possible source of ion energization

Ponderomotive force (for $k_v = k_z = 0$)

$$\vec{F}_{p} = -\frac{\partial}{\partial x} \left(\frac{\left|\vec{B}_{1}\right|^{2}}{16\pi} \frac{\Omega_{r0}^{2}}{\left(\omega^{2} - \Omega_{r0}^{2}\right)} \right) \hat{x} + k_{x} \frac{\left|\vec{B}_{1}\right|^{2}}{8\pi} \frac{\Omega_{r0}^{2}}{\left(\omega^{2} - \Omega_{r0}^{2}\right)} \hat{y}$$

- Ponderomotive force can be magnified by the rotation resonance
- Ideal for 1-dimensional force balance

Since Ω_r represents a cut-off the wave is not damped as $\omega \rightarrow \Omega_o$

- Consider a 3-species (ion, Electron, and dust) plasma
- For short wavelength ($kl_d >> 1$) recover Alfven and magnetosonic waves with minor frequency corrections

$$\omega = kV_A \left(1 + \frac{1}{2k_x^2 l_d^2}\right) \qquad \omega = k_z V_A \left(1 - \frac{1}{2k_x^2 l_d^2}\right) \qquad l_d = \frac{V_A}{\Omega_r} \qquad \Omega_r$$

Magnetosonic branch

Alfven branch

Dust Hall Length

• For long wavelength ($kl_d << 1$) two new branches appear

 $\omega^{2} = \Omega_{r}^{2} + (k^{2} + k_{z}^{2})V_{A}^{2}$

Alfven-Magnetosonic Hybrid Wave Similar to Langmuir waves

 $k_{z} \approx 0$

 $\omega^2 = k_z^2 (k_z^2 + k_x^2) V_A^4 / \Omega_r^2$

Ion Whistler Wave

[Ganguli and Rudakov, PRL, 2004; Ganguli and Rudakov, PoP, 2005]

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$$\approx \frac{Zn_d}{n_e} \Omega_i$$

New "Rotation" Frequency

$$\rightarrow \omega^{2} = \Omega_{r}^{2} + k_{\perp}^{2} V_{A}^{2}$$
$$\omega^{2} = \omega_{pe}^{2} + k^{2} V_{th}^{2}$$
Langmuir wave

Turbulence in Multi-Ion Species Plasma: Strong? Weak? Both? Composite?

Strong turbulence? Similar to Langmuir turbulence

$$i\frac{\partial \mathbf{v}_{1s}}{\partial t} = \partial \Omega \mathbf{v}_{1s} - \frac{V_A^2}{2\Omega_r}\frac{\partial^2 \mathbf{v}_{1s}}{\partial x^2}$$

$$\partial \Omega = \delta(\frac{ZeBn_d}{m_i cn_e}) = \Omega_r \frac{\delta n_d}{n_{d0}} = \Omega_r \frac{\delta B}{B_0}$$

- Fast time-scale is $\Omega_r (\equiv \omega_{pe})$

- ponderomotive force
- Solutions: Solitons

Unlike Langmuir Waves no Dissipation as Wavelength Approaches l_{d}

$$i\frac{\partial \mathbf{v}_{1s}}{\partial \mathbf{t}} = -\Omega_r \frac{\left|\mathbf{v}_{1s}\right|^2}{V_A^2} \mathbf{v}_{1s} - \frac{V_A^2}{2\Omega_r} \frac{\partial^2 \mathbf{v}_{1s}}{\partial x^2}$$

Slow time-scale is dust kV_{Δ} ($\equiv kc_s$)

Long time average: t >> 1/ Ω_r ,1/ Ω_d Nonlinear frequency shift, $\delta \omega$, due to

The nonlinear Schrodinger Equation

Turbulence in Multi-Ion Species Plasma: Strong? Weak? Both? Composite?

Weak turbulence? Similar to Kolmogorov Cascade of Alfven waves

$$(\omega^2 = \Omega_r^2 + k_x^2 V_A^2) \rightarrow \omega = k_z V_A \left(1 - \frac{1}{2} k_x^2 l_d^2 \right) \text{ and } \omega = k V_A \left(1 - \frac{1}{2} k_x^2 l_d^2 \right)$$

 $+1/2k_x^2l_d^2$

Weak turbulence

Short wavelength $kl_d > 1$

 Strong turbulence dominates for k << k_d but breaks down for k ~ k_d

• Collapse towards k_d pumps weak turbulence for $k >> k_d$

Peak in energy density at k_d
Typical structure scale size ~ l_d

$$= \Omega_r / V_A \qquad \Omega_r \approx \frac{Z n_d}{n_e} \Omega_i$$

Astrophysical Relevance

Artist Rendition Based on Observations

Molecular Clouds

This cloud of gas and dust is being deleted. Likely, within a few million years, the intense light from bright stars will have boiled it away completely. The cloud has broken off of part of the Carina Nebula, a star forming region about 8000 light years away. CREDIT: Hubble Heritage Team (STScI/AURA), N. Walborn (STScI) & R. Barbß (La Plata Obs.), NASA.

- $kV_{\Delta} \sim \Omega_r$ defines structure (filament) scale size
- $l_{\rm d} \sim V_{\rm A} / \Omega_{\rm r} \sim (c / \omega_{\rm pi})(n_{\rm e} / Zn_{\rm d})(n_{\rm i} / n_{\rm e})^{1/2}$
- $n_e \sim 10^{-3}$ cc, $n_d \sim 10^{-8}$ cc, c / $\omega_{pi} \sim 10^9$ cms
- $l_{\rm d} \sim 10^{14} \, {\rm cms} \sim 10 \, {\rm AU}$

[Ganguli and Rudakov, **PRL**, 2004; Ganguli and Rudakov, **PoP**, 2005]

Astrophysical Turbulence and Transport: Kolmogorov Type Cascade and/or Strong Turbulence?

In 1D case there is no collapse

- Repeated scatterings of rotation waves leads to longer wavelengths
 - Dispersion progressively vanishes
 - Reminiscent of Bose-Einstein Condensation (BEC)
 - The rotation frequency represents the ground state

$$(\omega^2 = \Omega_r^2 + k_x^2 V_A^2) \implies (\omega^2 \approx \Omega_r^2)$$

- Condensates are long-lived structures
 - Condensate scale size L >> l_d

- Many inherent problems with in-situ measurements can be addressed through laboratory experiments
 - Space-time ambiguity
 - Unsteady plasma
- Provide complete characterization of a physical process
 - Repeated measurements possible in laboratory
- Laboratory experiments of triggered emission at NRL have led to a more comprehensive analysis of NASA/Van Allen Probe chorus data to show
 - Stepwise nature, presence of multiple waves, 3D wave propagation, signatures of induced scatterings, etc.
- Led to deeper understanding of the cause and effects of transverse electric fields
 - New class of broadband waves were found correlated with plasma compression which clarified unexplained auroral observations
 - This knowledge is now being used to understand the plasma dynamics of compressed layers, e.g., dipolarization fronts

